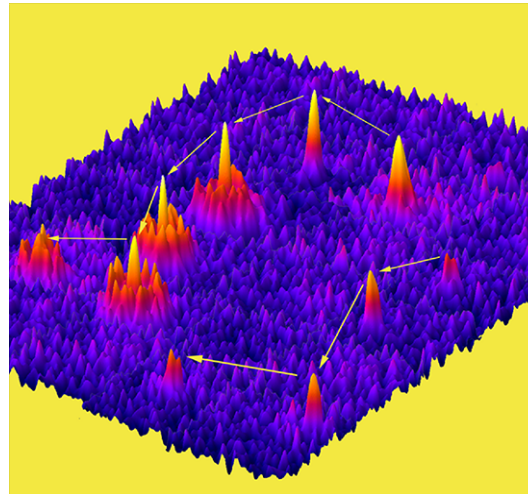


Course „Optics, Forces & Development“

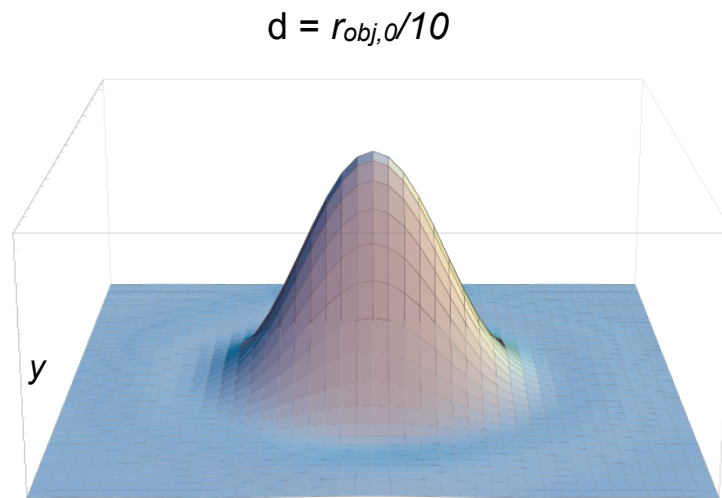
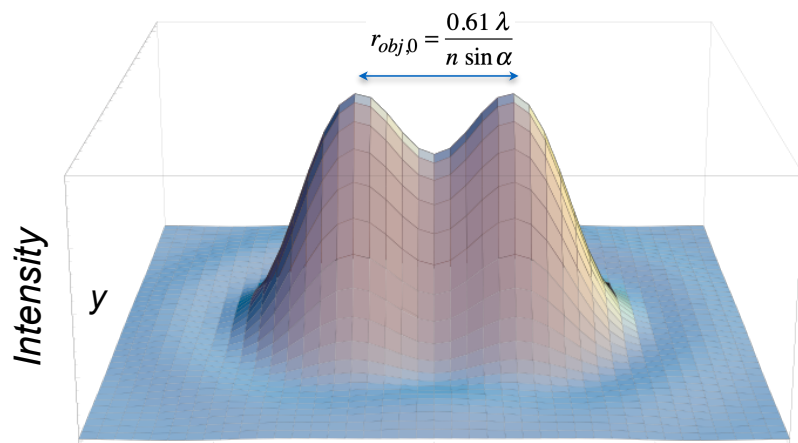
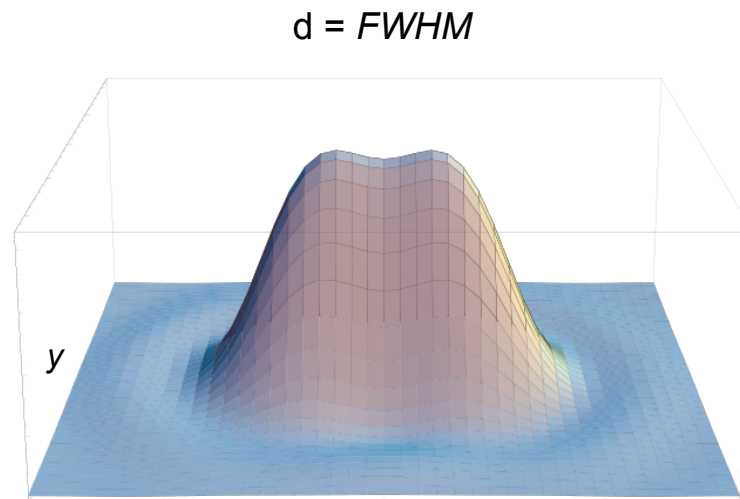
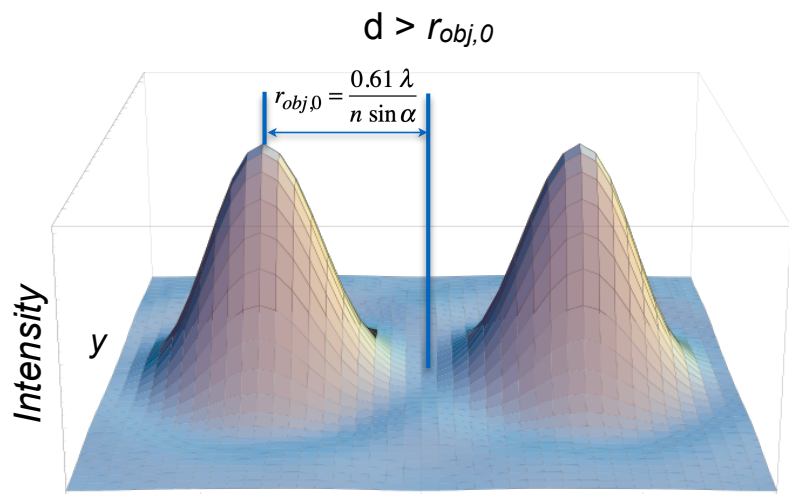


Principles of Optics II

Ulrich Kubitscheck

Clausius-Institute of Physical and Theoretical Chemistry  
Rheinische Friedrich-Wilhelms-Universität Bonn

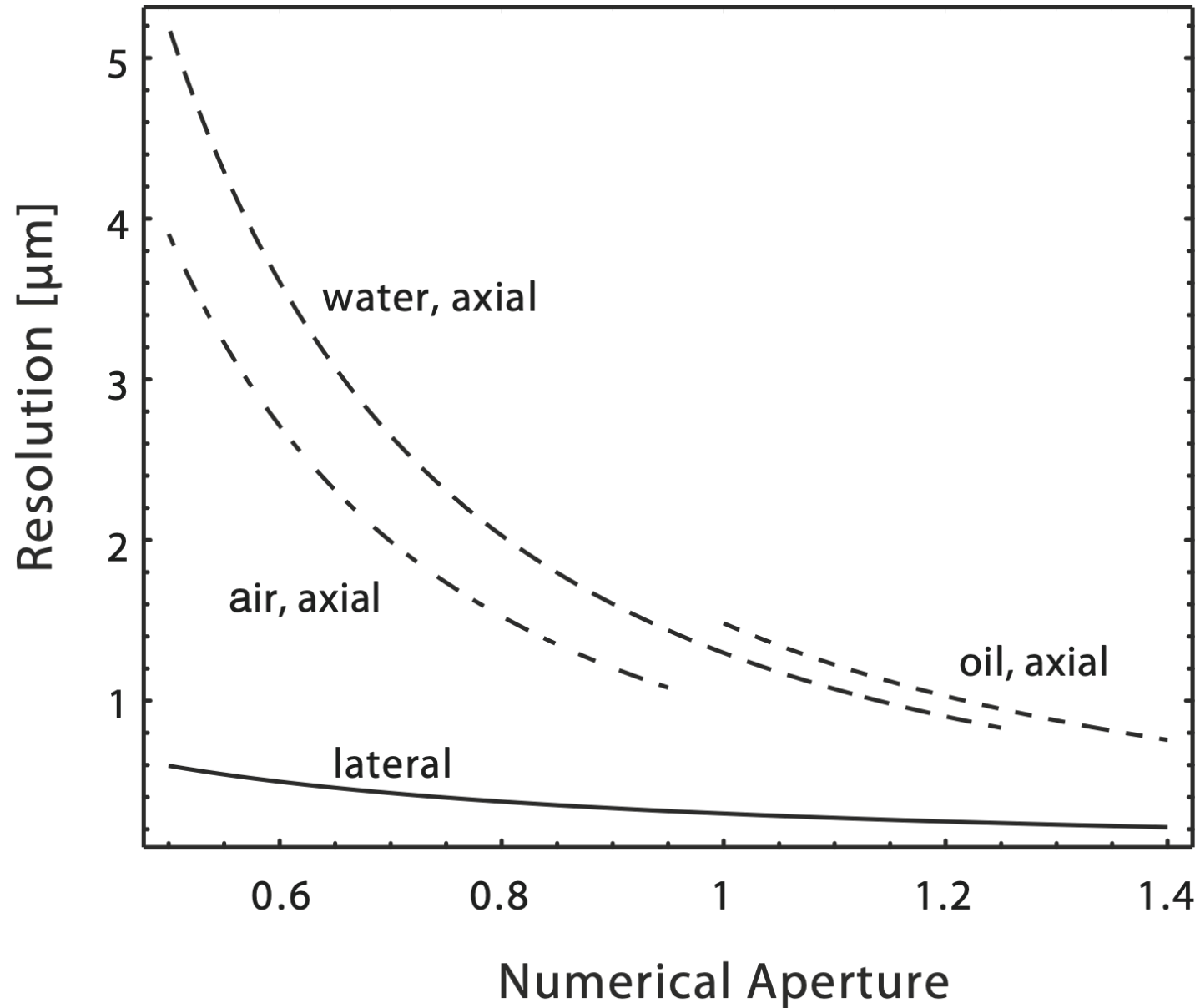
# Sum of Point Spread Functions for Incoherent Point Objects



