

# Course: Optics, forces & development

**In vivo 3D-microscopy for the analysis of cell behaviour in developing embryos**

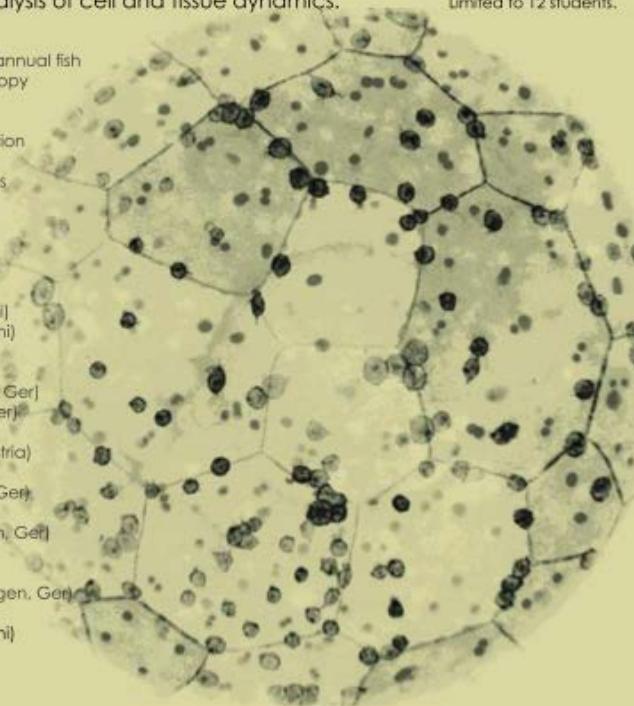
Santiago – Chile, January 14-29<sup>th</sup>, 2013

This practical and theoretical course is aimed at graduate students from Latin America interested in the use of optics and microscopic techniques for *in vivo* 3D visualisation and analysis of cell and tissue dynamics.

Limited to 12 students.

**Topics:**

- . Development of zebrafish and annual fish
- . Confocal and spinning microscopy
- . Light sheet microscopy
- . Super-resolution microscopy
- . Photoactivation and laser ablation
- . In vivo electroporation
- . Force estimation in cells & tissues
- . Optical tweezers
- . Particle tracking
- . Image processing and analysis



**Teachers:**

- . Roberto Bernál (U. Santiago, Chil)
- . Sebastián Brauchi (U. Austral, Chil)
- . Miguel Concha (U. Chile, Chil)
- . Mauricio Cerdá (U. Chile, Chil)
- . Jörg Enderlein (Univ. Göttingen, Ger)
- . Nikta Fakhri (Univ. Göttingen, Ger)
- . Steffen Hörtel (U. Chile, Chil)
- . Carl-Philipp Heisenberg (IST, Austria)
- . Jorge Jara (U. Chile, Chil)
- . Ulrich Kubitscheck (Univ. Bonn, Ger)
- . Omar Ramírez (U. Chile, Chil)
- . Florian Rehfeldt (Univ. Göttingen, Ger)
- . German Reig (U. Chile, Chil)
- . Felipe Santibáñez (U. Chile, Chil)
- . Christoph Schmidt (Univ. Göttingen, Ger)
- . Jan Spille (Univ. Bonn, Ger)
- . Juan Pablo Staforelli (CEFOP, Chil)

**Organisers:**

- . Miguel Concha (U. Chile)
- . Steffen Hörtel (U. Chile)

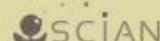
Travel Fellowships will be available. Indicate your interest in the application.

**To apply send:**

- . Curriculum Vitae
  - . Letter of Intention
  - . Reference from supervisor/mentor
- To: [mconcha@med.uchile.cl](mailto:mconcha@med.uchile.cl)

**Deadline for application** - December 26<sup>th</sup> 2012

**Results** - December 28<sup>th</sup> 2012



UNIVERSIDAD  
DE CHILE

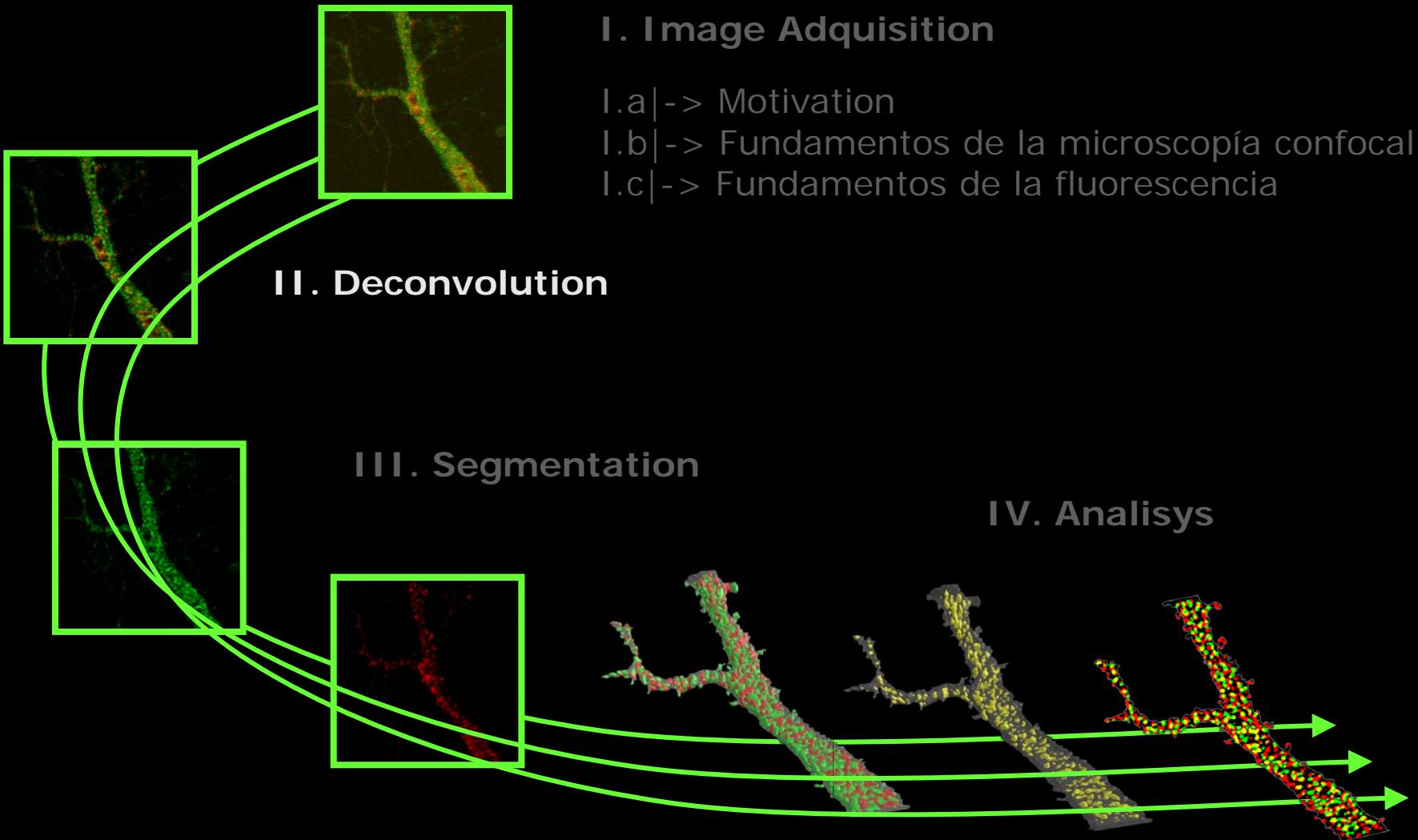
**CONICYT**

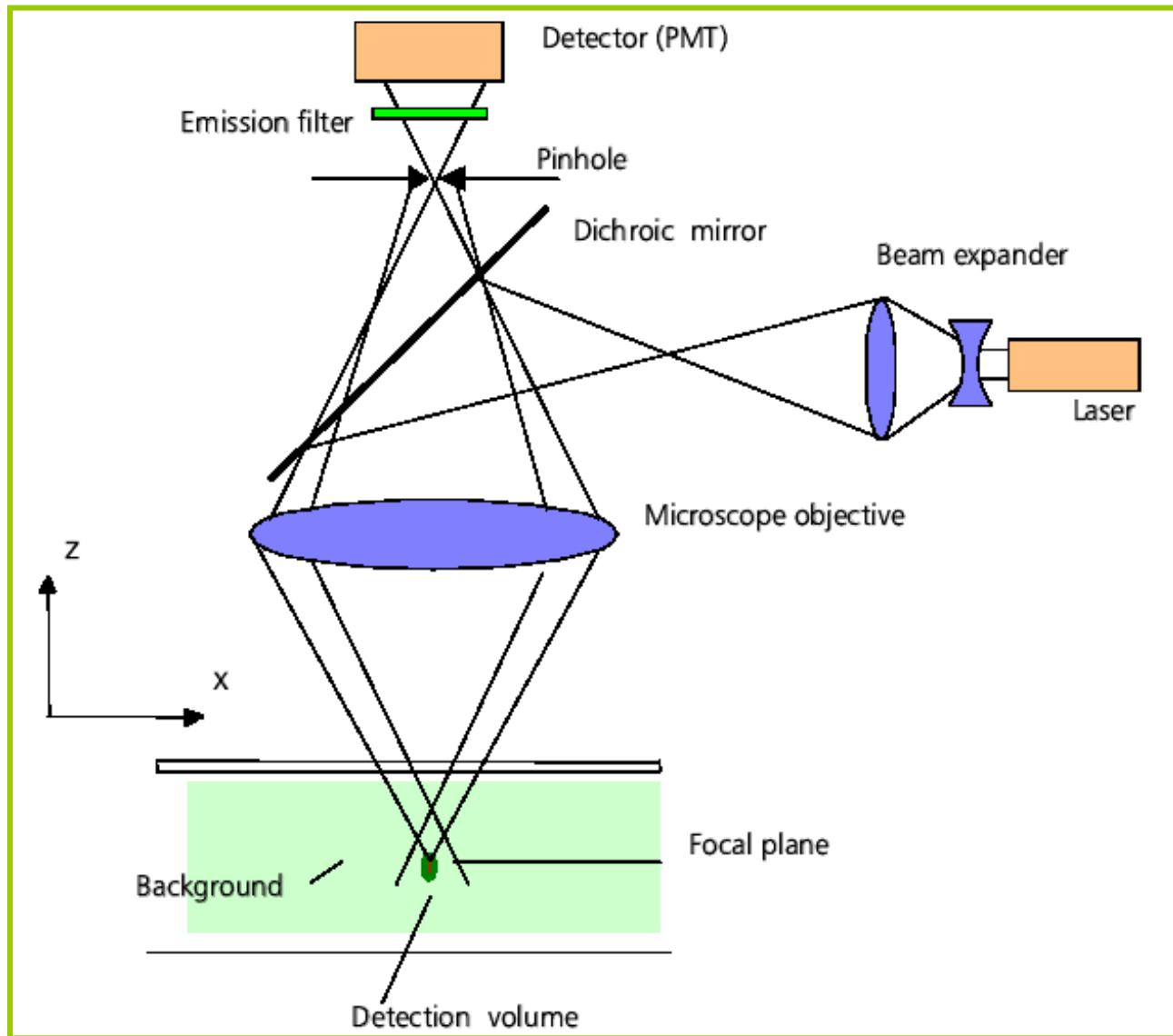
PONDECYT 1120558, 1120579 & 3130598  
PONDEF D1111096



CIENTÍFICA  
CULTURAL  
INICIATIVA  
ICM  
CHILE  
ICM P09-015-F

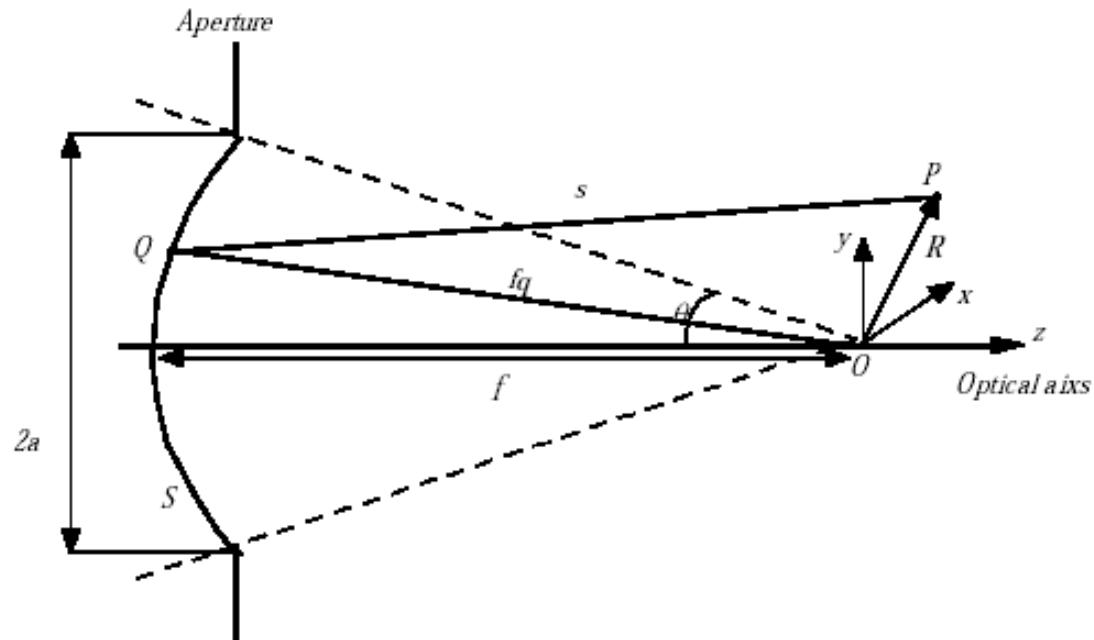






## From Geometric Optics to Diffraction Theory:

**Diffraction:** The deviation of an electromagnetic wavefront from the path predicted by geometric optics when the wavefront interacts with a physical object such as an opening or an edge.