lateral distance, x

lateral distance, x

# Radial and axial resolution as function of the NA



# The resolution limit in the biological context

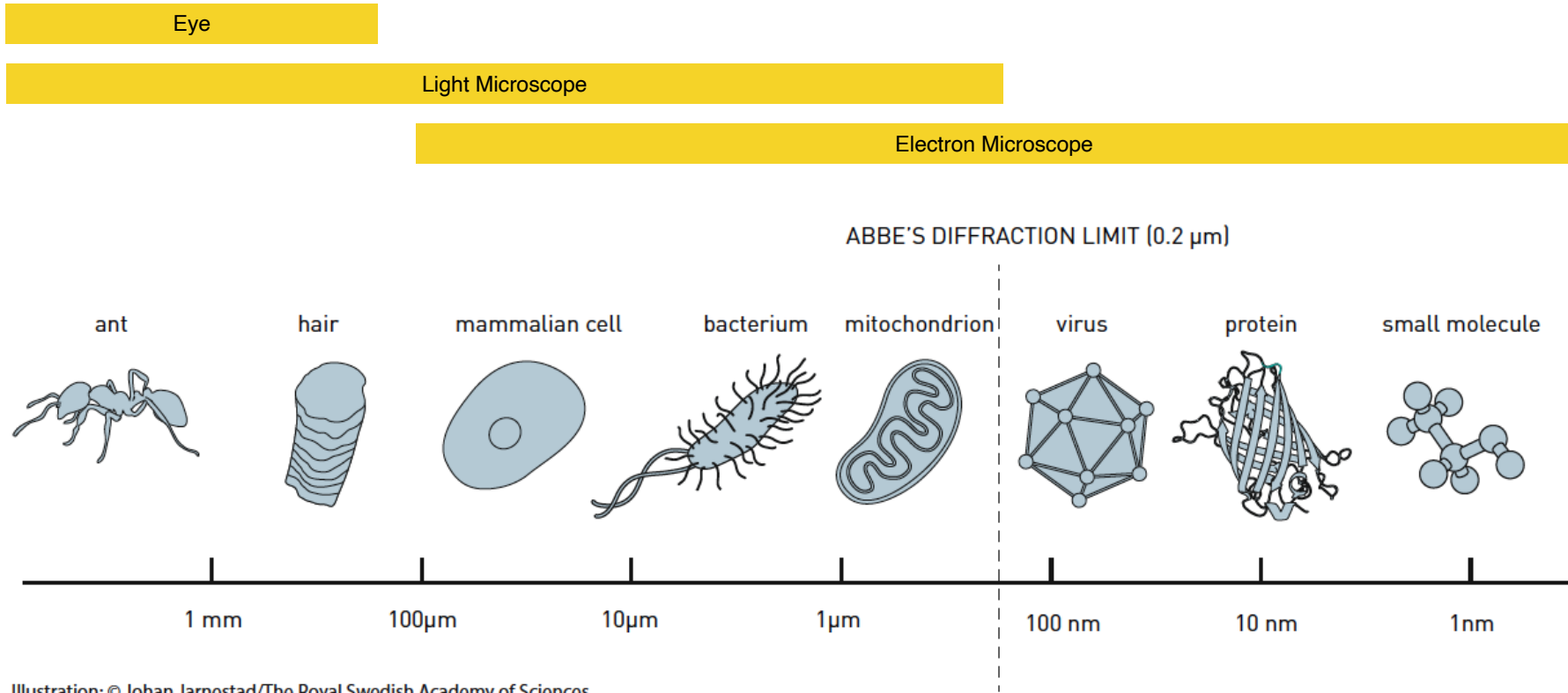
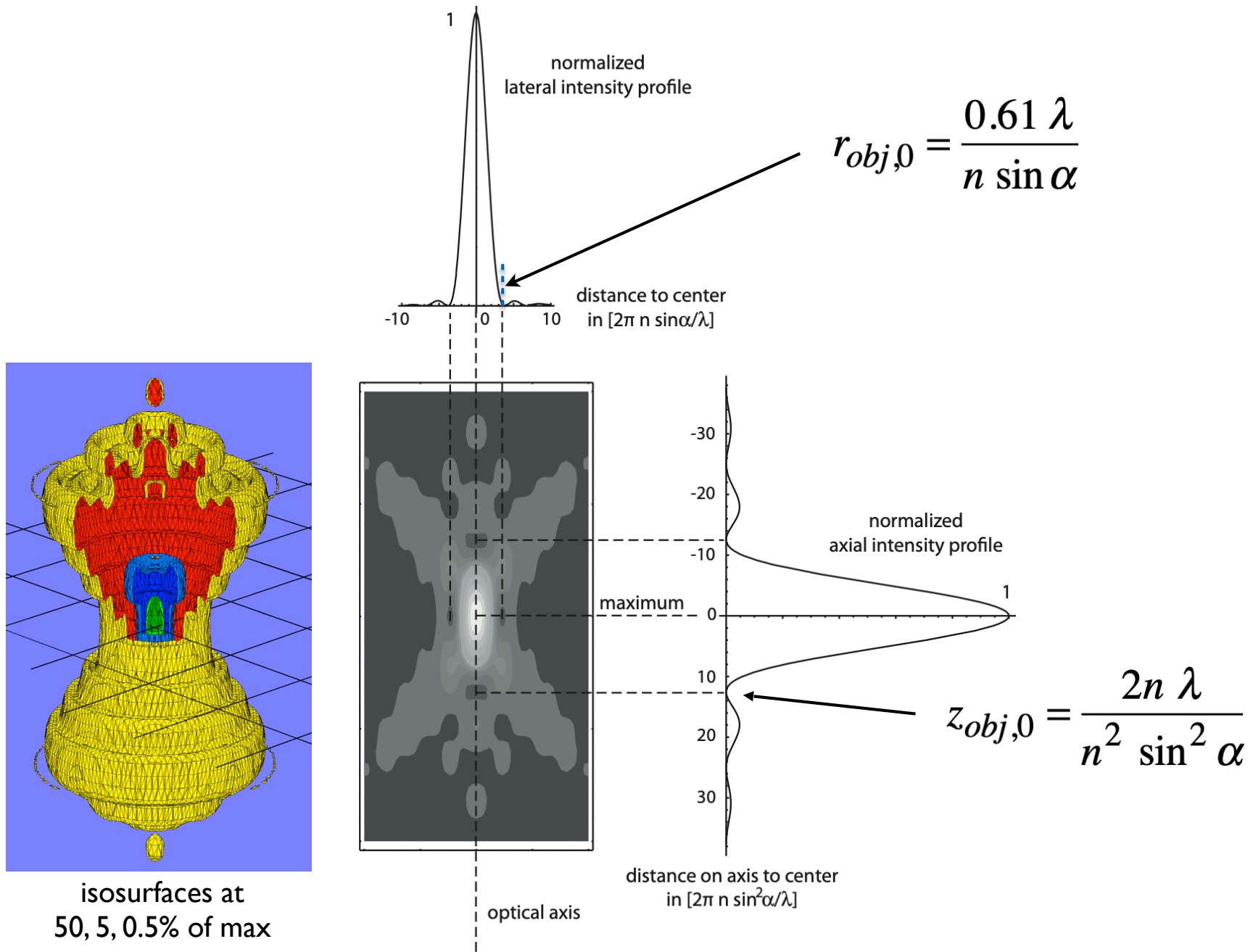


Illustration: © Johan Jarnestad/The Royal Swedish Academy of Sciences

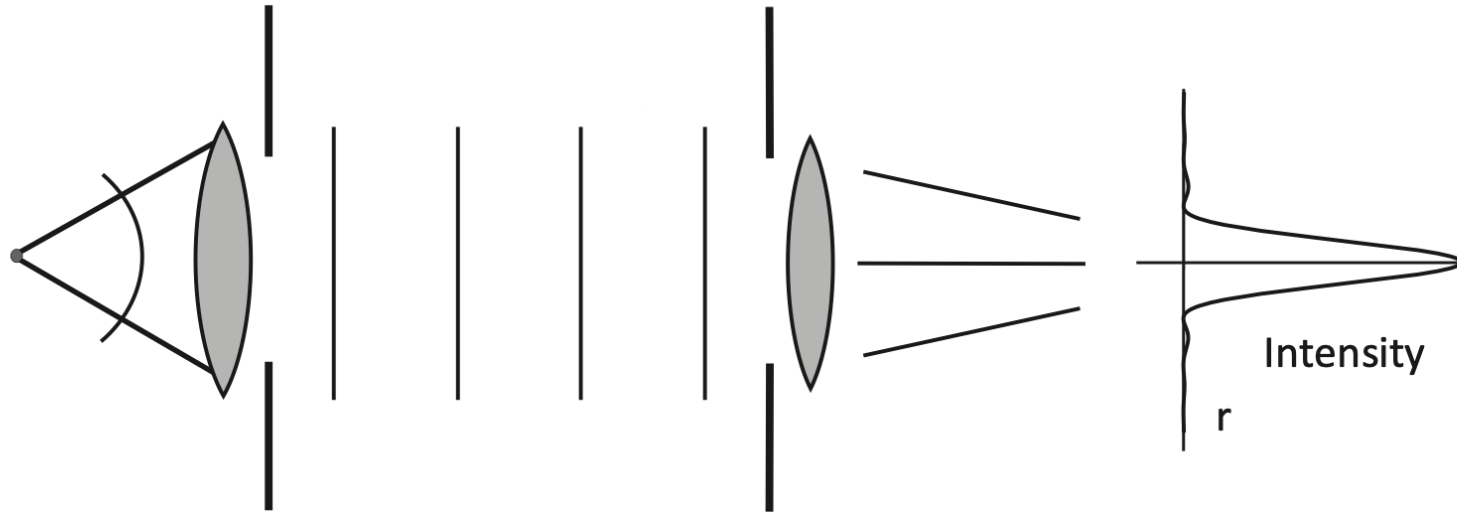


# 3D Point spread function (PSF)



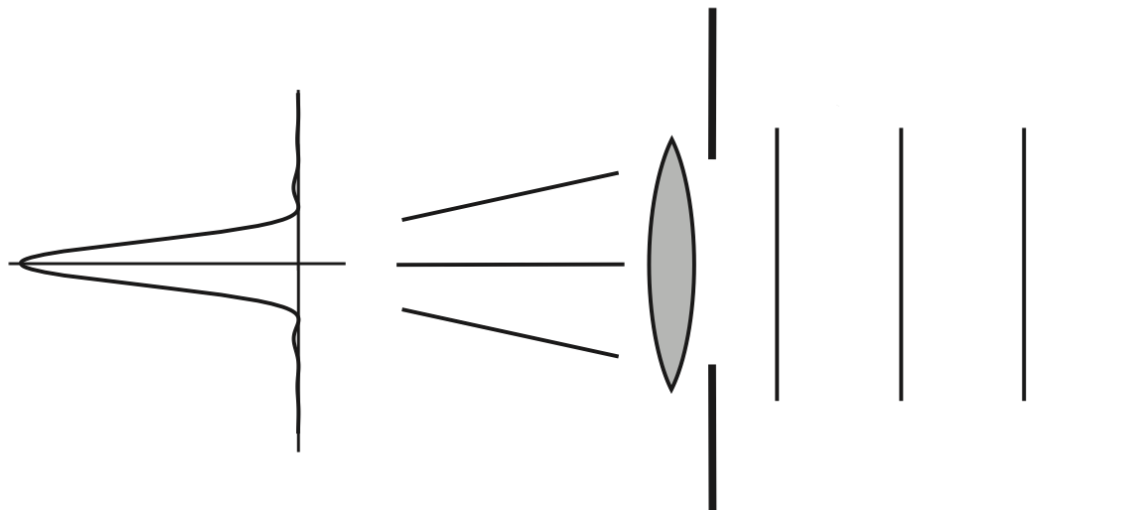
# Radial and axial intensity profile of the light distribution in the focus of a lens

Imaging of a point



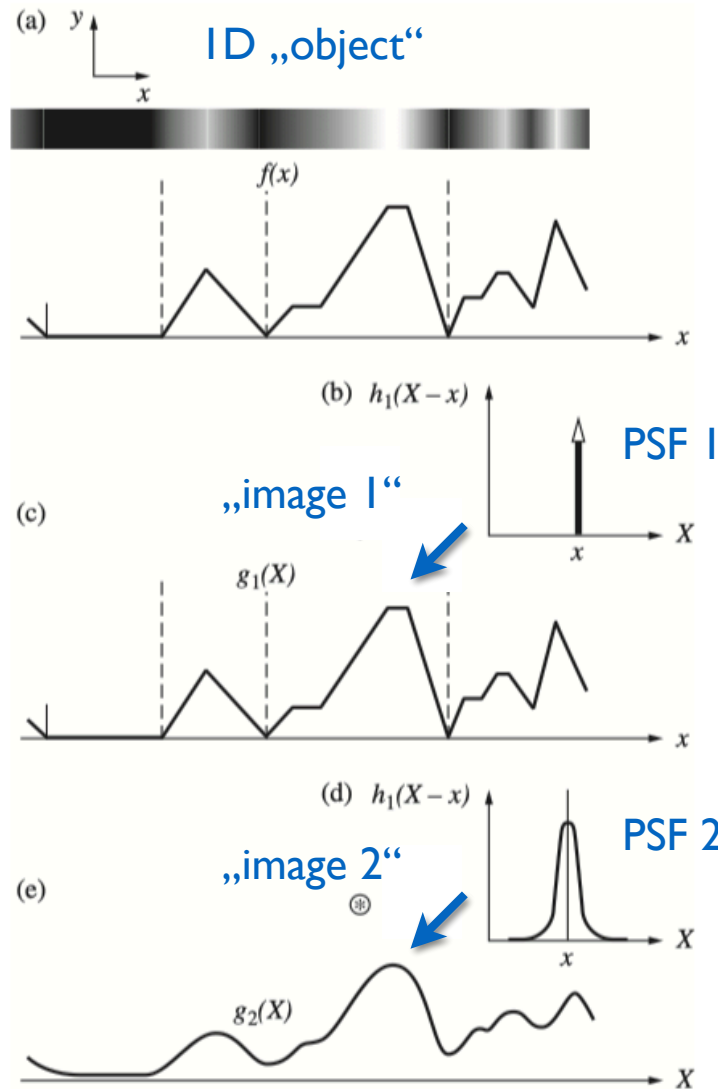
object space

Illumination of a „point“

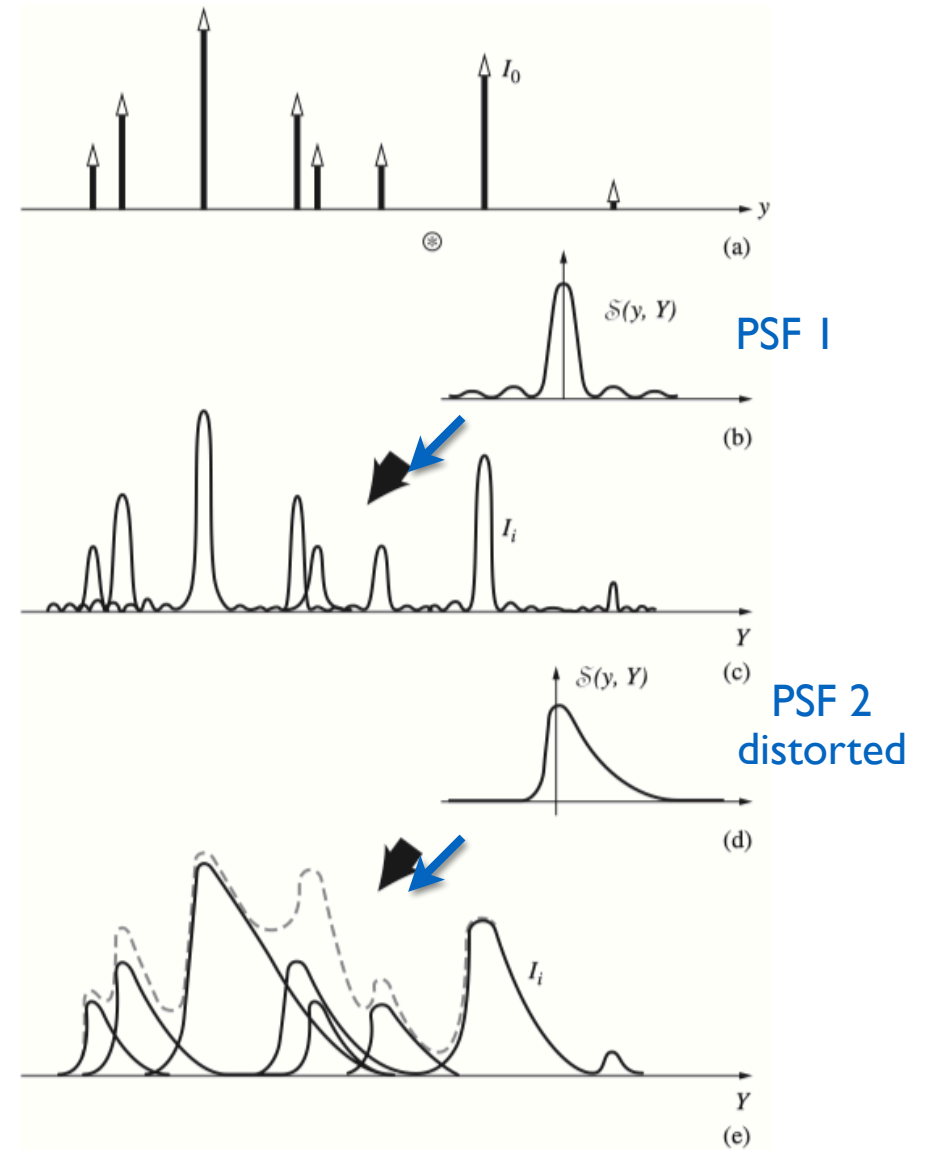


## 6. More PSF: convolution and deconvolution

# More on the PSF: convolution in microscopy

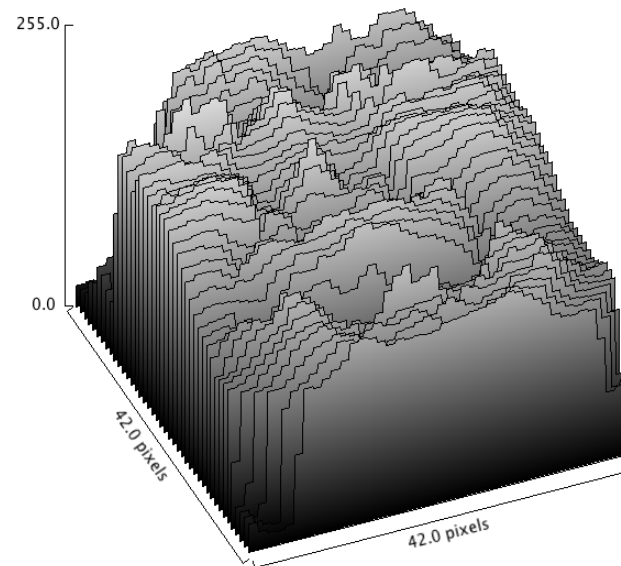
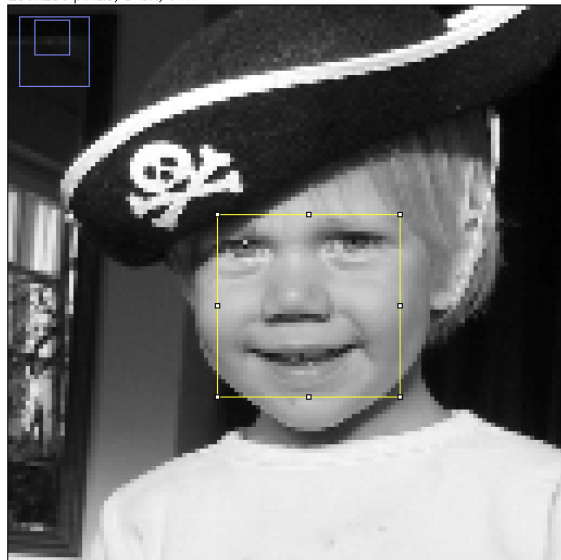


The irradiance distribution is converted to a function  $f(x)$  shown in (a). This is convolved with  $\delta$ -function (b) to yield a duplicate of  $f(x)$ . By contrast, convolving  $f(x)$  with the spread function  $h_2$  in (d) yields a smoothed-out curve represented by  $g_2(x)$  in (e).



Here (a) is convolved first with (b) to produce (c) and then with (d) to produce (e). The resulting pattern is the sum of all the spread-out contributions, as indicated by the dashed curve in (e).

Images are arrays of integer values  $h(i,j)$

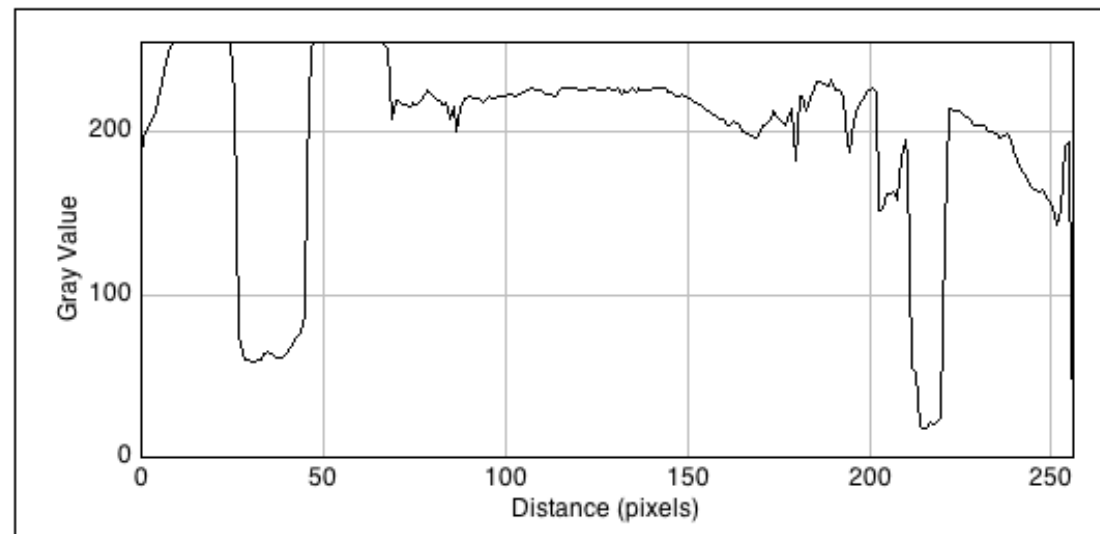


Surface profile

$i, j$ -values correspond to position



Line profile



## Gauss filter for image smoothing... and convolution

$$\begin{aligned}h'(i,j) = & \{h(i-1,j-1) + 2 h(i-1,j) + h(i-1,j+1) \\ & + 2 h(i,j-1) + 4 h(i,j) + 2 h(i,j+1) \\ & + h(i+1,j-1) + 2 h(i+1,j) + h(i+1,j+1)\} / 16\end{aligned}$$

0	0	1	2	3
0	1	2	3	2
1	2	3	2	1
2	3	2	1	0
3	2	1	0	0

or

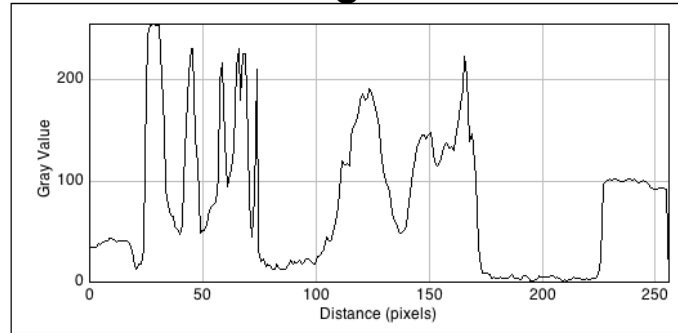
$$h'(i,j) = \sum_{u=-1}^1 \sum_{v=-1}^1 h(i+u, j+v) \cdot g(u,v)$$
$$g(u,v) = \frac{1}{16} \begin{pmatrix} 1 & 2 & 1 \\ 2 & 4 & 2 \\ 1 & 2 & 1 \end{pmatrix}$$

or

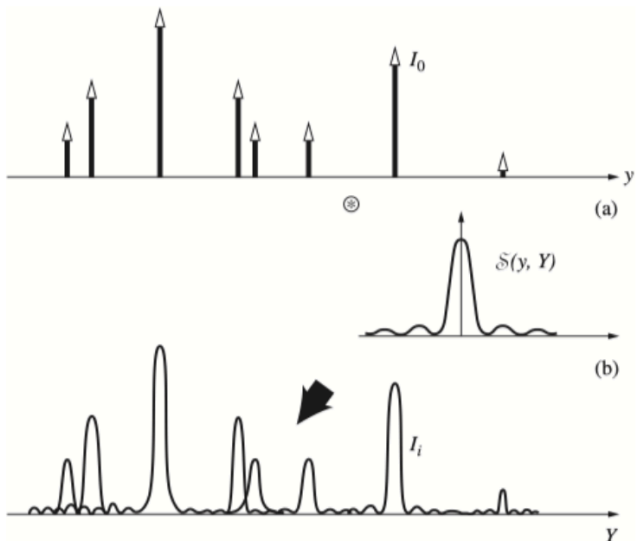
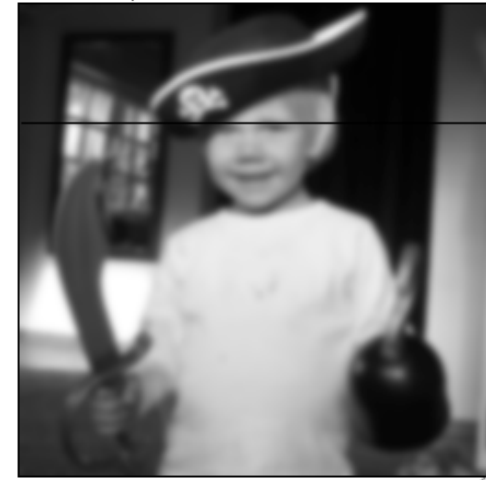
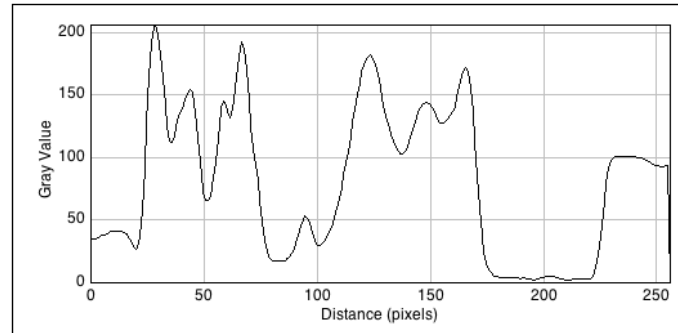
$$h' = h \otimes g \quad h' \text{ is the result of the „convolution“ of } h \text{ with } g$$