**Figure 2.1** Diffraction of a converging spherical wave at a circular aperture

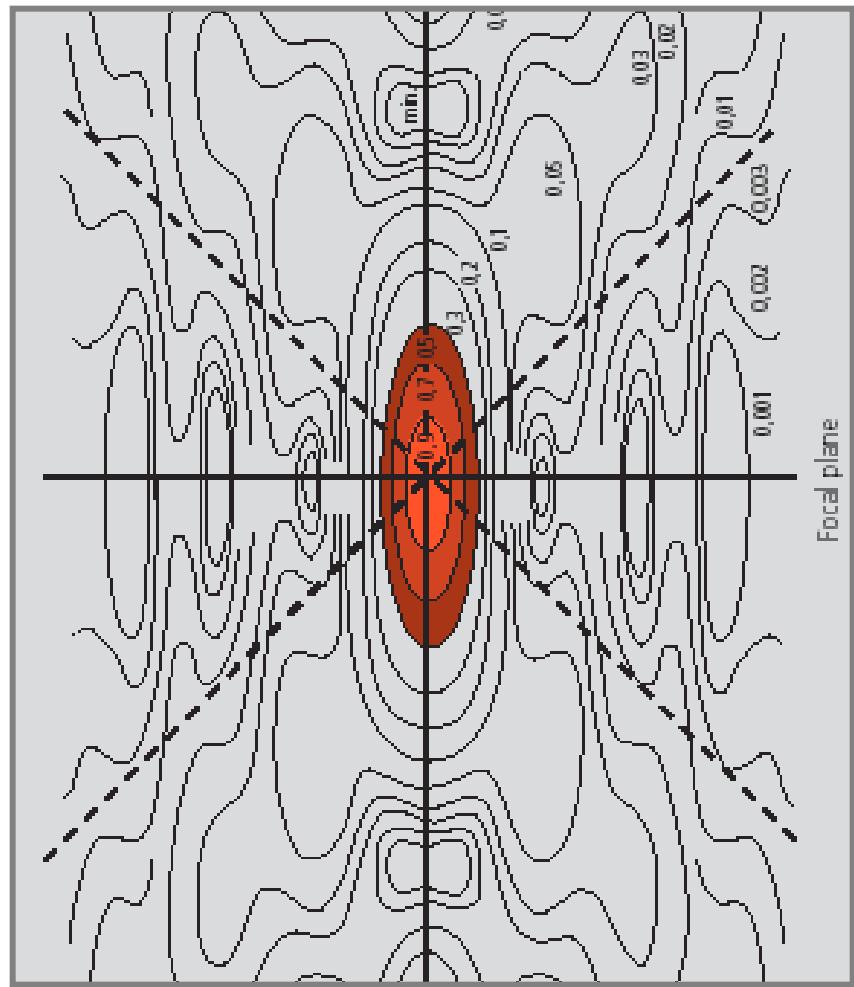
Óptica no-geométrica /  
Teoría de difracción

$$\text{PSF} = |U|^2 = f(J_0)$$

U, Integral de Difracción de Kirhoff

$J_0$ , Serie de funciones de Bessel

(Born & Wolf, Principles of Optics, 6th edition 1988,  
Pergamon Press)



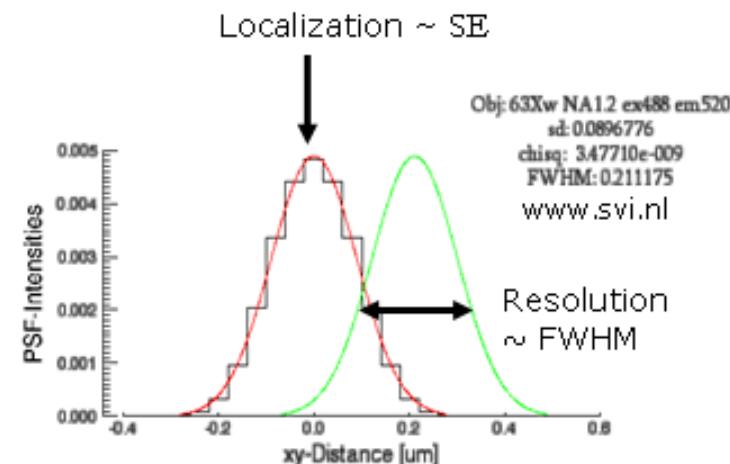
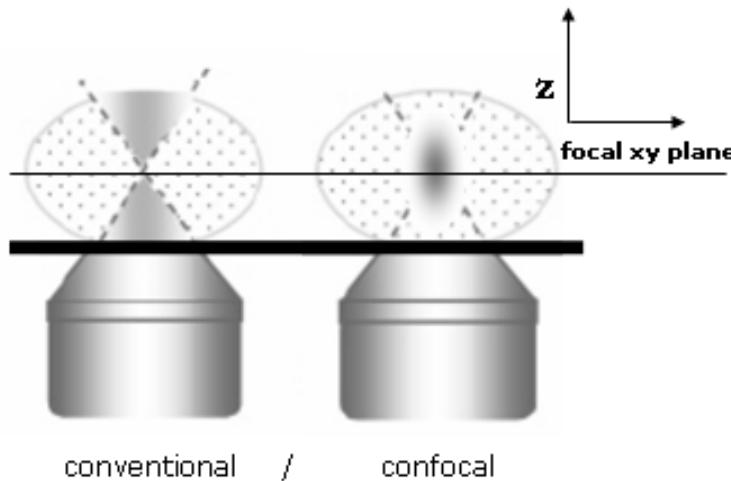
## | Diffraction limited microscopy

E. Abbe ( $\dagger$  1905)

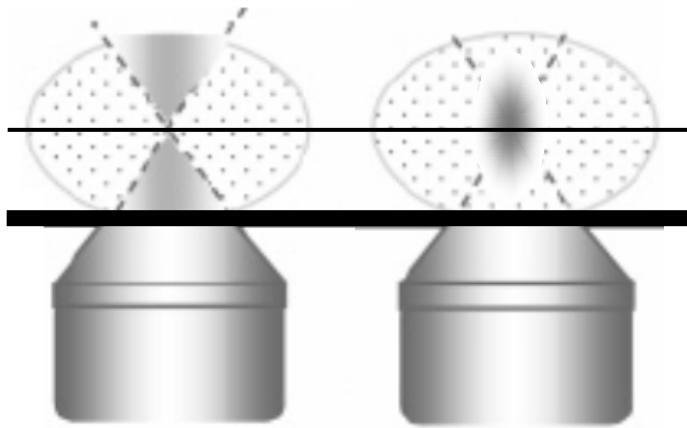
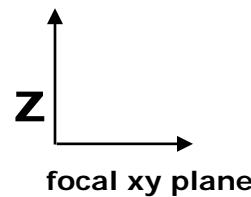


$$\lambda / 2 \cdot \text{NA} \sim \lambda / 2 \quad \text{Resolution (Full Width at Half Maximum, FWHM)}$$

$$\text{FWHM} / N^{1/2} \quad \text{Localization, } N \text{ number of photons}$$



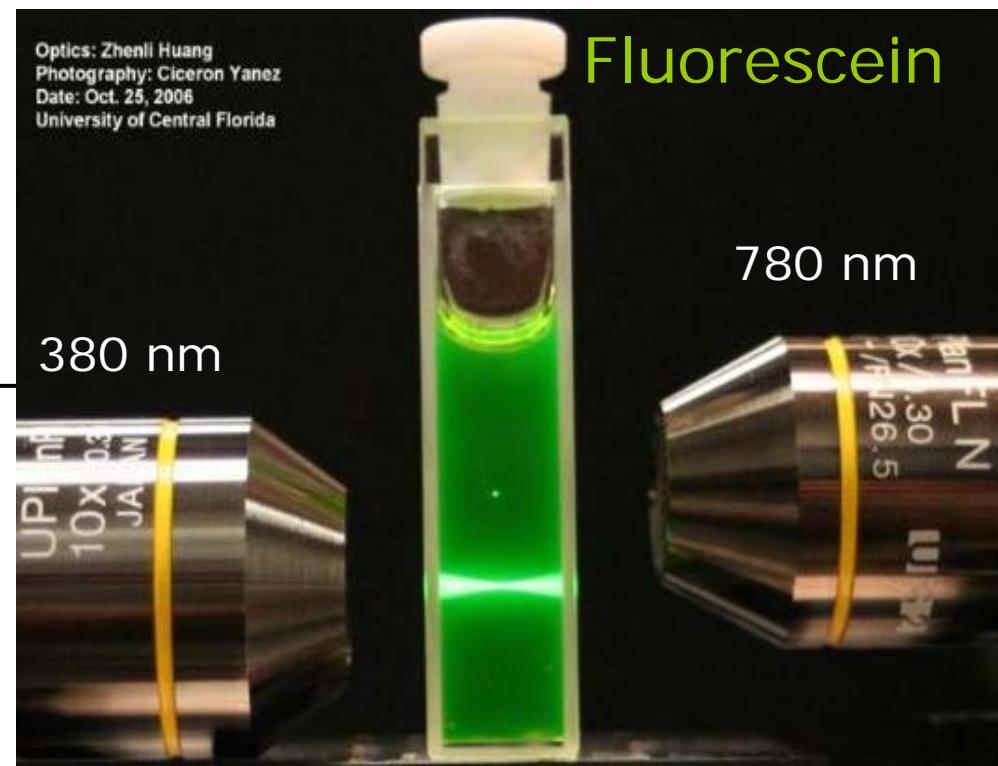
| Best localization: confocal microscopy