# Image smoothing = low pass filtering

original



smoothed or low pass filtered



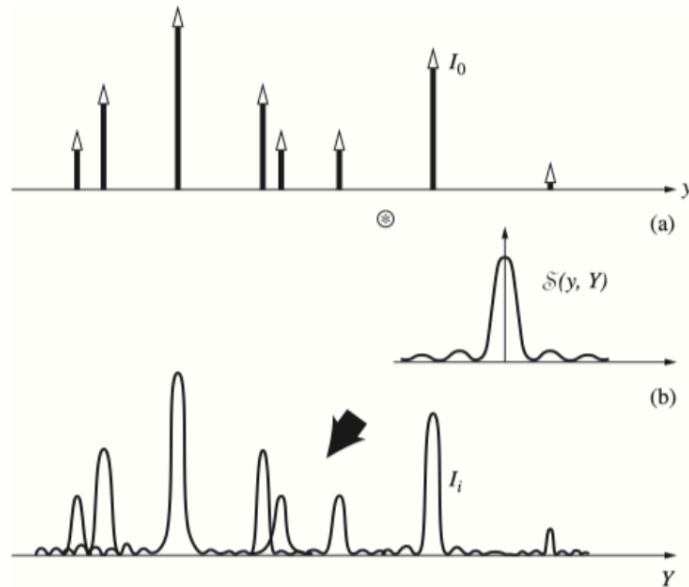
„original“

„lens“

„image“

„lenses“ are nothing else than „optical low pass filters“

# Restoration of original object function by deconvolution



object function  $O(x,y,z) \leftrightarrow \mathbb{O}(\omega_x, \omega_y, \omega_z)$

lens function  $PSF(x,y,z) \leftrightarrow \mathbb{O}TF(\omega_x, \omega_y, \omega_z)$

image function  $I(x,y,z) \leftrightarrow \mathbb{I}(\omega_x, \omega_y, \omega_z)$

$$I(x,y,z) = O(x,y,z) \otimes PSF(x,y,z) \leftrightarrow \mathbb{I}(\omega_x, \omega_y, \omega_z) = \mathbb{O}(\omega_x, \omega_y, \omega_z) \cdot \mathbb{O}TF(\omega_x, \omega_y, \omega_z)$$

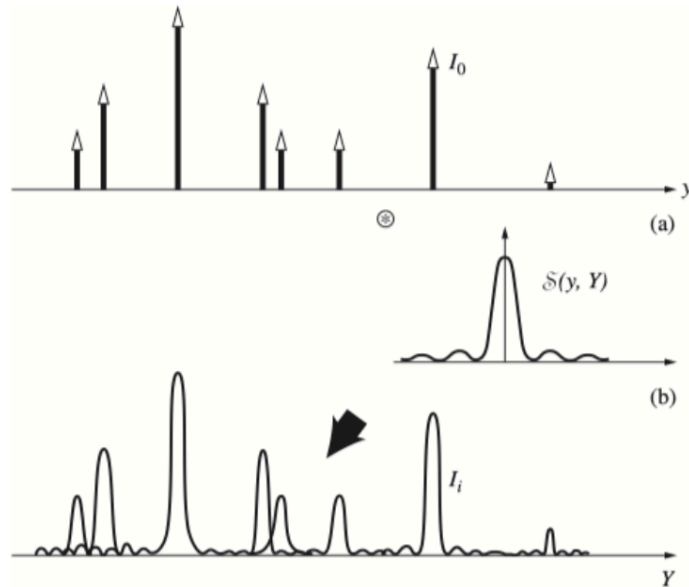
$$\Rightarrow \mathbb{O}(\omega_x, \omega_y, \omega_z) = \mathbb{I}(\omega_x, \omega_y, \omega_z) / \mathbb{O}TF(\omega_x, \omega_y, \omega_z)$$

$$\Rightarrow \mathbb{O}(\omega_x, \omega_y, \omega_z) \leftrightarrow O(x,y,z)$$

Theoretically, we can invert the effect of the PSF by „deconvolution“



# Restoration of original object function by deconvolution



object function  $O(x,y,z) \leftrightarrow \textcircled{\omega_x, \omega_y, \omega_z}$

lens function  $PSF(x,y,z) \leftrightarrow \textcircled{\text{TF}}(\omega_x, \omega_y, \omega_z)$

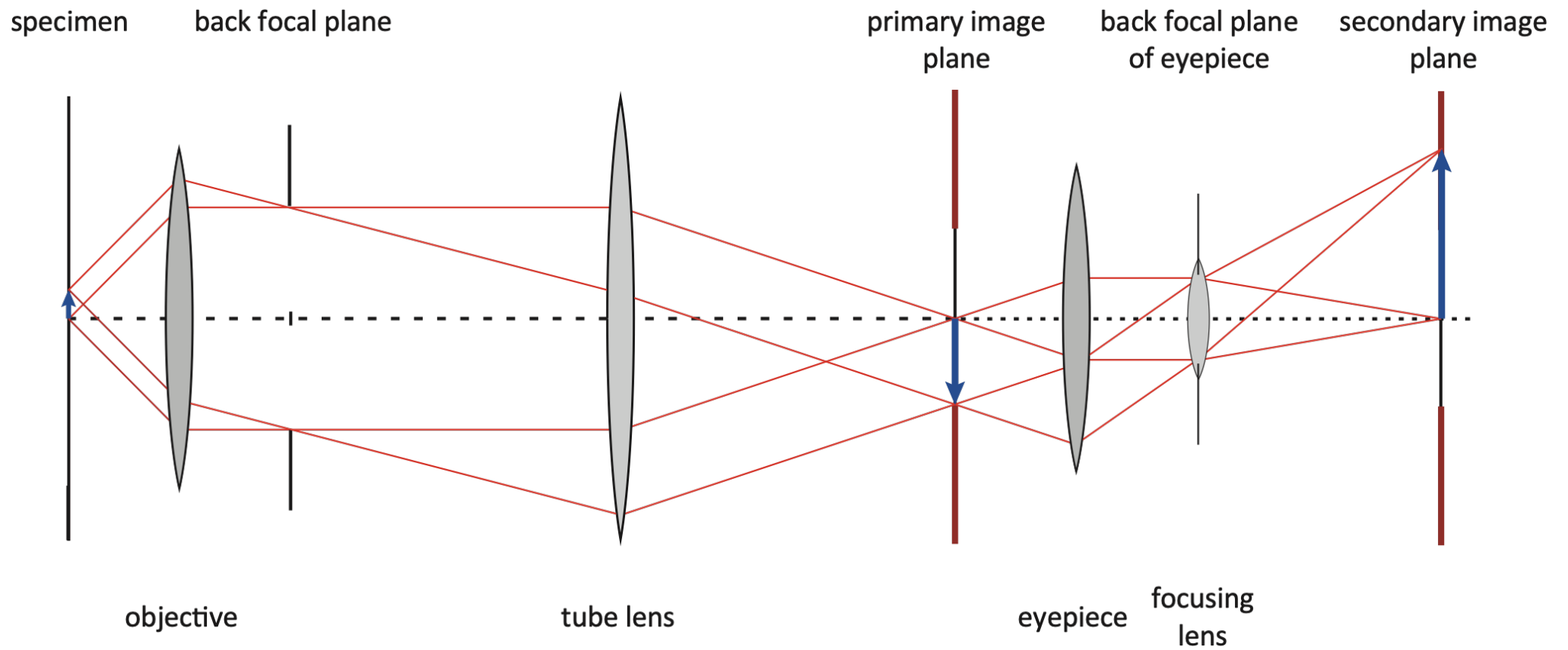
image function  $I(x,y,z) \leftrightarrow \textcircled{\omega_x, \omega_y, \omega_z}$

$$I'(x,y,z) = O(x,y,z) \otimes PSF(x,y,z) + \text{Noise}(x,y,z)$$

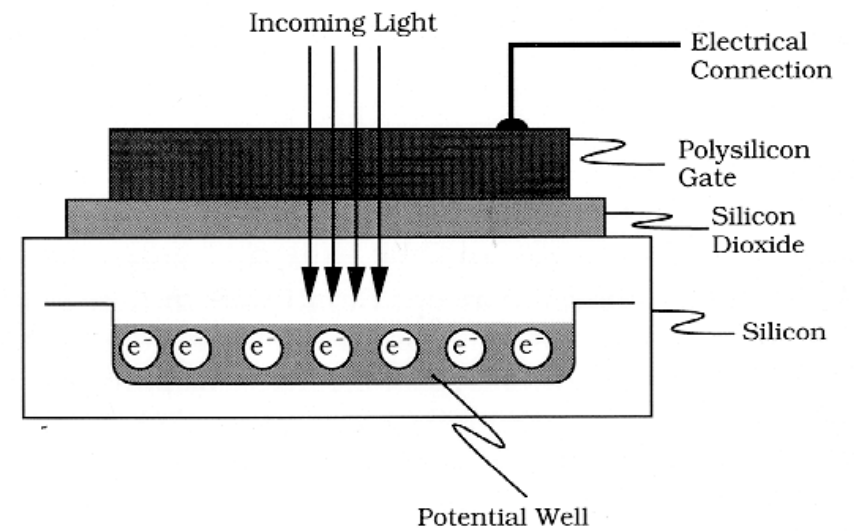
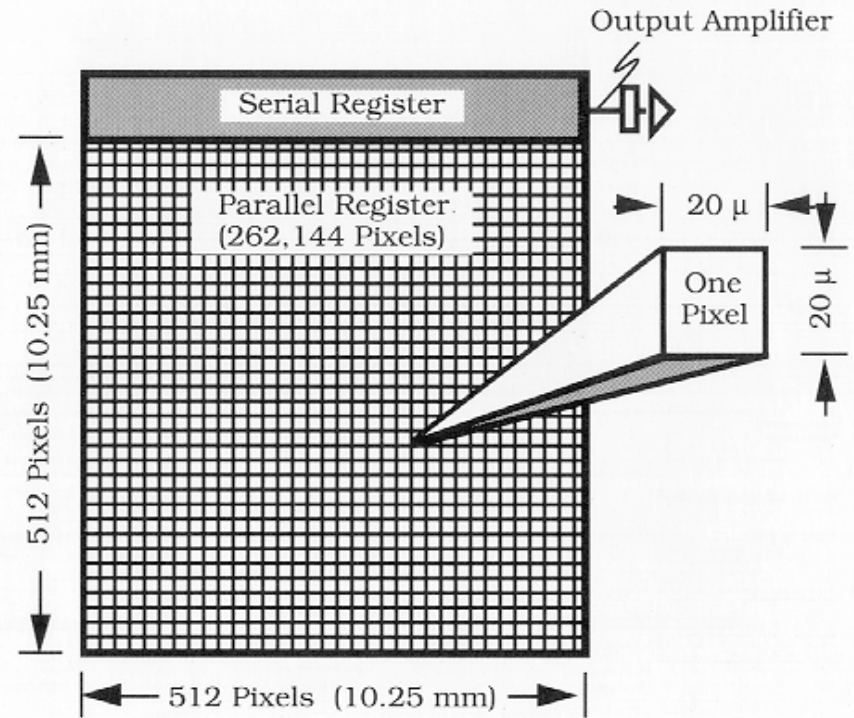
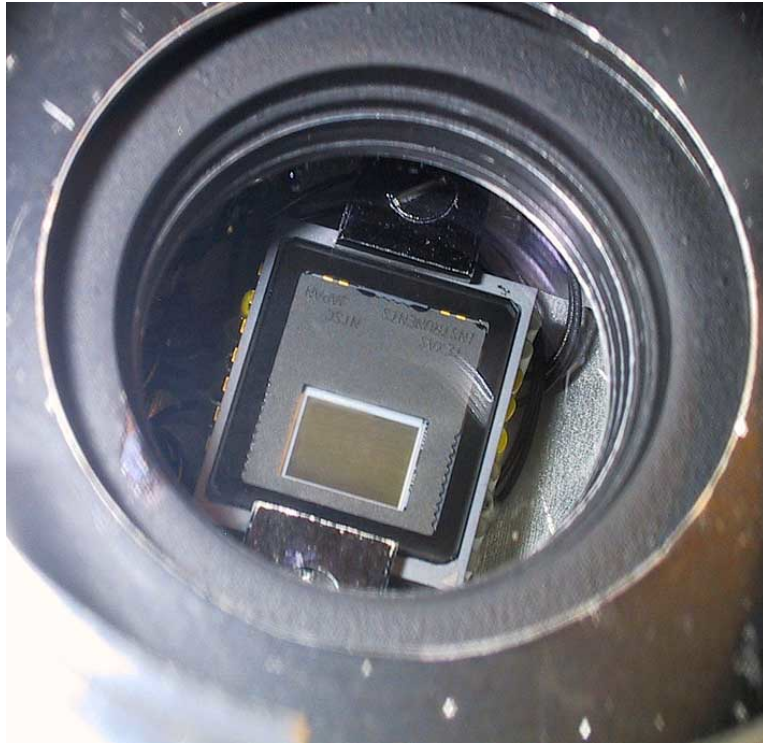
Theoretically, we can invert the effect of the PSF by „deconvolution“.  
Practically, this is far from easy!

## 7. Image detection by cameras and pixel size

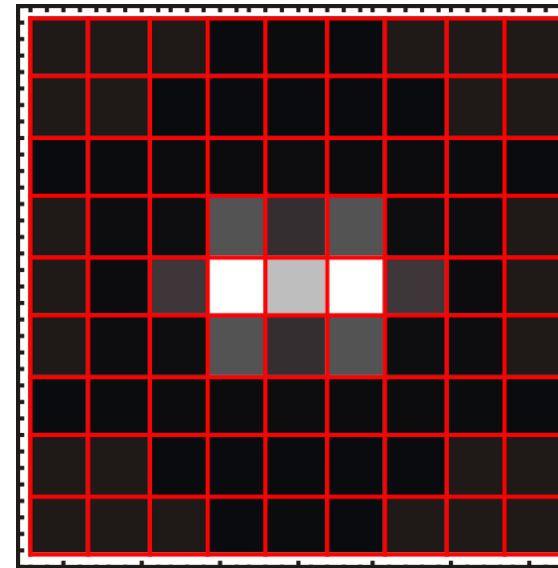
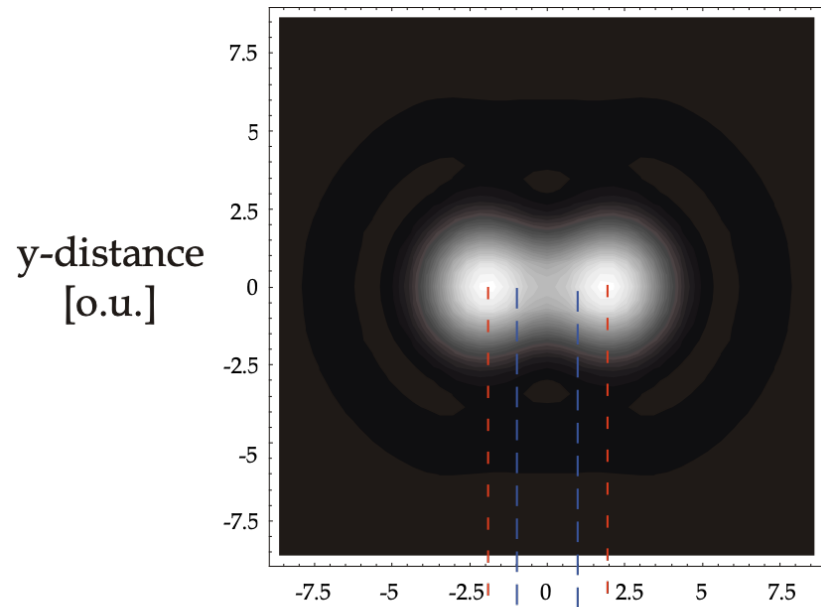
# Construction of a microscope by combination of two magnification stages



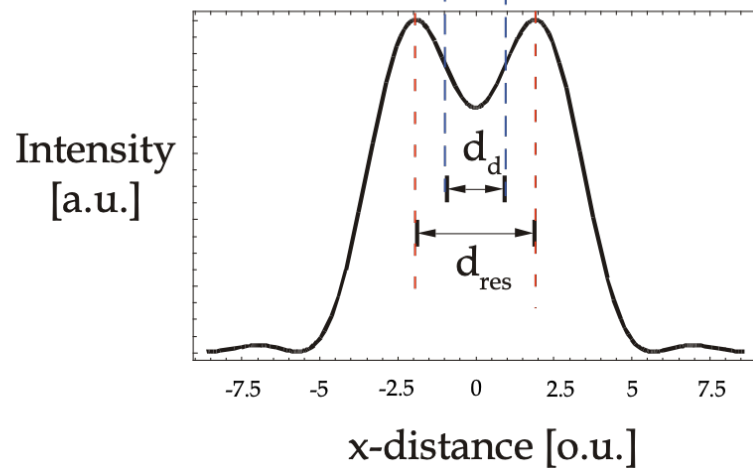
# CCD-Chips



# Optical Resolution and Choice of Detection Pixel Size



$$d_d = 0.5 d_{\text{res}}$$



$$d_d \leq \frac{d_{\text{res}}}{2}$$

Nyquist-Theorem

# Minimal Magnification Required to Avoid Resolution Losses

$$d_d \leq M \frac{d_{res}}{2}$$

$$M_{opt} \geq 2 \frac{d_d}{d_{res}}$$

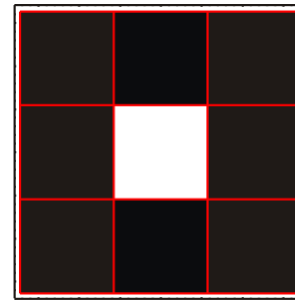
CCD camera:

$$d_{res} = 0.25 \mu m$$

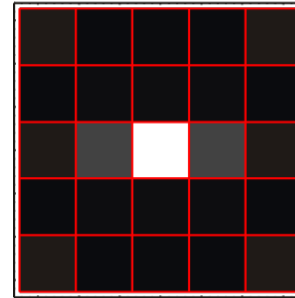
$$d_d = 10 \mu m$$

$$\rightarrow M_{opt} \geq 80$$

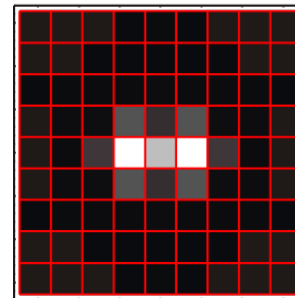
under-sampling



$$d_d = 1.5 d_{res}$$

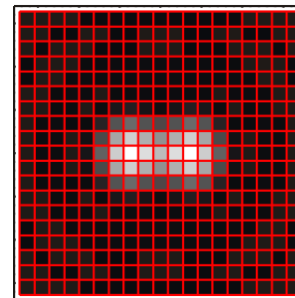


$$d_d = 0.9 d_{res}$$



$$d_d = 0.5 d_{res}$$

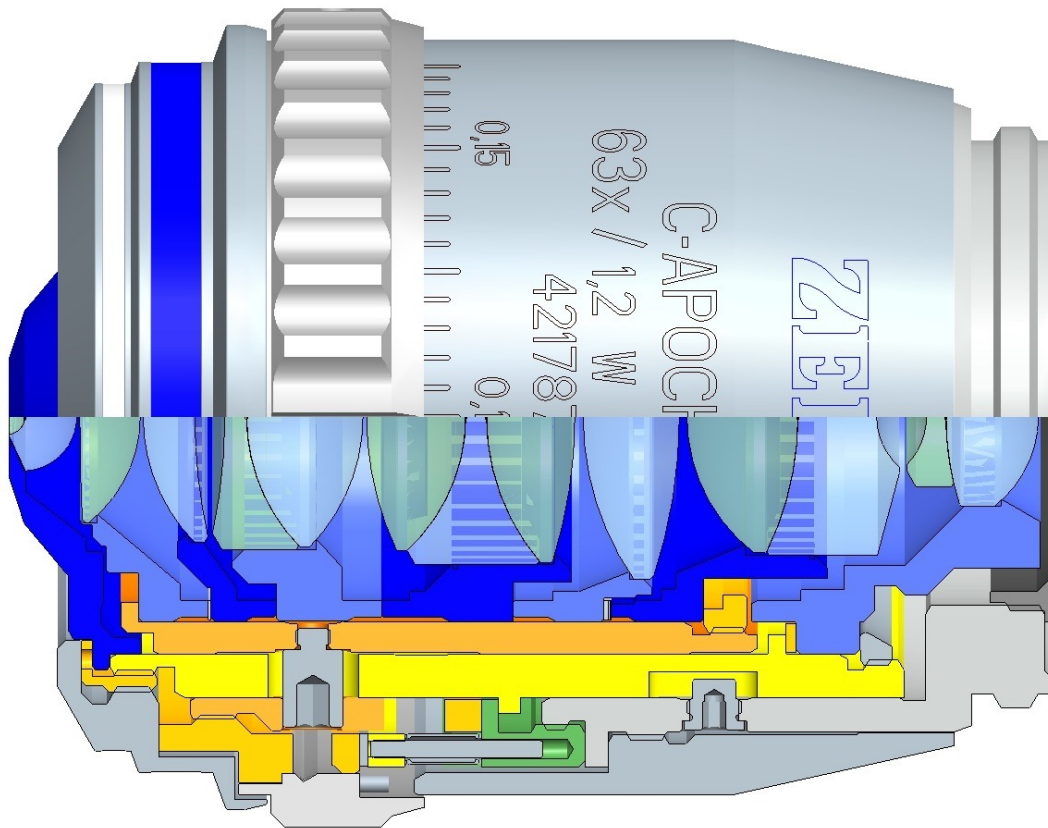
over-sampling



$$d_d = 0.24 d_{res}$$

## 8. Objective lenses

# Objectives



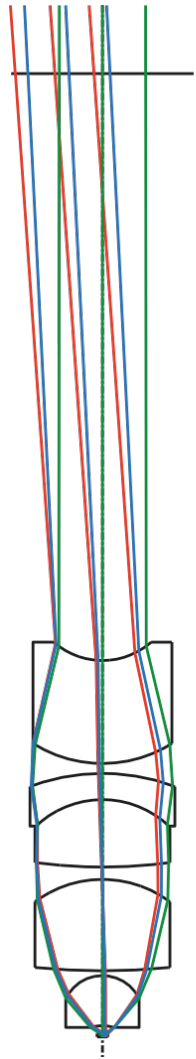
Color code	Magnification
white	100 - 160x
dark blue	60 - 63x
light blue	40 - 50x
green	16 - 32x
yellow	10x
orange	6.3x
red	4 - 5x
brown	2.5x
grey	1.6x
black	1 - 1.25x