convencional

/

confocal



# | -> Beyond diffraction

M Goeppert-Mayer  
1906-1972



M Gustafson  
1960-2011



S Hell  
MPI Göttingen  
BIOQUANT HdG



E Betzig  
Janelia Farm



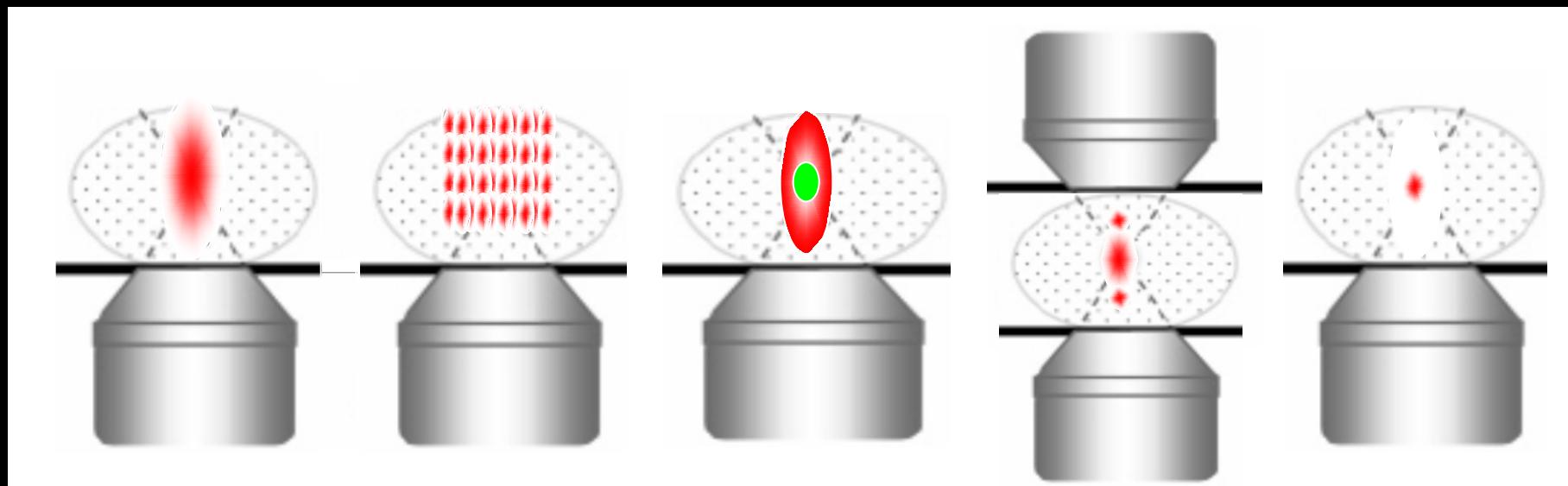
$\text{FWHM}(xy) \sim \lambda/2$

$\sim \lambda/4$

$\sim \lambda/\infty$

$\sim \lambda/4$

$\sim \lambda/100$



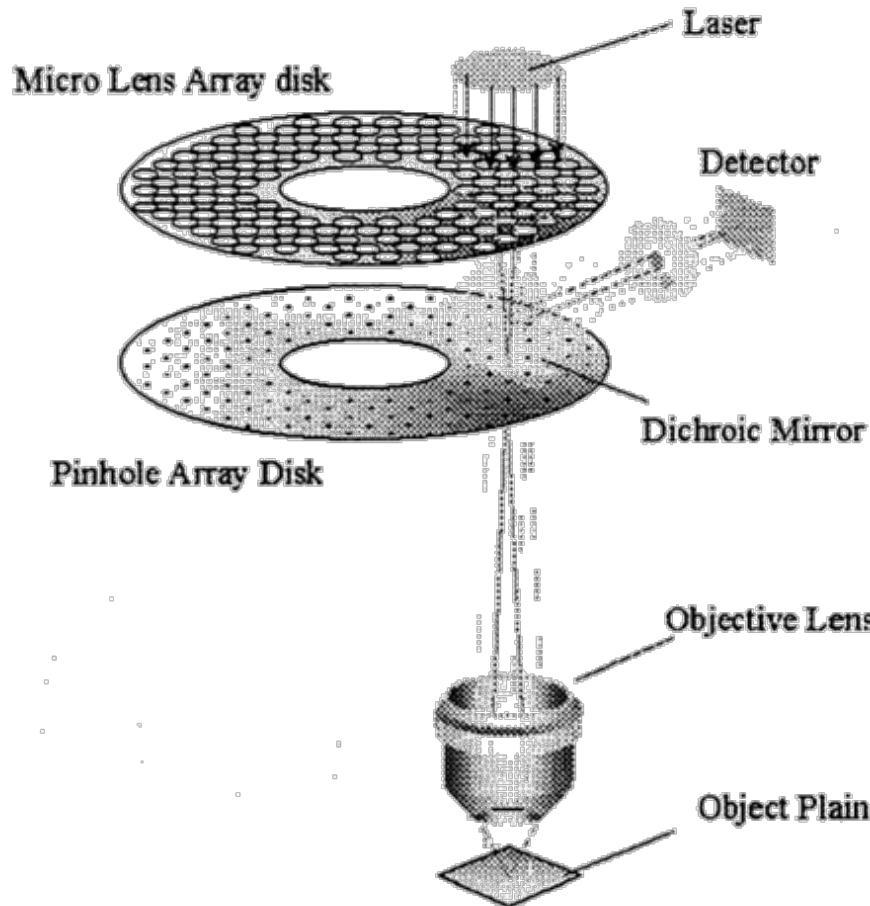
2-photon

SIM

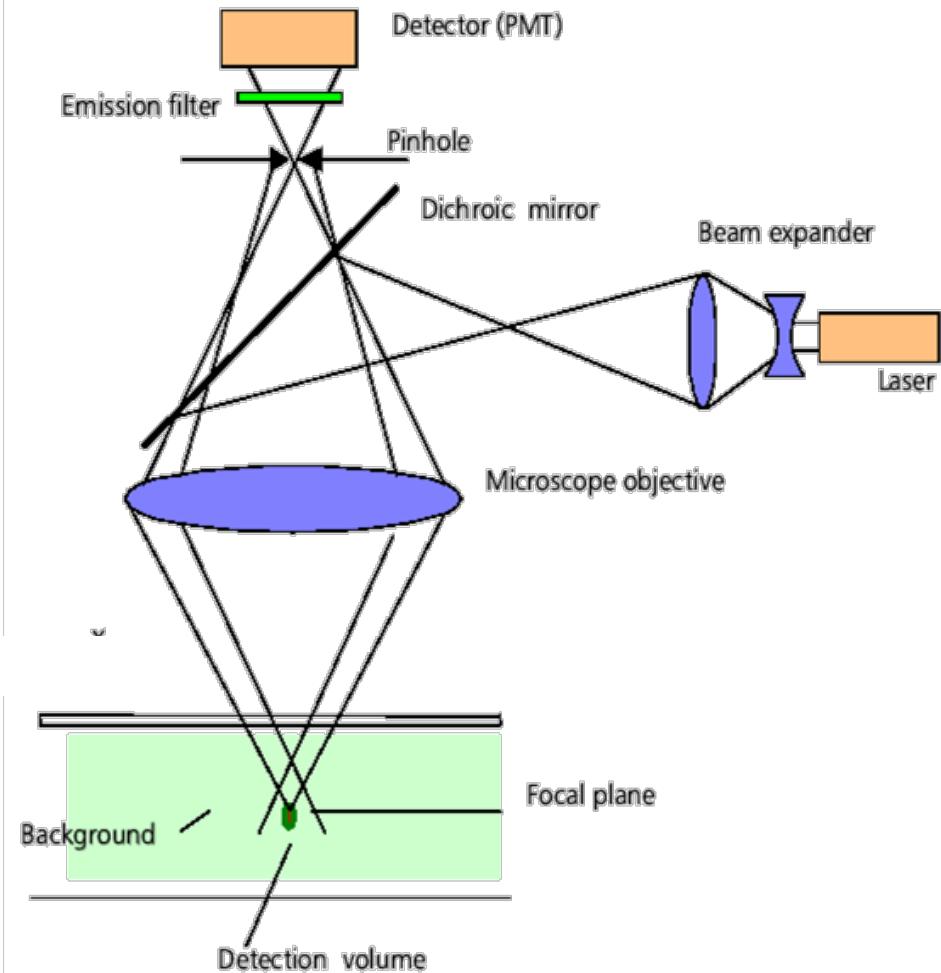
STED

4- $\pi$

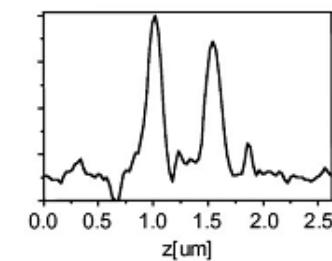
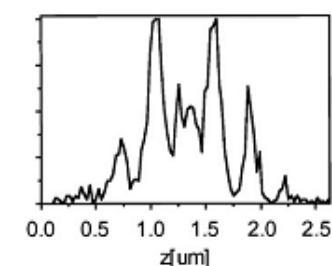
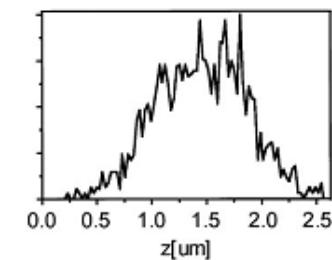
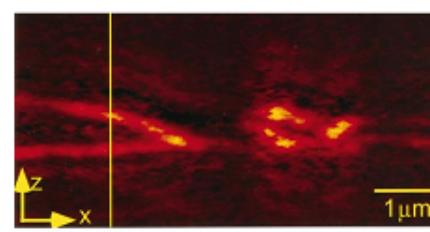
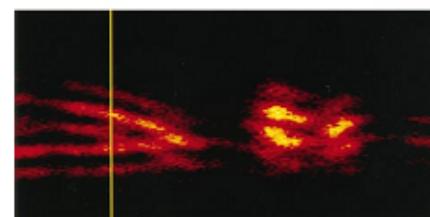
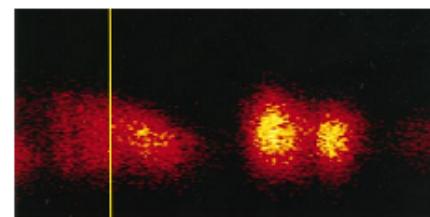
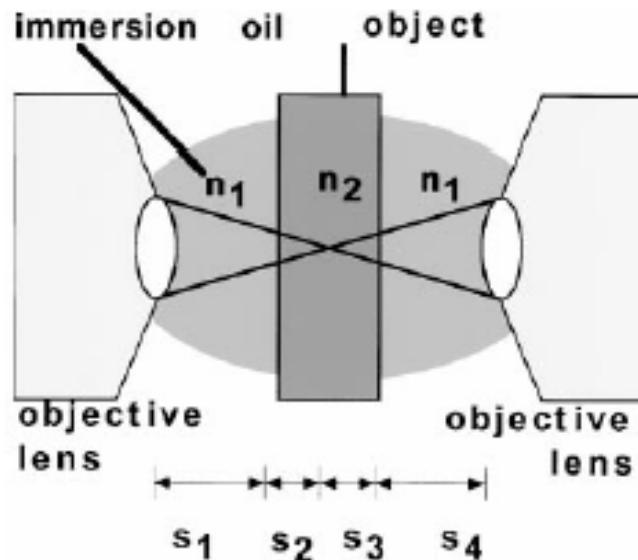
PALM



spinning disk



confocal

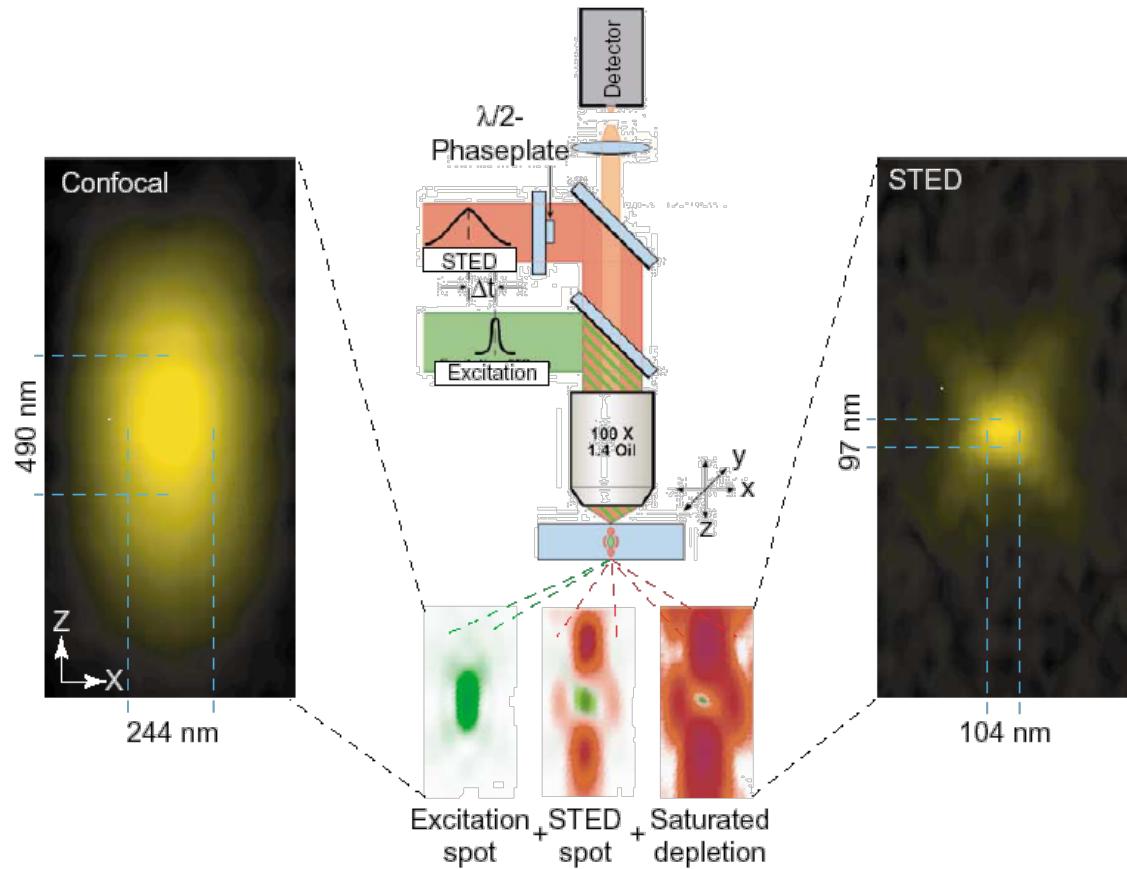


## 4Pi-Confocal Imaging in Fixed Biological Specimens

Martin Schrader,\* Karsten Bahlmann,\* Günter Giese,# and Stefan W. Hell\*  
 Biophysical Journal Volume 75 October 1998 1659–1668

# STED Microscopy

## Stimulated Emission Depletion

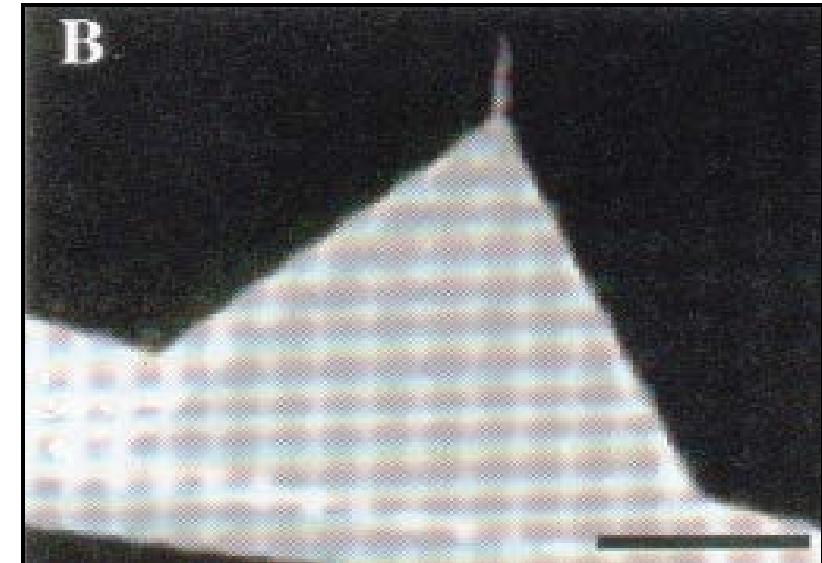
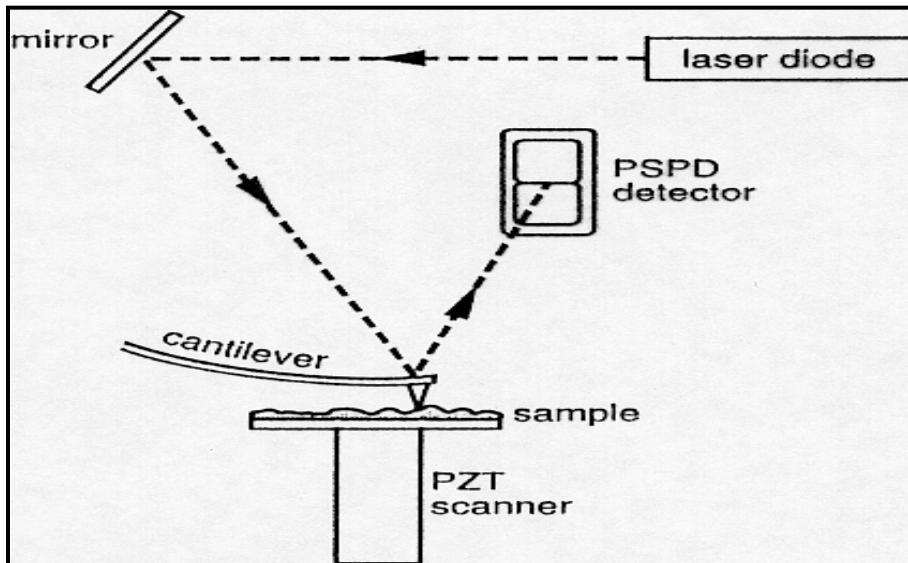


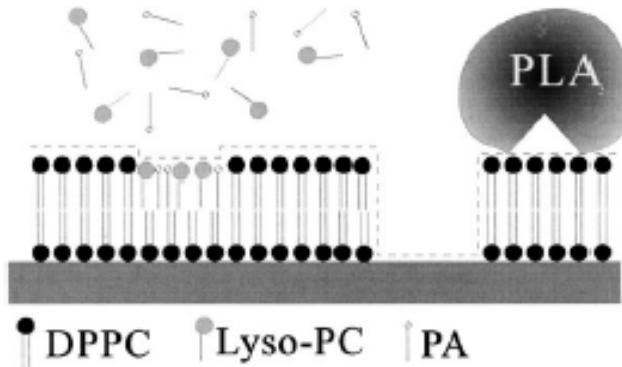
**Concepts for nanoscale resolution in fluorescence microscopy**  
 Stefan W Hell\*, Marcus Dyba<sup>1</sup> and Stefan Jakobs<sup>2</sup>

Current Opinion in Neurobiology 2004, 14:599–609

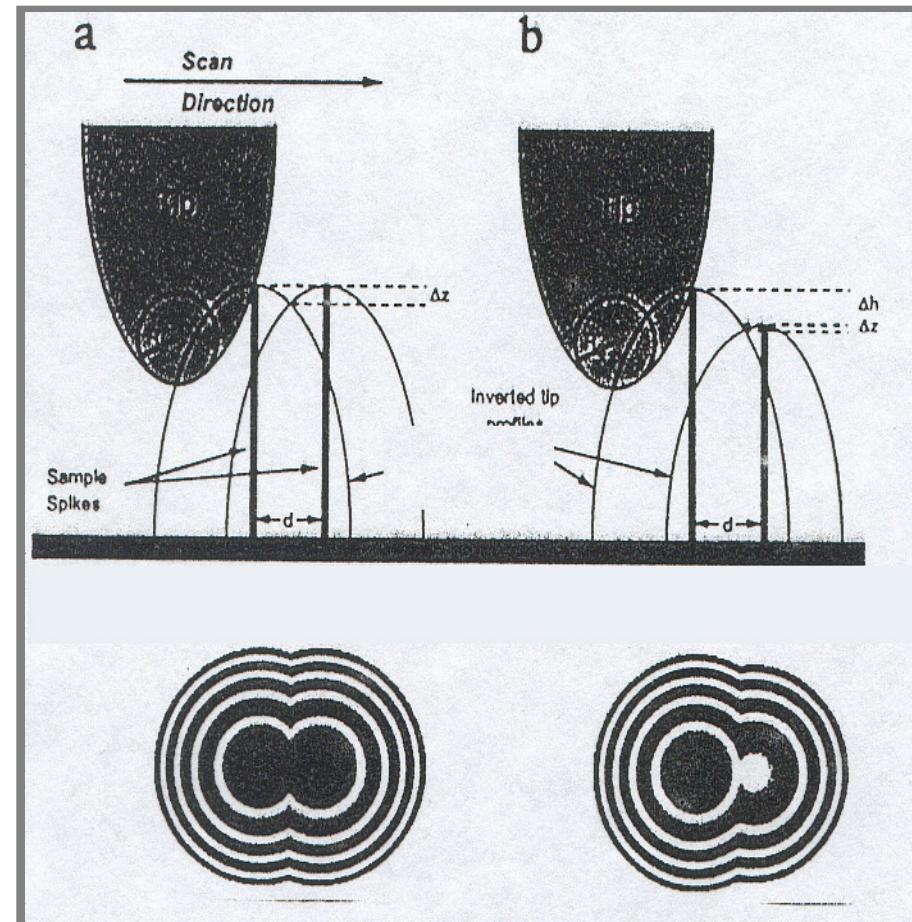
AFM allows the investigation of structural and functional properties of biomolecules in liquid environments, by a unique combination of :

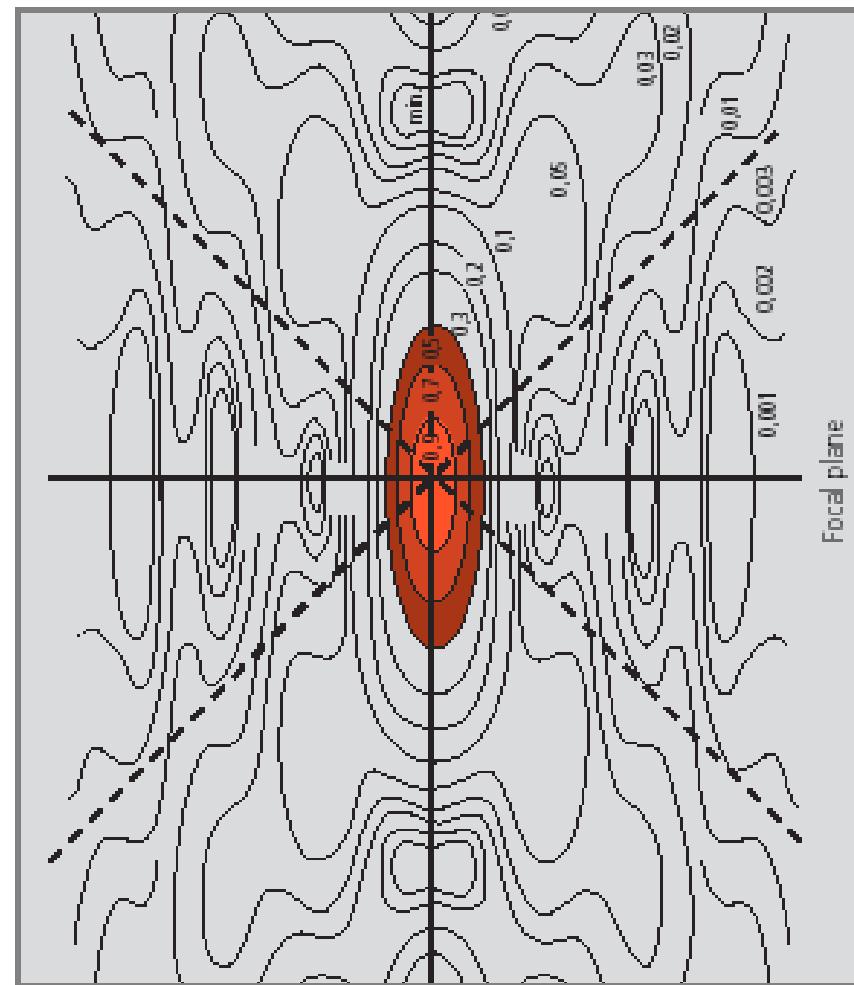
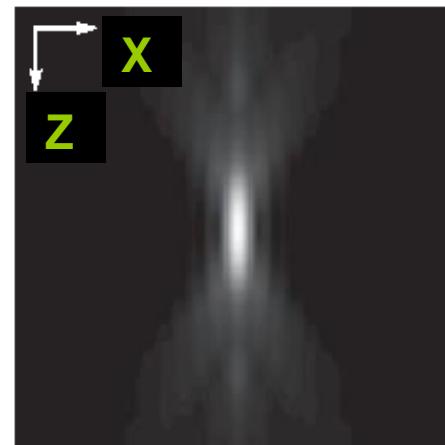
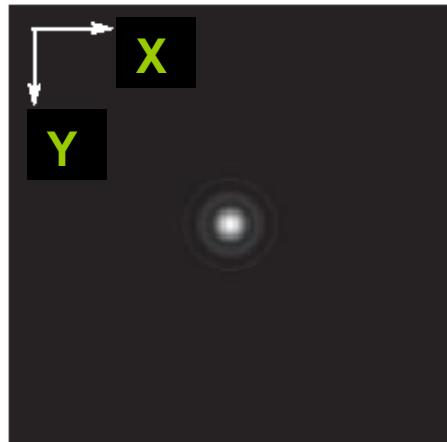
- **subnanometer** spatial resolution
- **millisecond** temporal resolution
- **piconewton** force sensitivity

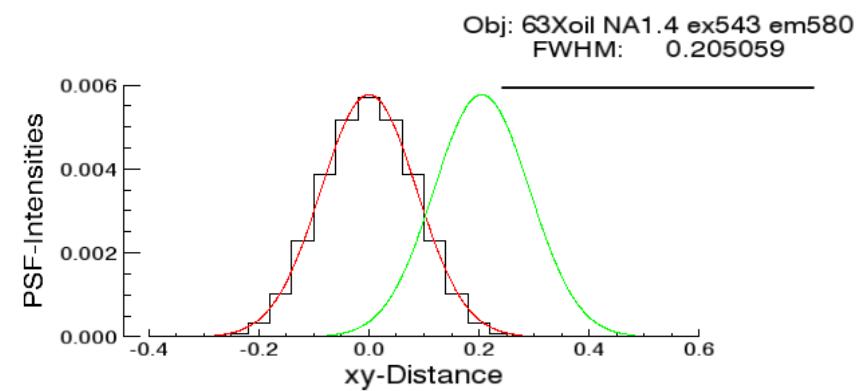
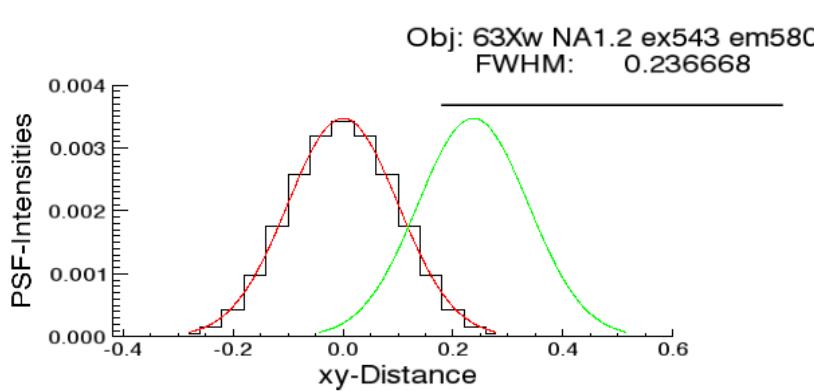
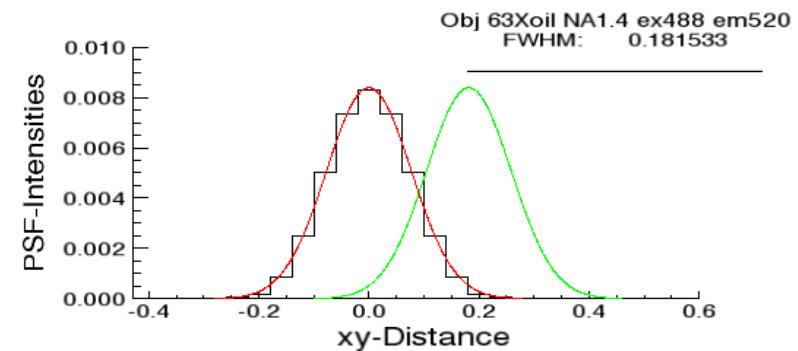
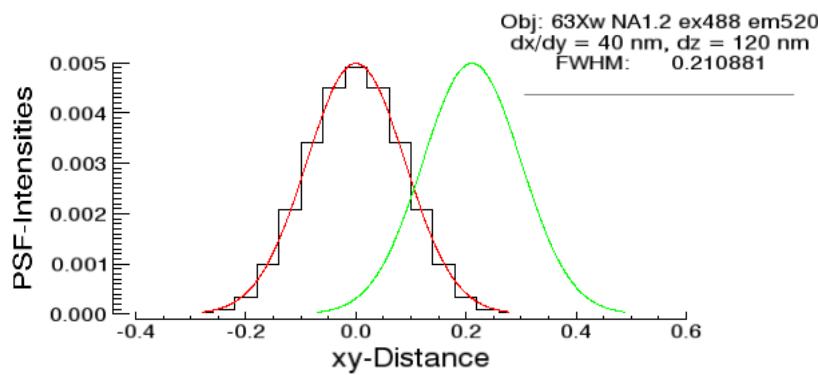