Color code	Immersion
white	water
orange	glycerol
red	Multi-immersion
black	oil

With kind permission by Carl Zeiss Microscopy GmbH

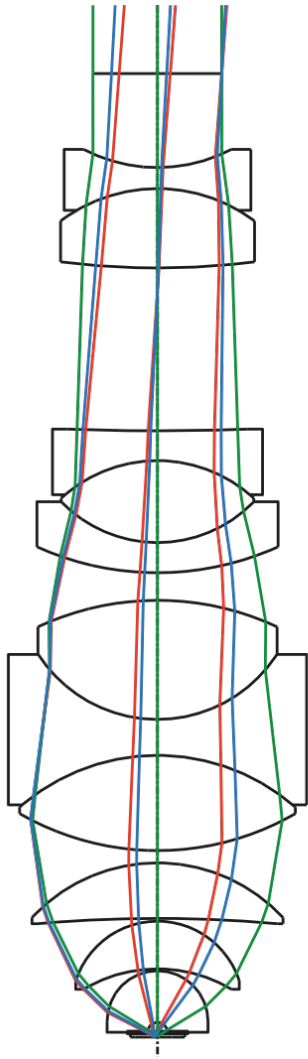


# Objective Lens Classes



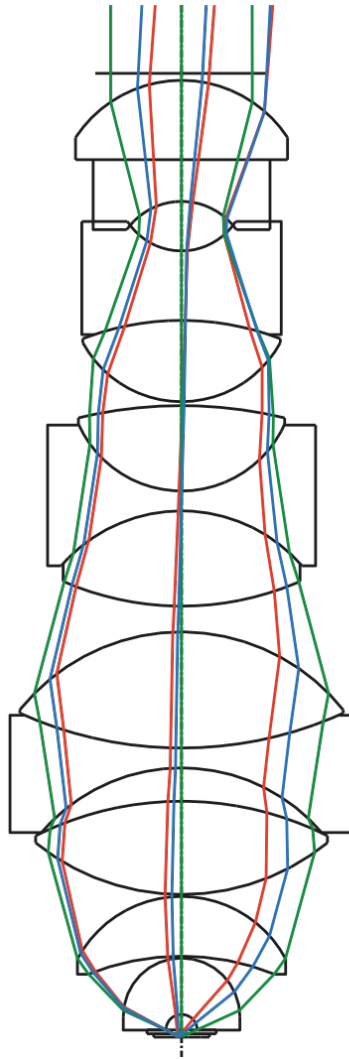
N-Achroplan NA 0.85

air immersion;



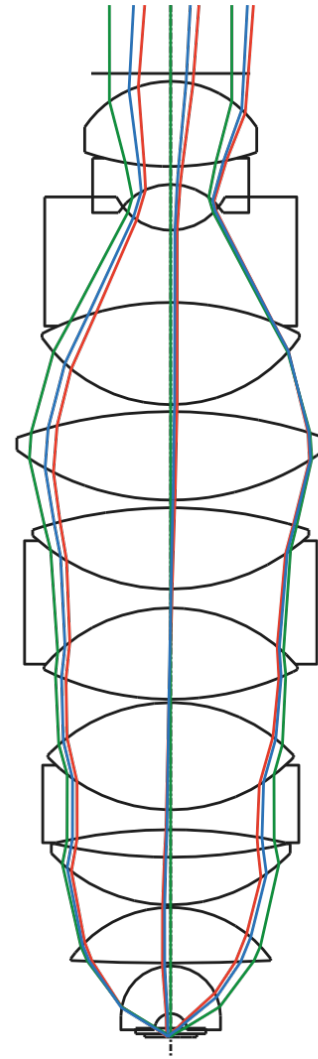
Plan-Neofluar NA 1.25

oil immersion



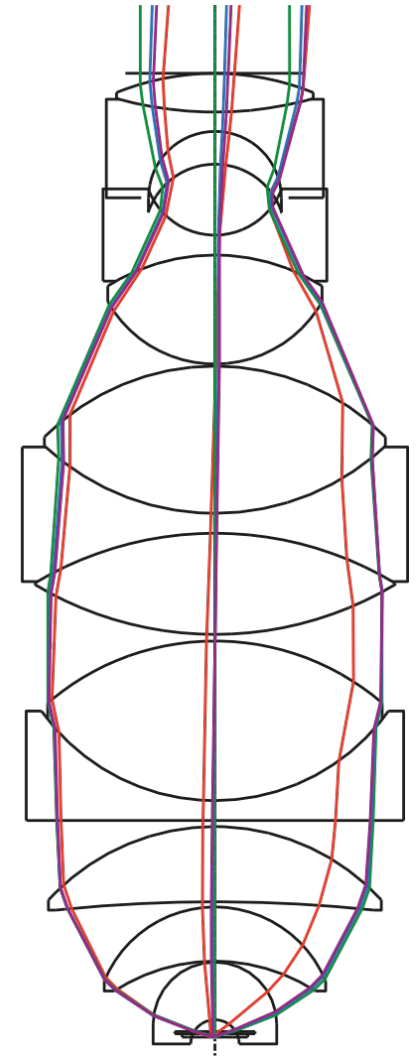
Plan-Apochromat NA 1.4

oil immersion



C-Apochromat NA 1.2

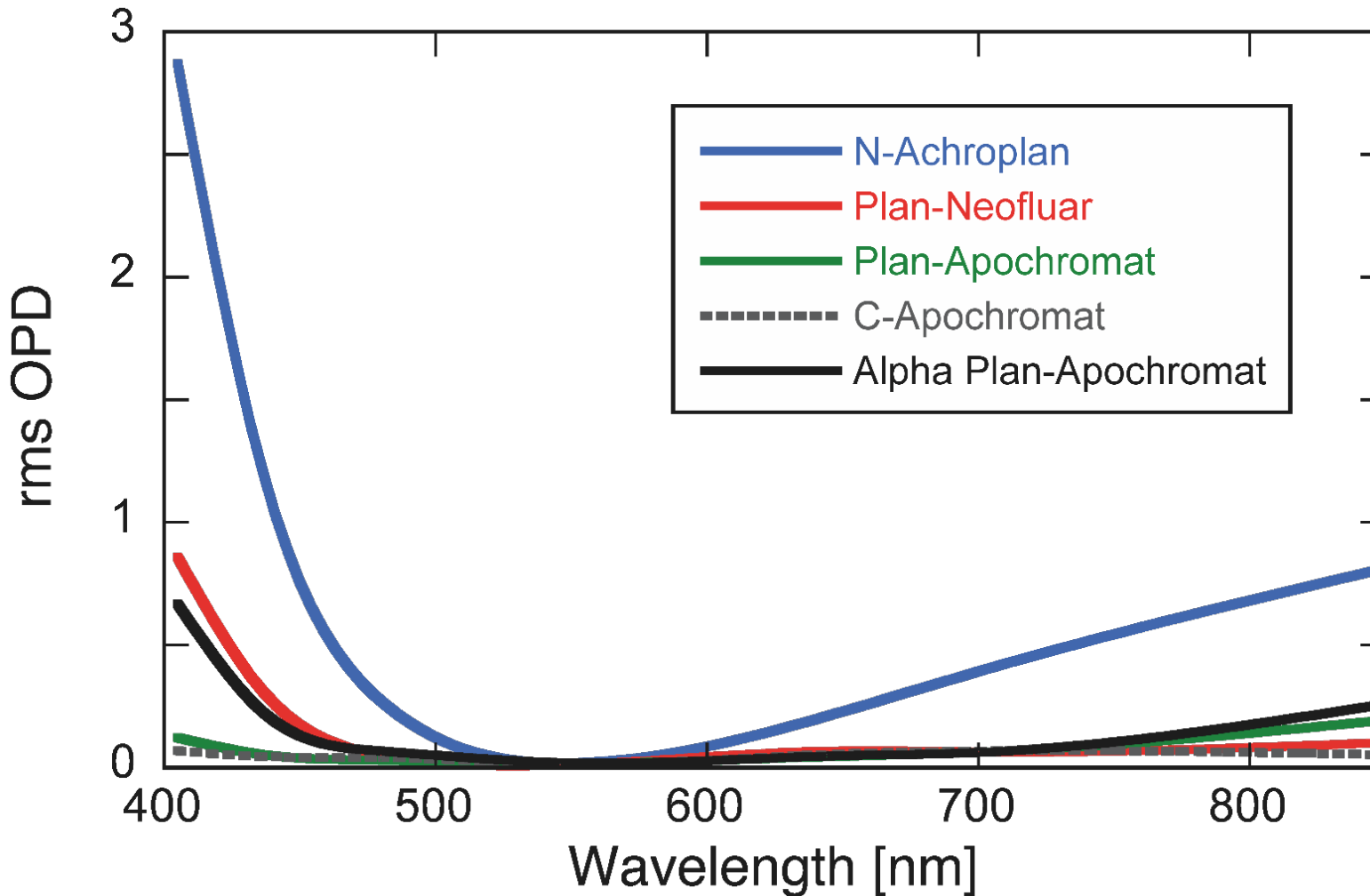
water immersion



Alpha Plan-Apochromat NA 1.4

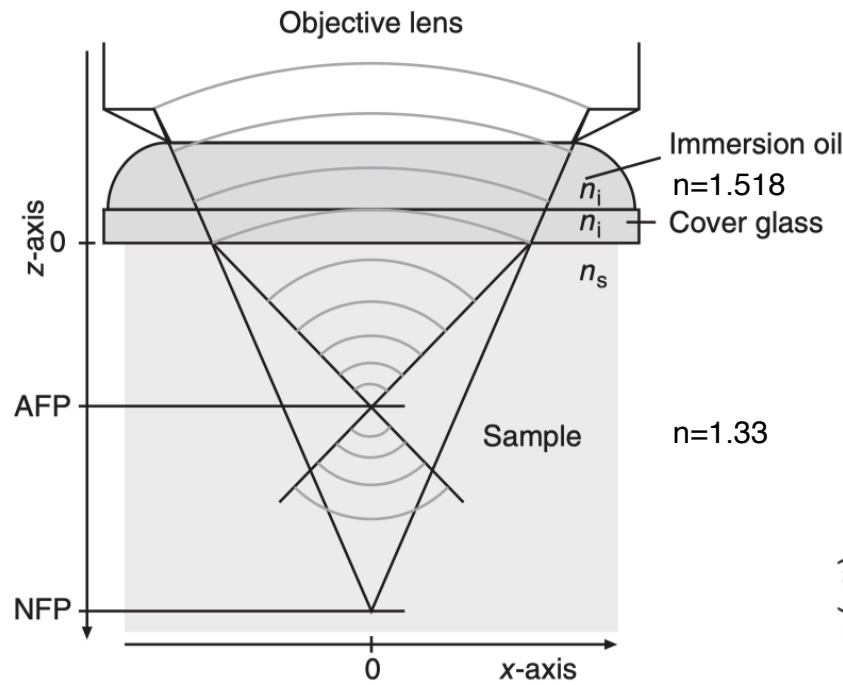
oil immersion

# Optical Correction of Objectives

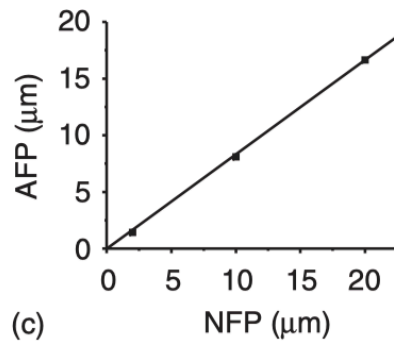


Comparison of the degree of correction for the objectives shown above in terms of the root-mean-square deviations of the optical path length difference (rms-OPD) in the exit pupil of the objective plotted as a function of the wavelength

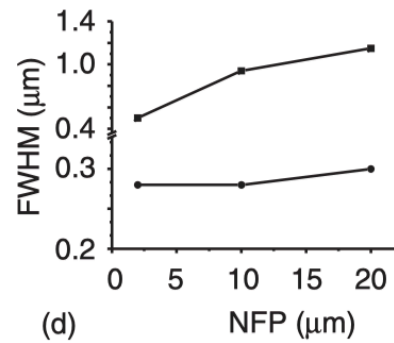
# Using an oil immersion objective for imaging in water



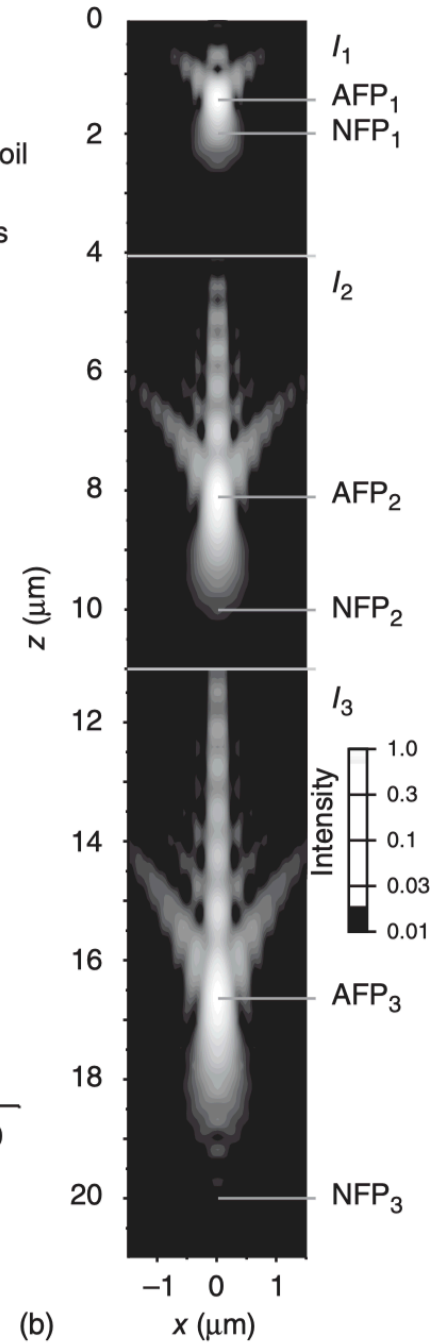
(a)