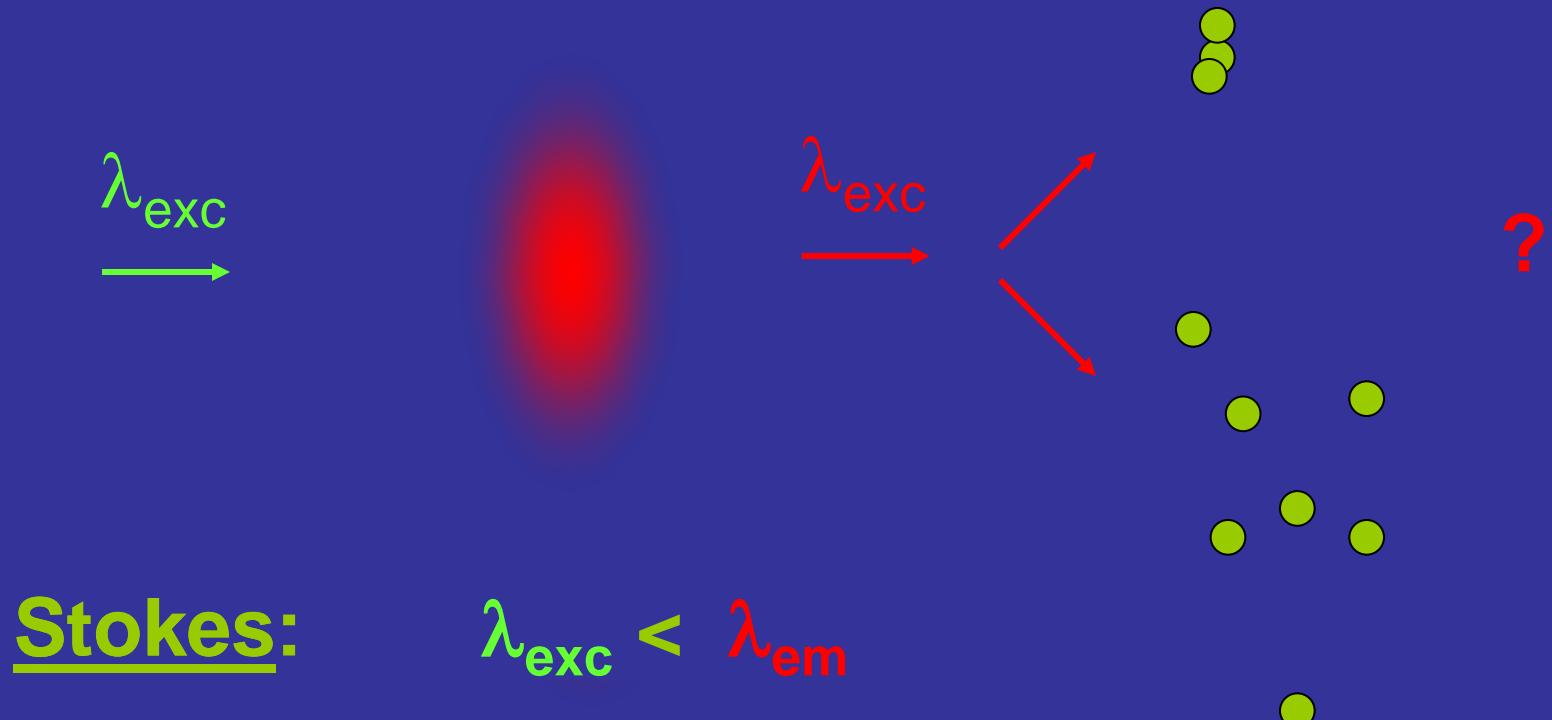


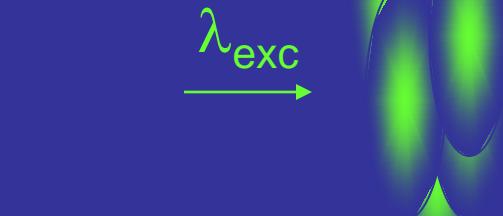
M Grandbois et al. (1998) *Biophys J.*



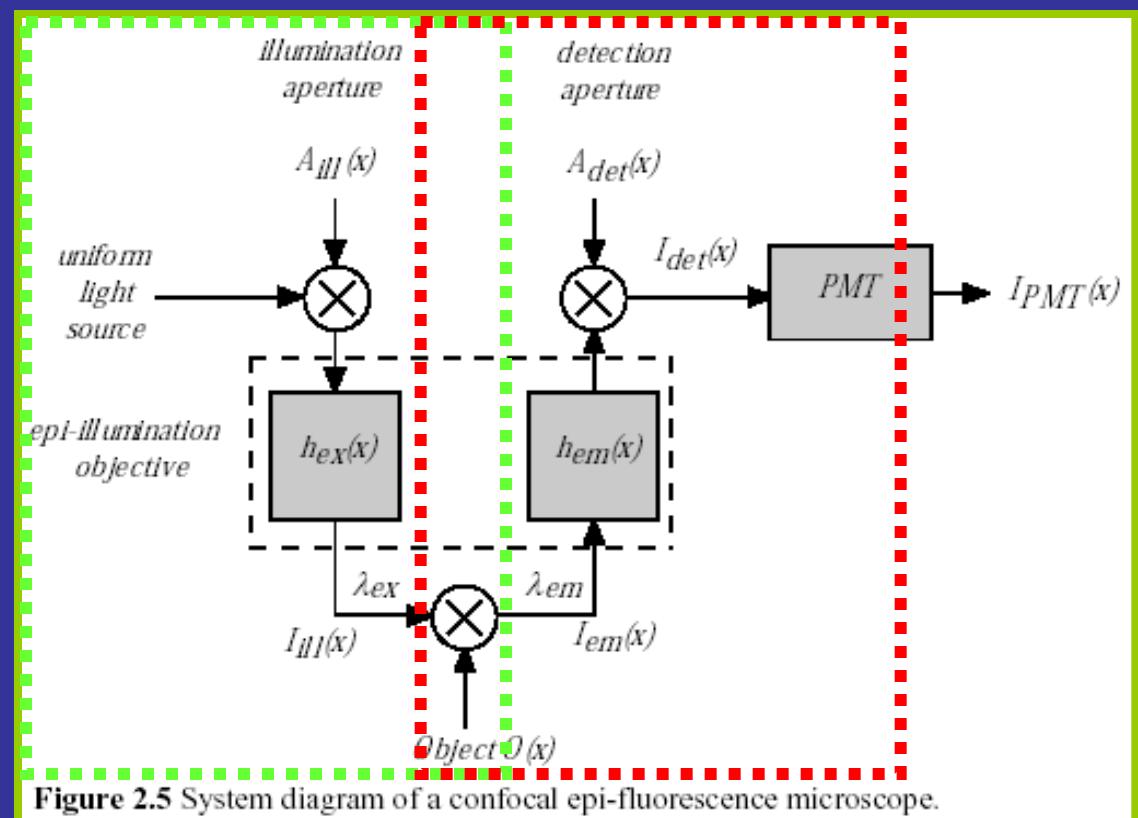
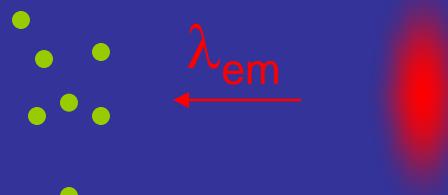




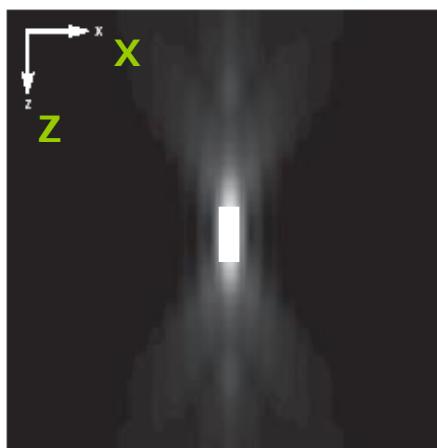




Stokes:  $\lambda_{\text{exc}} < \lambda_{\text{em}}$   
 $n(\lambda_{\text{exc}}) > n(\lambda_{\text{em}})$



# | -> Convolution



**PSF:** Point Spread Function

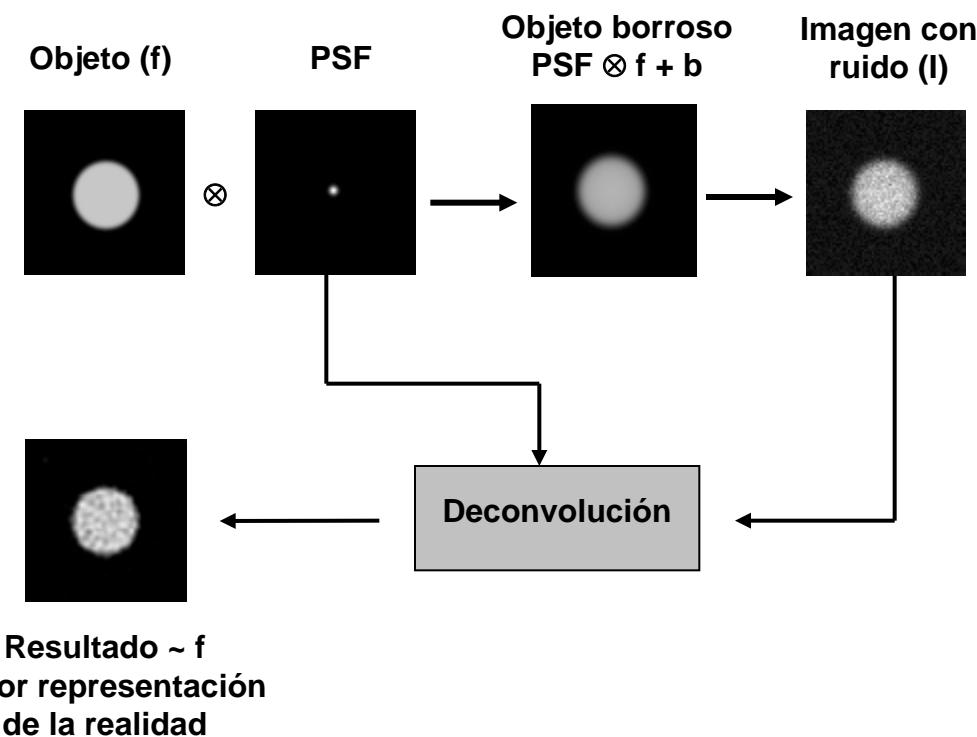
$$N(PSF(x, y, z) \otimes f(x, y, z) + b(x, y, z)) = I(x, y, z)$$

**f:** Object Function

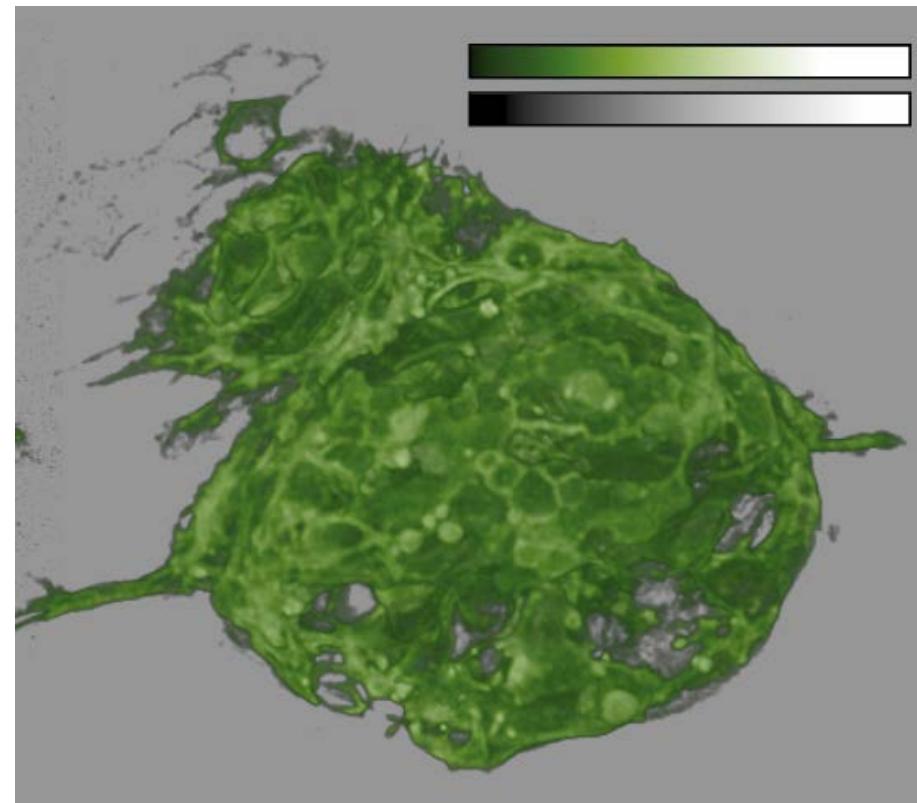
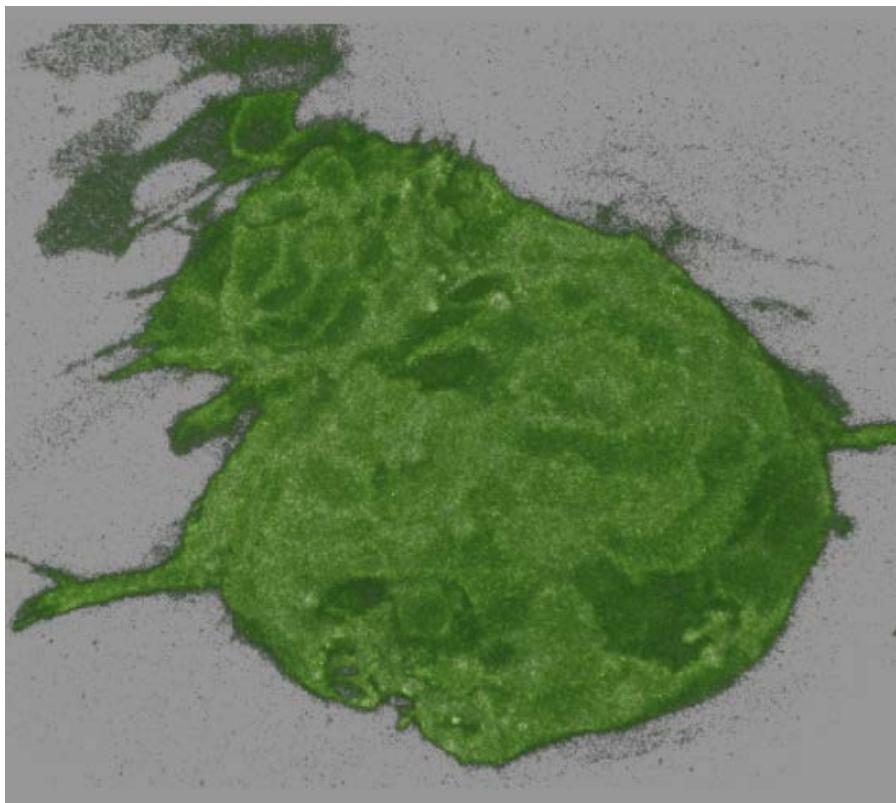
**b:** Offset Function

**I:** Image Matrix

**N:** Noise Function



# | -> Deconvolution



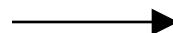
**PSF:** Point Spread Function

**f:** Object Function

**b:** Offset Function

**I:** Image Matrix

**N:** Noise Function



$$N(PSF(x, y, z) \otimes f(x, y, z) + b(x, y, z)) = I(x, y, z)$$

 <b>Calculator</b>	<input checked="" type="radio"/> confocal <input type="radio"/> widefield <input type="radio"/> nipkow <input type="radio"/> 4Pi	Select one
<u>Numerical aperture</u>	1.3	
<u>Excitation wavelength</u>	488 (nm)	
<u>Emission wavelength</u>	520 (nm)	
<u>Number of excitation photons</u>	1	
<u>Backprojected pinhole radius</u>	250 (nm)	
<u>B.P. distance between pinholes</u>	2.53 Only for Nipkow disks ( $\mu\text{m}$ )	
<u>Lens medium refractive index</u>	1.515	
<u>Specimen medium refractive index</u>	1.45	
<u>Acquisition depth</u>	0 ( $\mu\text{m}$ )	
<input type="checkbox"/> Calculate also PSF		

**PSF:** Point Spread Function

**f:** Object Function

**b:** Offset Function

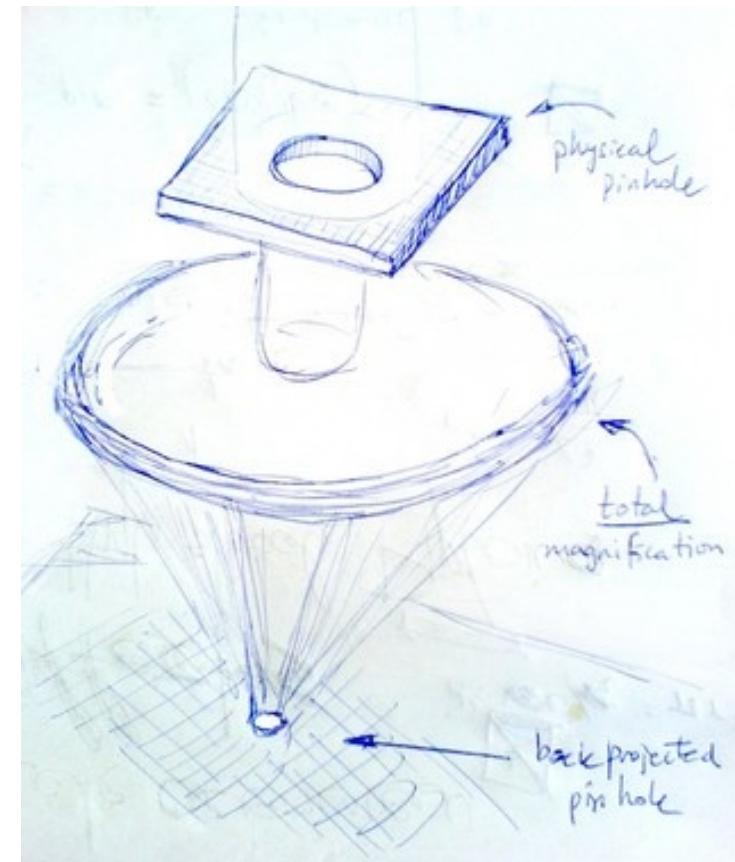
**I:** Image Matrix

**N:** Noise Function

$$N(PSF(x, y, z) \otimes f(x, y, z) + b(x, y, z)) = I(x, y, z)$$

## Backprojected confocal pinhole

<http://support.svi.nl/wiki/NyquistCalculator>



**PSF:** Point Spread Function

**f:** Object Function

**b:** Offset Function

**I:** Image Matrix

**N:** Noise Function

$$N(\mathbf{PSF}(x, y, z) \otimes f(x, y, z) + b(x, y, z)) = I(x, y, z)$$

## Biorad

- [Biorad MRC 500, 600 and 1024](#)
- [Biorad Radiance](#)

## Olympus

- [Olympus FV300](#)
- [Olympus FV500](#)
- [Olympus FV1000](#)

## Leica

- [Leica confocals TCS 4d, SP1 and NT](#)
- [Leica confocal SP2](#)
- [Leica confocal SP5](#)

## Zeiss

- [Zeiss LSM410 inverted](#)
- [Zeiss LSM510](#)

## Nikon

- [TE2000-E with the C1 scanning head](#)



Literature: eg. Noise Theory and Application to Physics: Philippe Réfrégier, Springer

**PSF:** Point Spread Function

**f:** Object Function

**b:** Offset Function

**I:** Image Matrix

**N:** Noise Function

- Black Body Irradiation (Poisson)

- Detector Noise (Gauss)

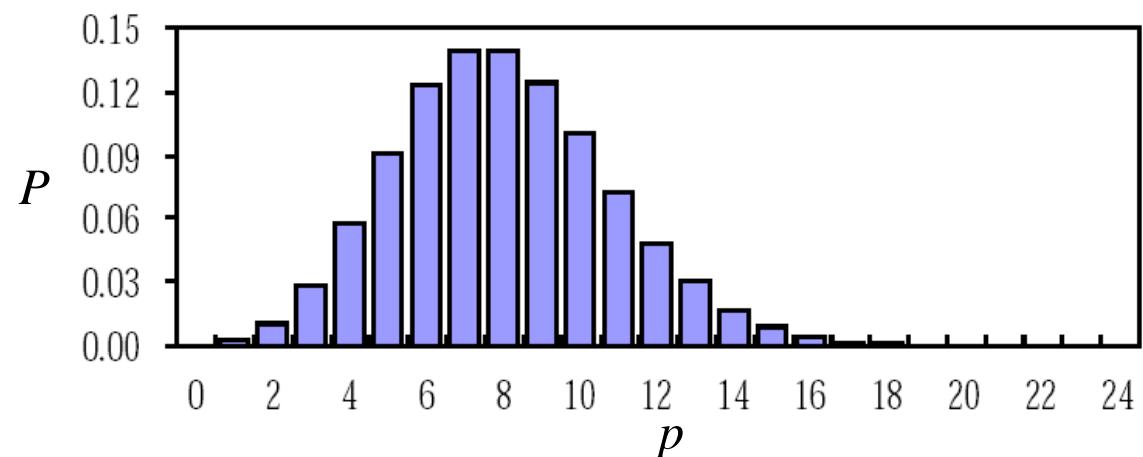
$$\mathbf{N}(\mathbf{PSF}(x, y, z) \otimes \mathbf{f}(x, y, z) + \mathbf{b}(x, y, z)) = \mathbf{I}(x, y, z)$$

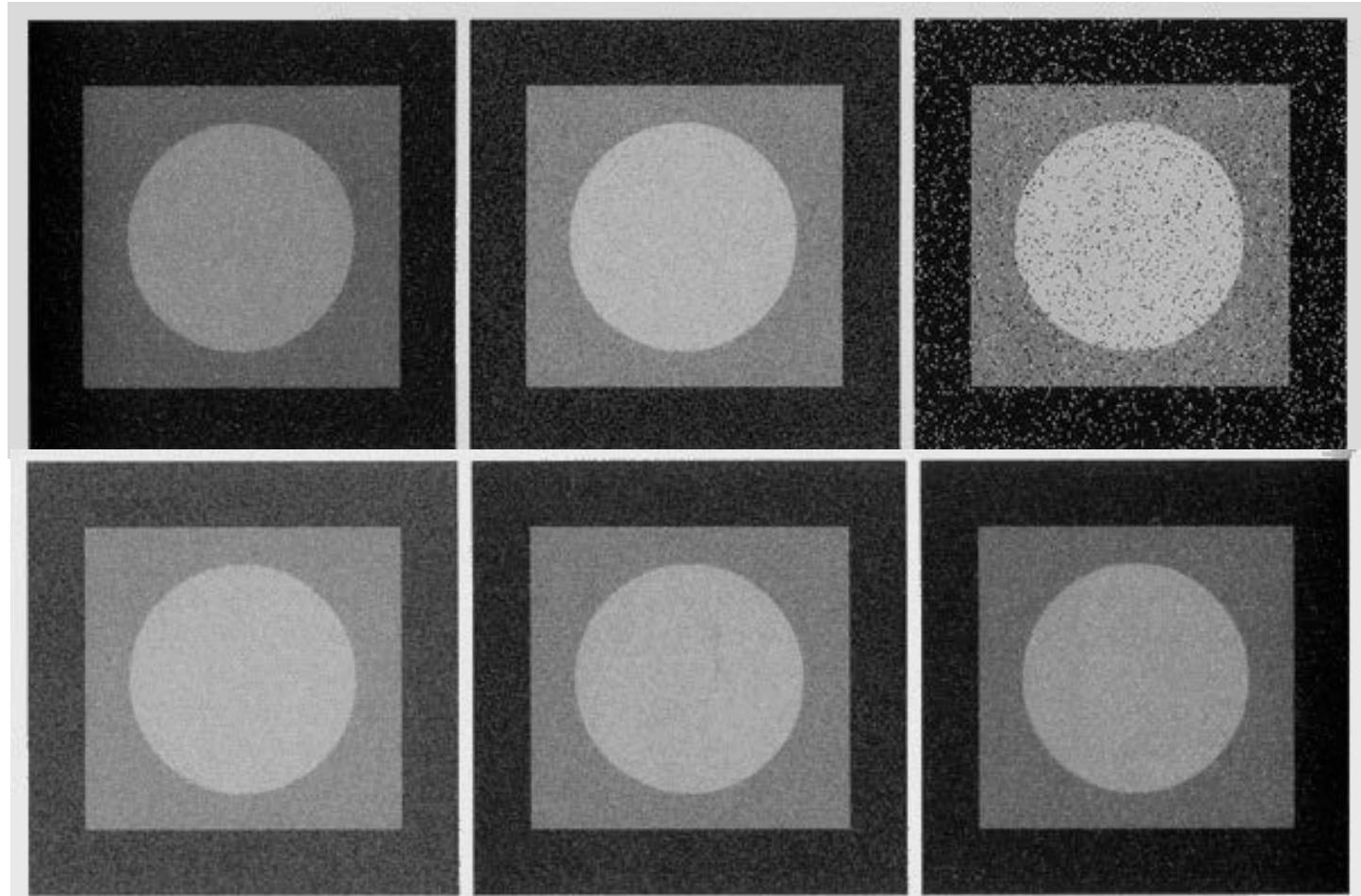
$$P(p, \mu) = \frac{\mu^p}{p!} \cdot e^{-\mu}$$

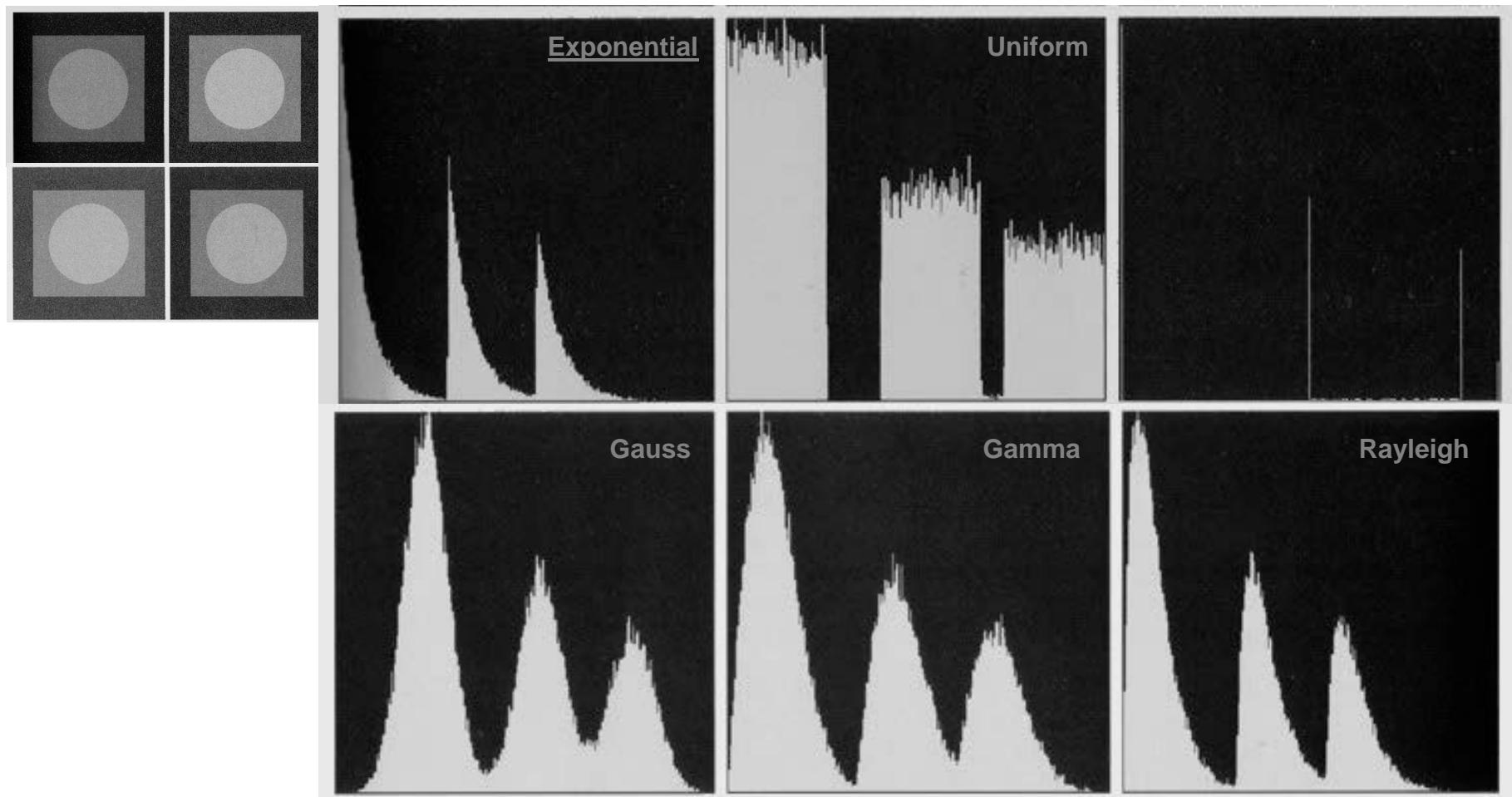
$$1. \bar{p} = \mu = \sigma^2, sd = \sigma = \sqrt{\bar{p}} = \sqrt{\mu}$$

$$2. \text{counting} : \bar{p} \pm \sqrt{\bar{p}}$$

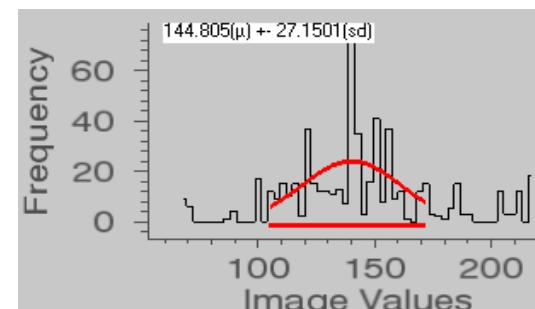
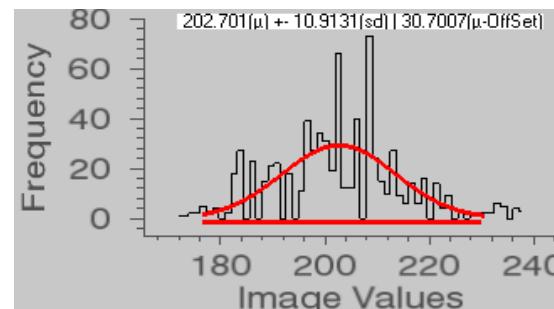
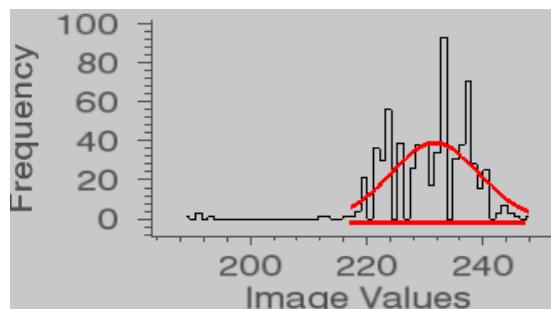
$$3. \text{Poisson(discrete)} \rightarrow \text{Gauss(continuous)} : \mu \rightarrow \infty$$