(c)



(d)



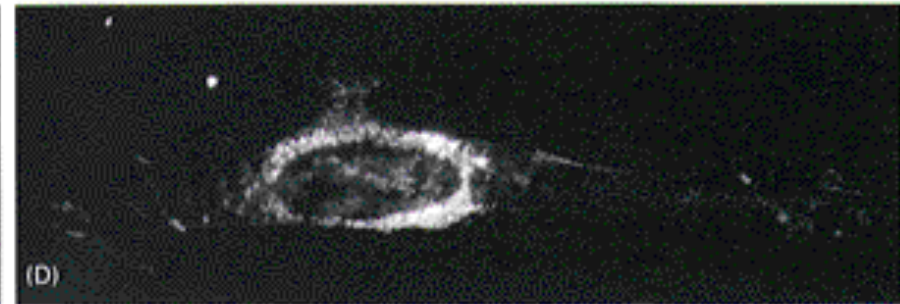
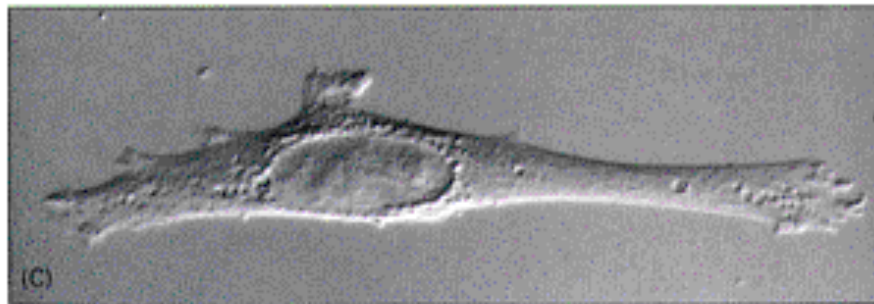
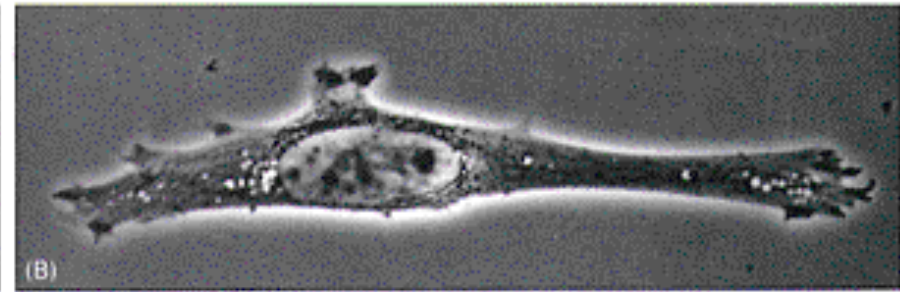
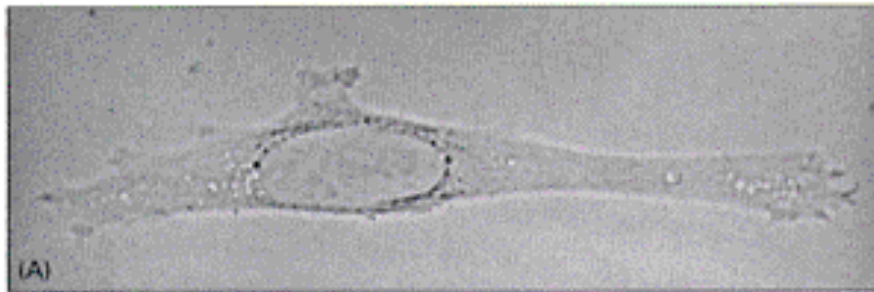
(b)

objective NA 1.3

# The contrast problem: physical contrast techniques

bright field

phase contrast



50  $\mu\text{m}$

Differential interference contrast (DIC)

dark field

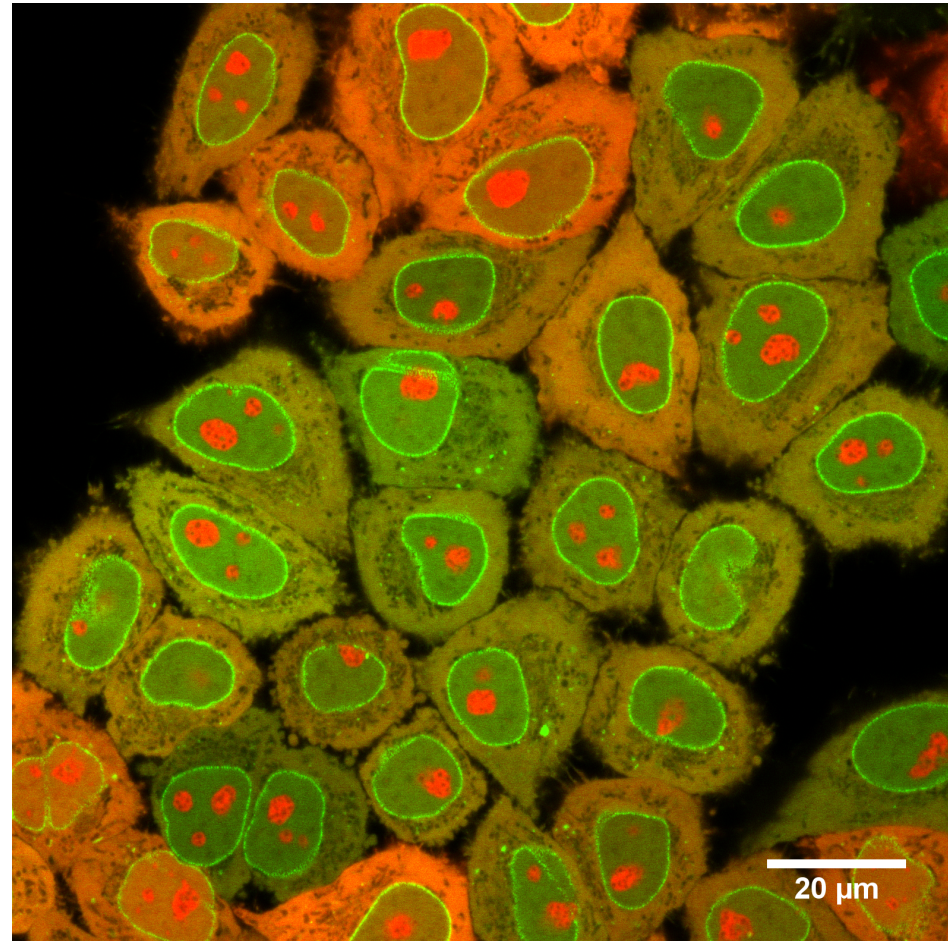
⇒ Image contrast is no inherent object property!

## 9. Fluorescence

# Advantages of Fluorescence Microscopy

---

- specific labeling
- excellent contrast
- in vivo observation
- observation of dynamics

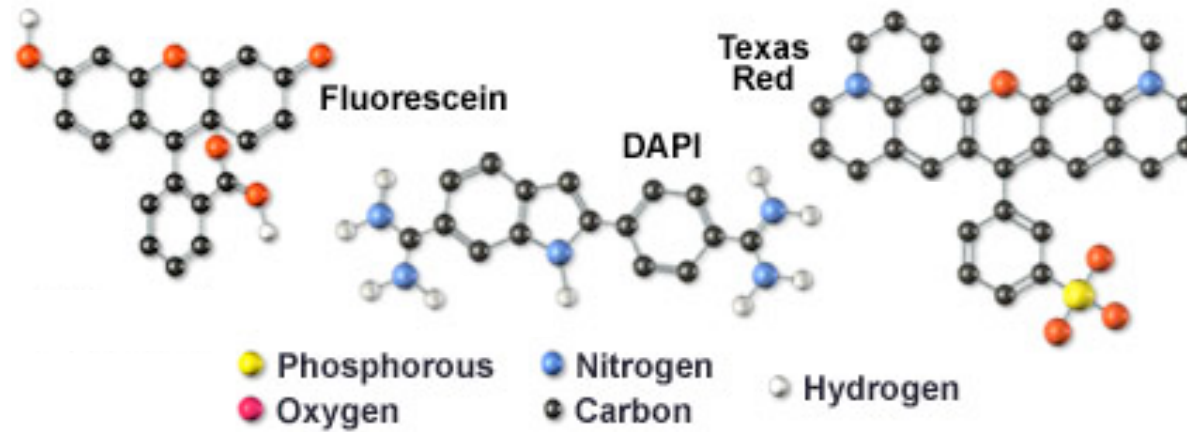


green: nuclear envelope labeled by NTF2-GFP  
red: large ribosomal subunits labeled by eIF6-Halo