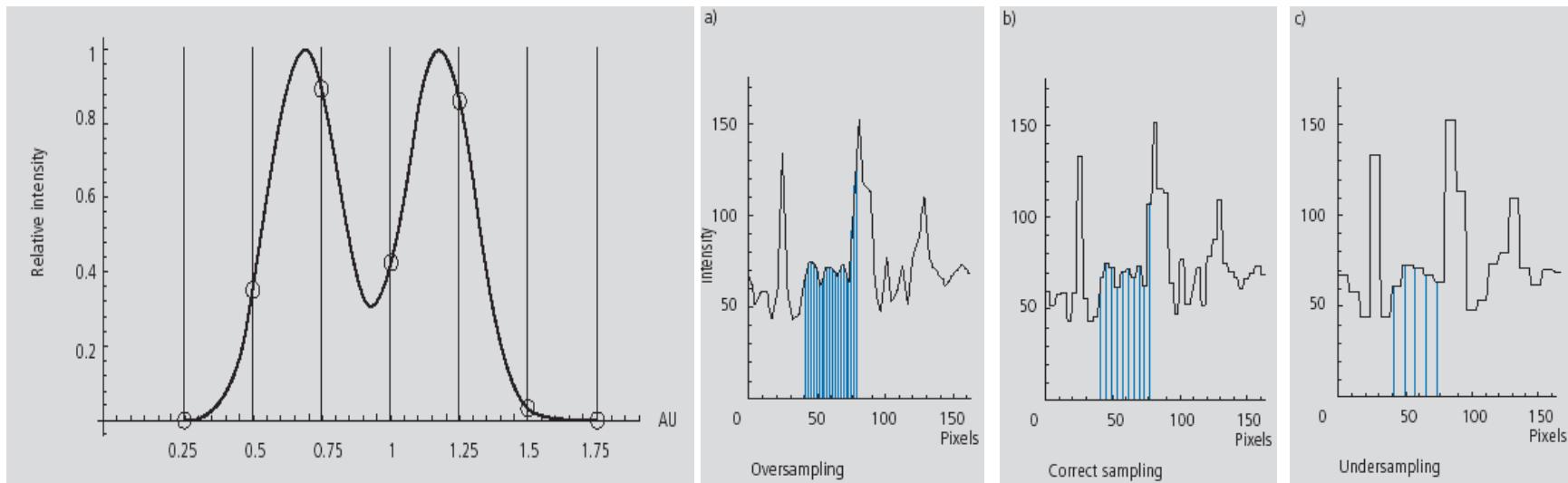
The Signal to Noise ratio (SN) is a number not always easy to estimate. The easiest way to obtain some figures is to look at the textures of bright areas in your object image. In the figure at left you see examples of such textures obtained from originally the same object image to which various levels of poisson noise were added.



$$SNR = \frac{\bar{I}}{\sigma} = \frac{\bar{I}}{\sqrt{\sigma^2}} = \frac{229}{7.5}$$

$$SNR = \frac{\bar{I}}{\sigma} = \frac{\bar{I}}{\sqrt{\sigma^2}} = \frac{200}{10}$$

$$SNR = \frac{\bar{I}}{\sigma} = \frac{\bar{I}}{\sqrt{\sigma^2}} = \frac{139}{27}$$



- Undersampling loses structures.
- Oversampling waists memory/computation time.

The 'Nyquist /Shannon Theorem' or 'Sampling Theorem' for the digital sampling of analogue signals suggests a Nyquist rate  $NR \geq 2v$  ?

**! Diffraction theory calculates lateral  $NR \sim 20 \text{ pixel}/\mu\text{m} (\sim 50 \text{ nm/pixel})$  !**  
**... axial  $NR \sim (\sim 150 \text{ nm/pixel})$**

**PSF:** Point Spread Function

**f:** Object Function

**b:** Offset Function

**I:** Image Matrix

**N:** Noise Function

$$N(PSF(x, y, z) \otimes f(x, y, z) + b(x, y, z)) = I(x, y, z)$$

Calculator


confocal

widefield

nipkow

4Pi

Select one

<u>Numerical aperture</u>	<input type="text" value="1.3"/>	
<u>Excitation wavelength</u>	<input type="text" value="488"/>	(nm)
<u>Emission wavelength</u>	<input type="text" value="520"/>	(nm)
<u>Number of excitation photons</u>	<input type="text" value="1"/>	
<u>Backprojected pinhole radius</u>	<input type="text" value="250"/>	(nm)
<u>B.P. distance between pinholes</u>	<input type="text" value="2.53"/>	Only for Nipkow disks (μm)
<u>Lens medium refractive index</u>	<input type="text" value="1.515"/>	
<u>Specimen medium refractive index</u>	<input type="text" value="1.45"/>	
<u>Acquisition depth</u>	<input type="text" value="0"/>	(μm)
<input type="checkbox"/> Calculate also PSF		

<http://support.svi.nl/wiki/NyquistCalculator>

**PSF:** Point Spread Function

**f:** Object Function

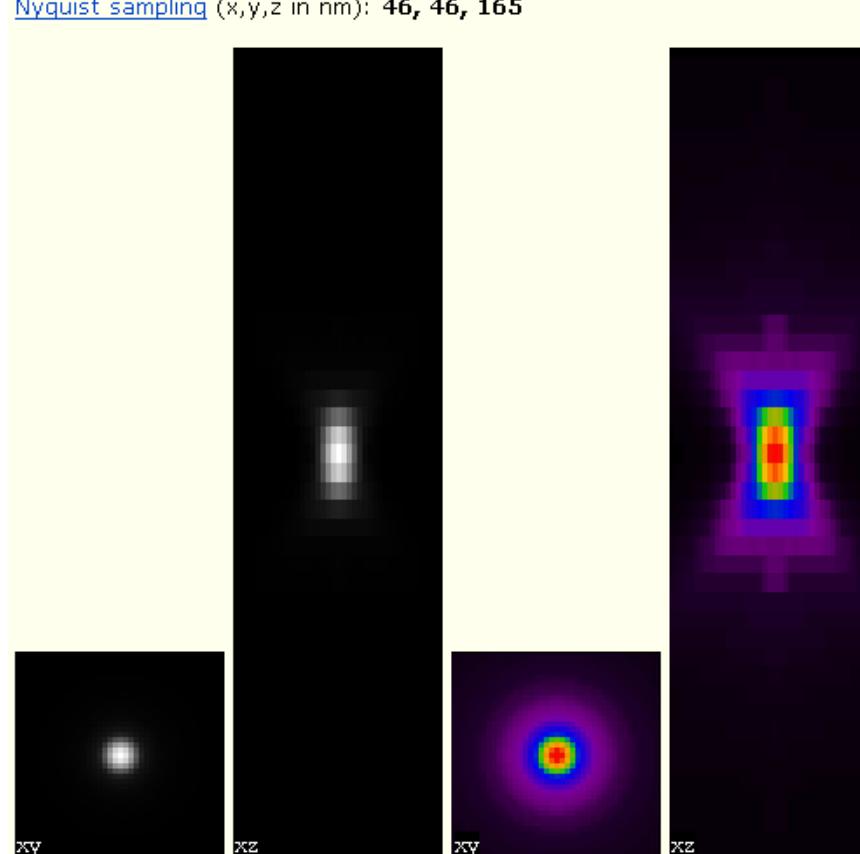
**b:** Offset Function

**I:** Image Matrix

**N:** Noise Function

$$N(\mathbf{PSF}(x, y, z) \otimes \mathbf{f}(x, y, z) + \mathbf{b}(x, y, z)) = \mathbf{I}(x, y, z)$$

Nyquist sampling (x,y,z in nm): **46, 46, 165**

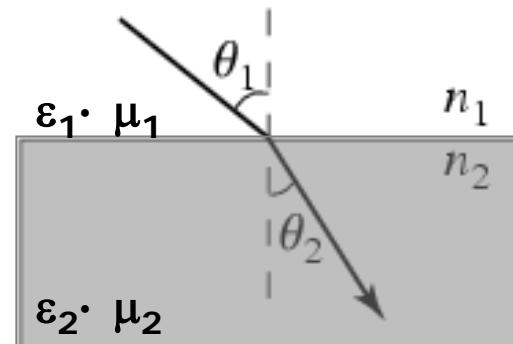


**Index of refraction:**  $n = (\epsilon \cdot \mu)^{1/2} = c/v$ ,  
 *$\epsilon$  electric permittivity and  $\mu$  magnetic permeability.*

### Snell's Law:

$$\sin\theta_1 n_1 = \sin \theta_2 n_2$$

- 1.518 [Zeiss Oil]
- 1.33 [Water]
- 1.0008 [Air]



### Refractive Index:

$$RI = n_1/n_2 = v_2/v_1$$

### Snell's Law:

$$\sin \theta_1 / n_1 = \sin \theta_2 / n_2$$

$$n = n(\lambda) !$$

- 1.518 [Zeiss]
- 1.33 [Water]
- 1.0008 [Air]

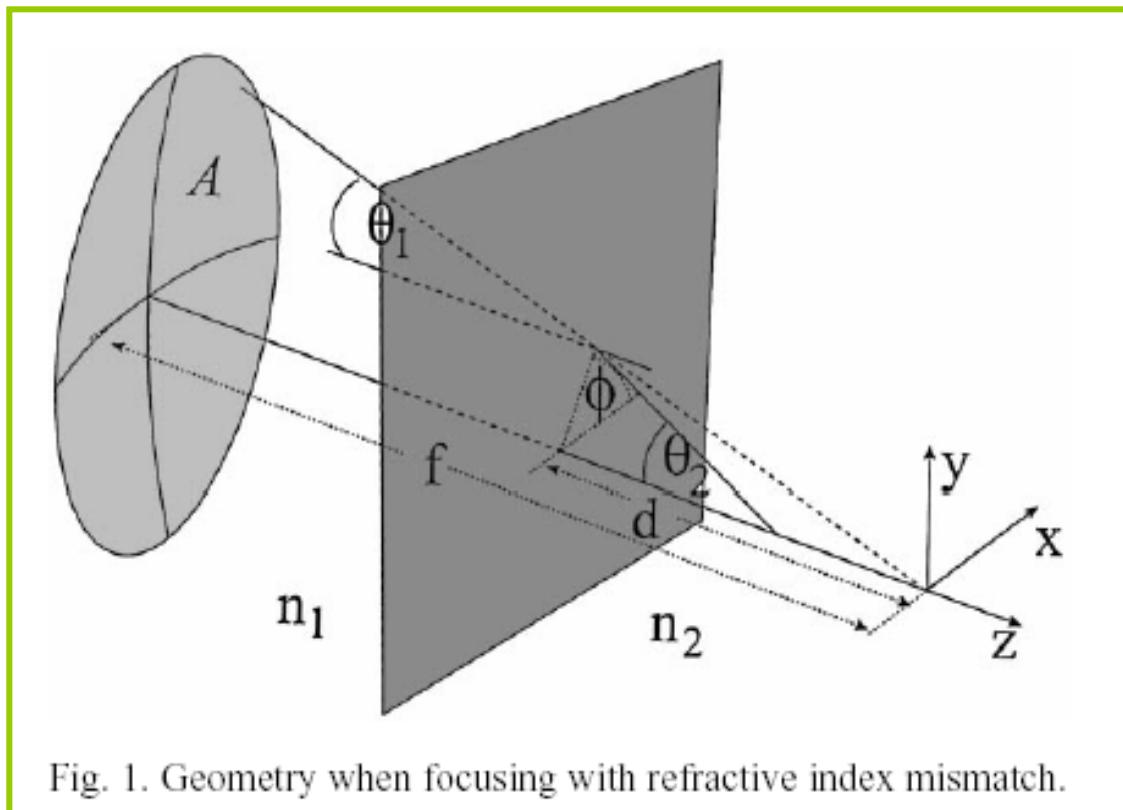
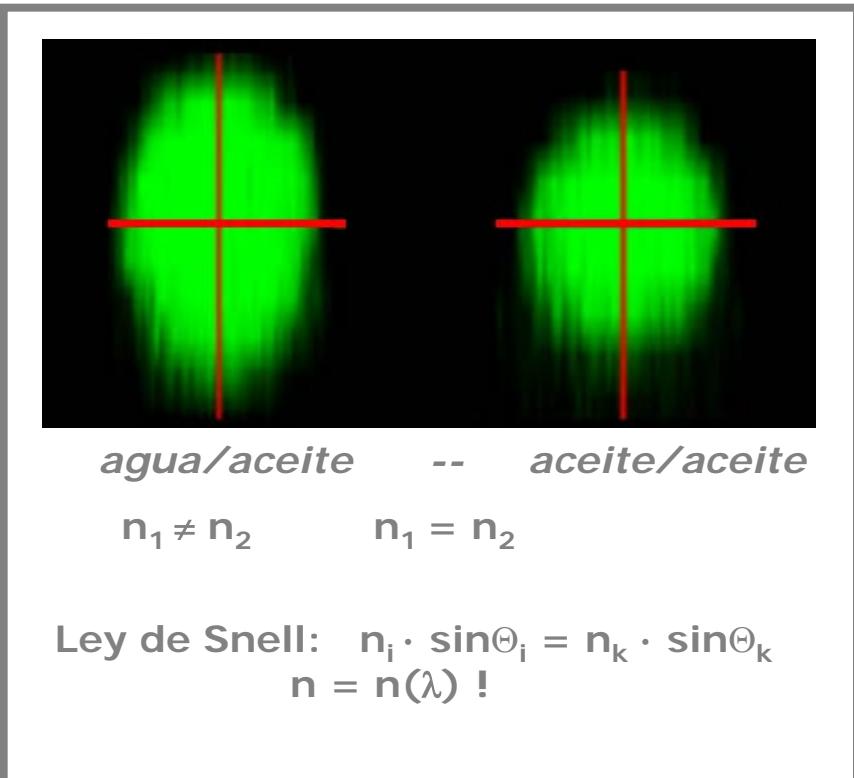
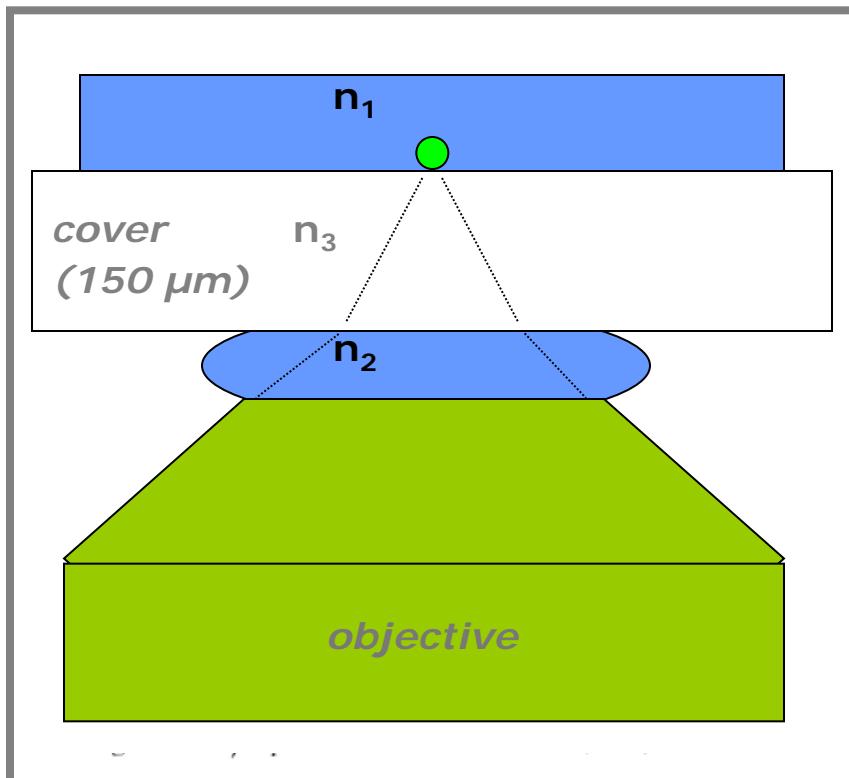
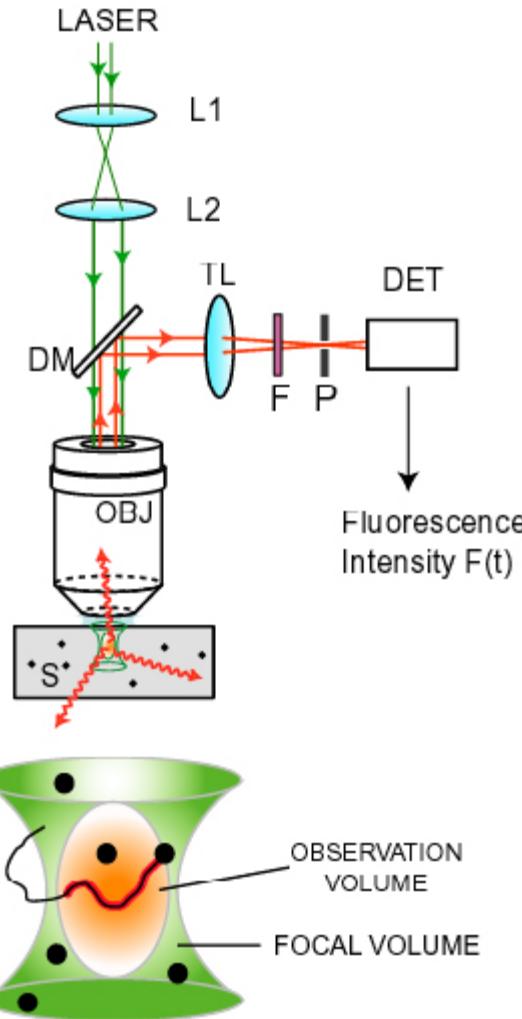


Fig. 1. Geometry when focusing with refractive index mismatch.

(Egner et al 1998)

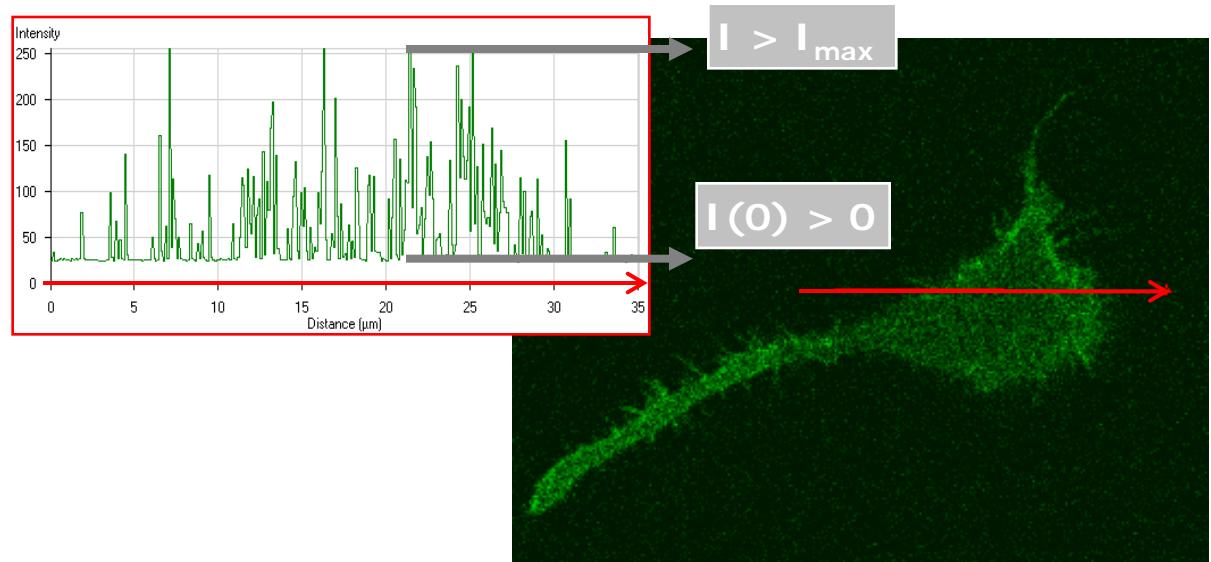
- Micro-esfera:  $\emptyset = 6 \mu\text{m}$

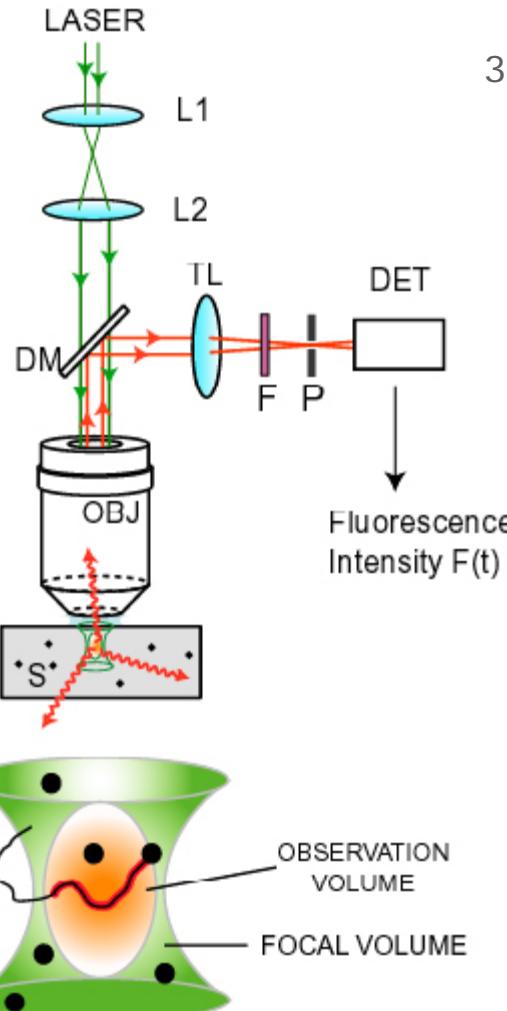




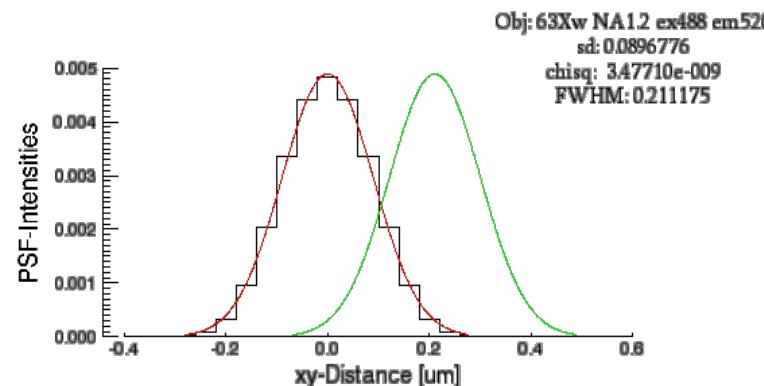
The observation volume (femtoliter) defined by the Point Spread Function must be considered as a minispectrofluorimeter.

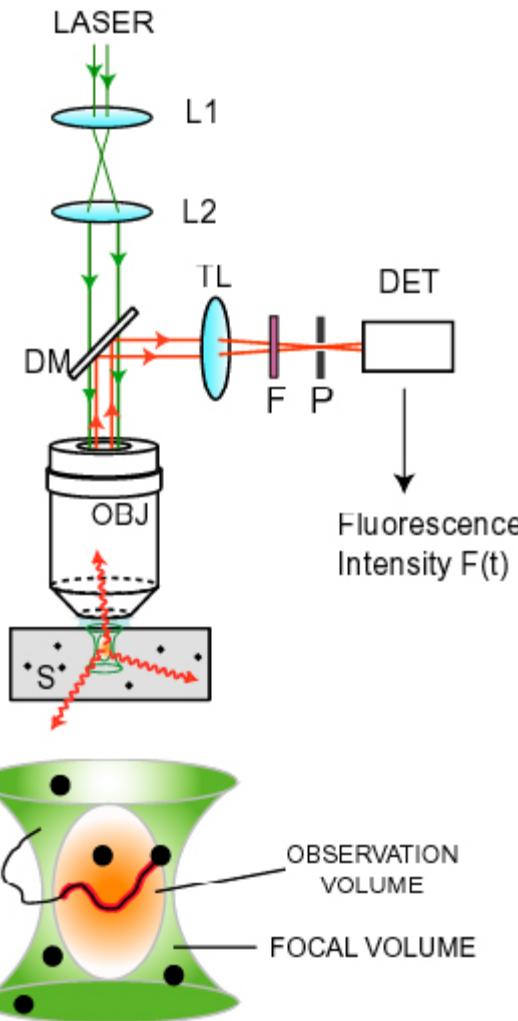
1. You need to consider the Offset  $I(0)$  in order to calibrate your signal  $I(0) \geq 0$  !
2. Never saturate the signal:  $I \leq I_{\max}$  (255 for 8 bit) !





3. You need to consider sampling distances in  $\Delta x$  and  $\Delta y \approx 50$  nm and  $\Delta z \approx 150-300$  nm for later deconvolution, or calculate the explicit sample distances @ <http://support.svi.nl/wiki/NyquistCalculator>



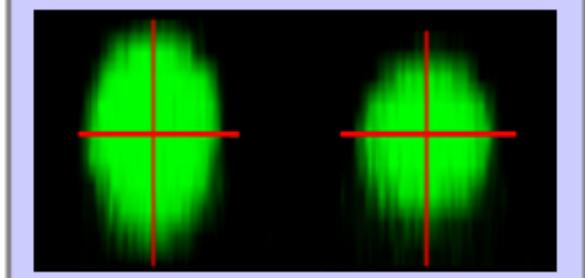
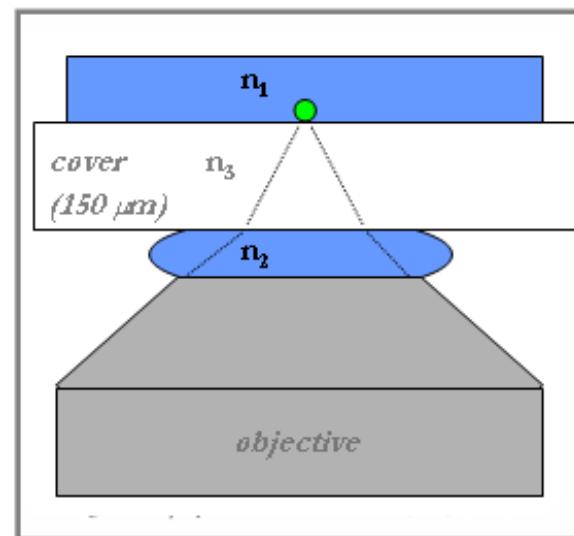


4. Use the right immersion setup !

$$n_1 = n_2 !$$

Keep refractive index / index of refraction constant !

● Micro-esfera:  $\varnothing = 6 \mu\text{m}$



$$n_1 \neq n_2 \quad n_1 = n_2$$

Ley de Snell:  $n_i \cdot \sin\Theta_i = n_k \cdot \sin\Theta_k$

$$n = n(\lambda) !$$