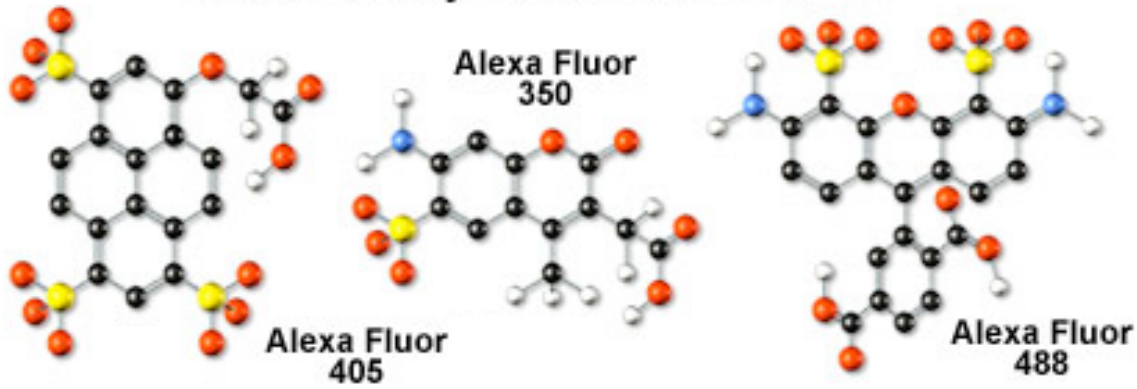


# Fluorescent dyes

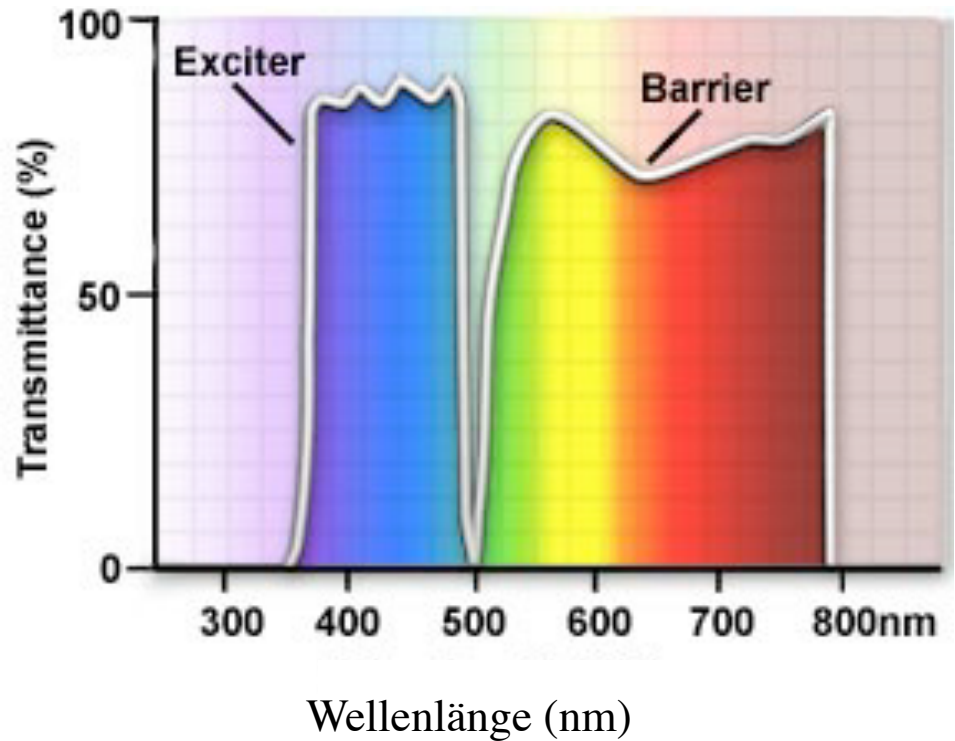
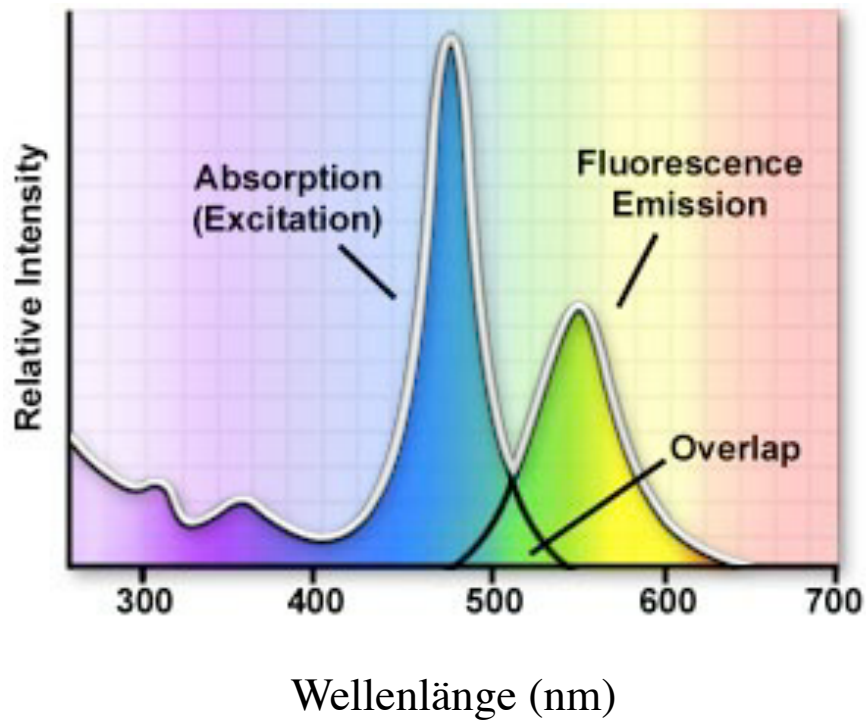
↳ length  $\approx$  1.3 nm



## Alexa Fluor Synthetic Fluorochromes



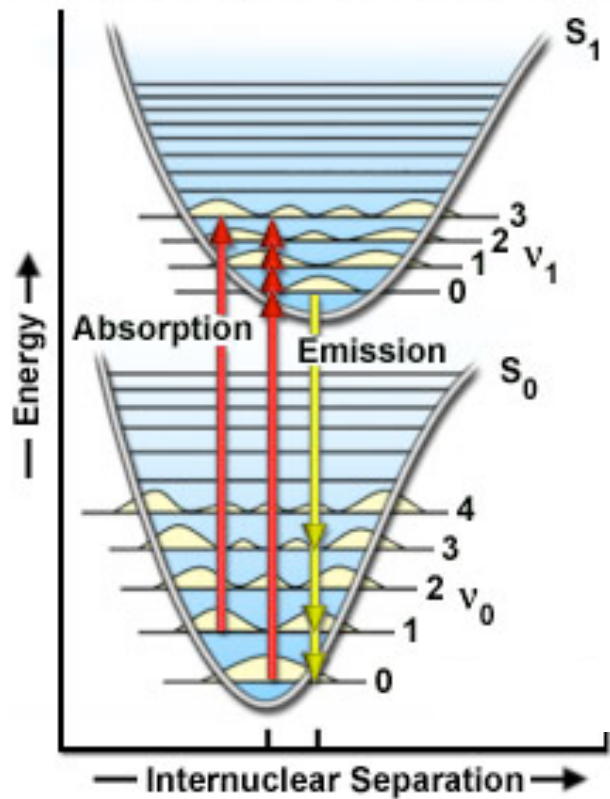
# Absorption and emission spectra & corresponding band pass filters



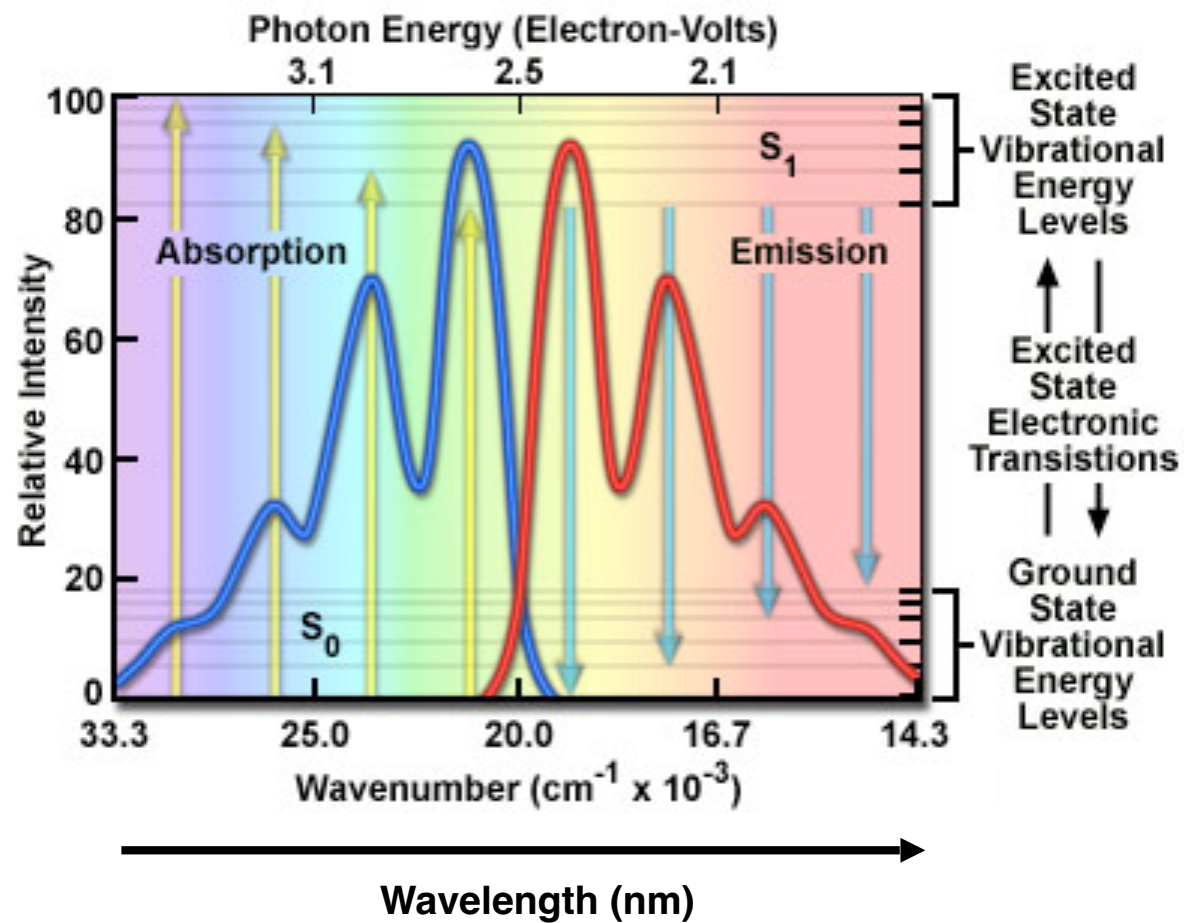


# Stokes shift and mirror image rule

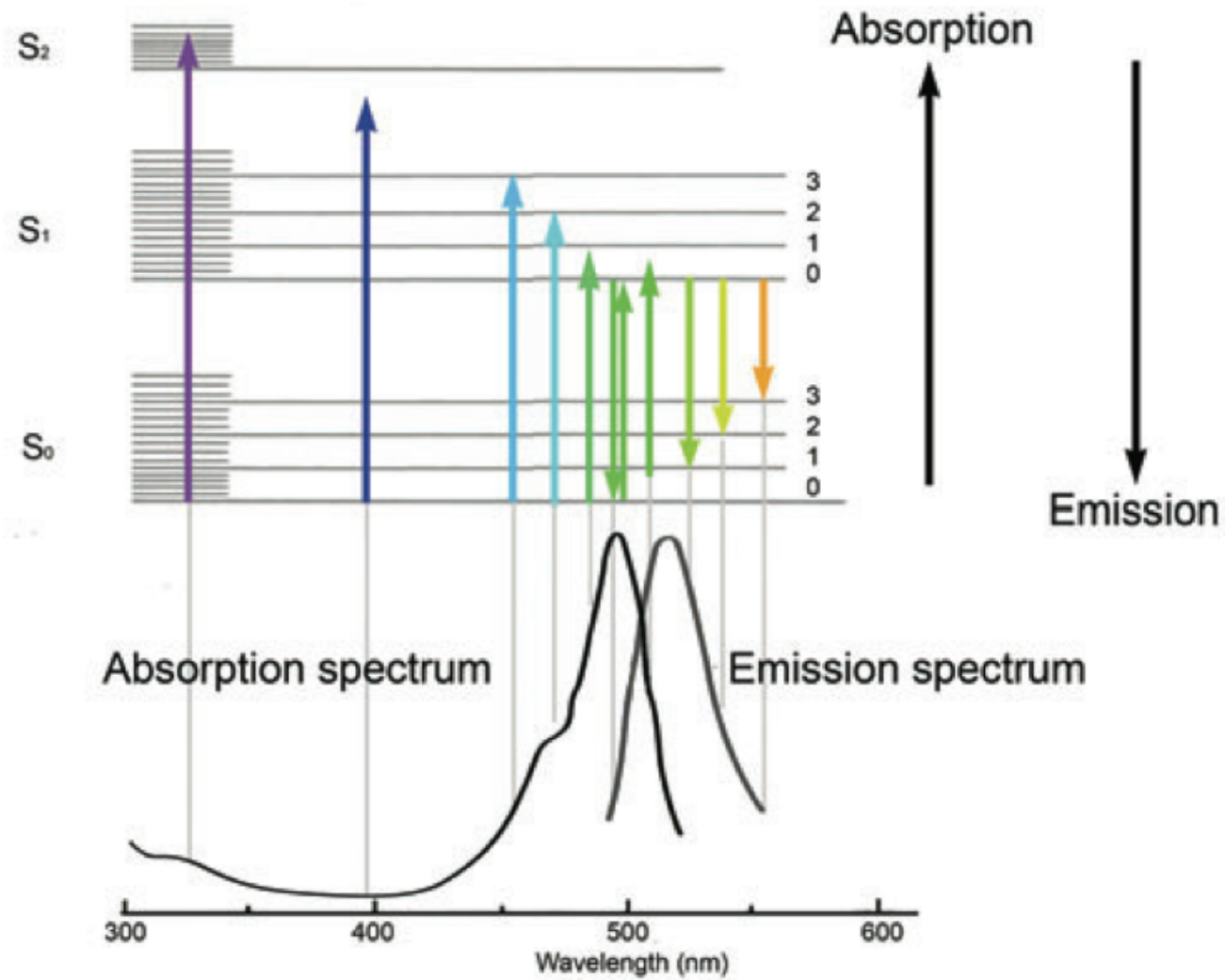
Franck-Condon Energy Diagram



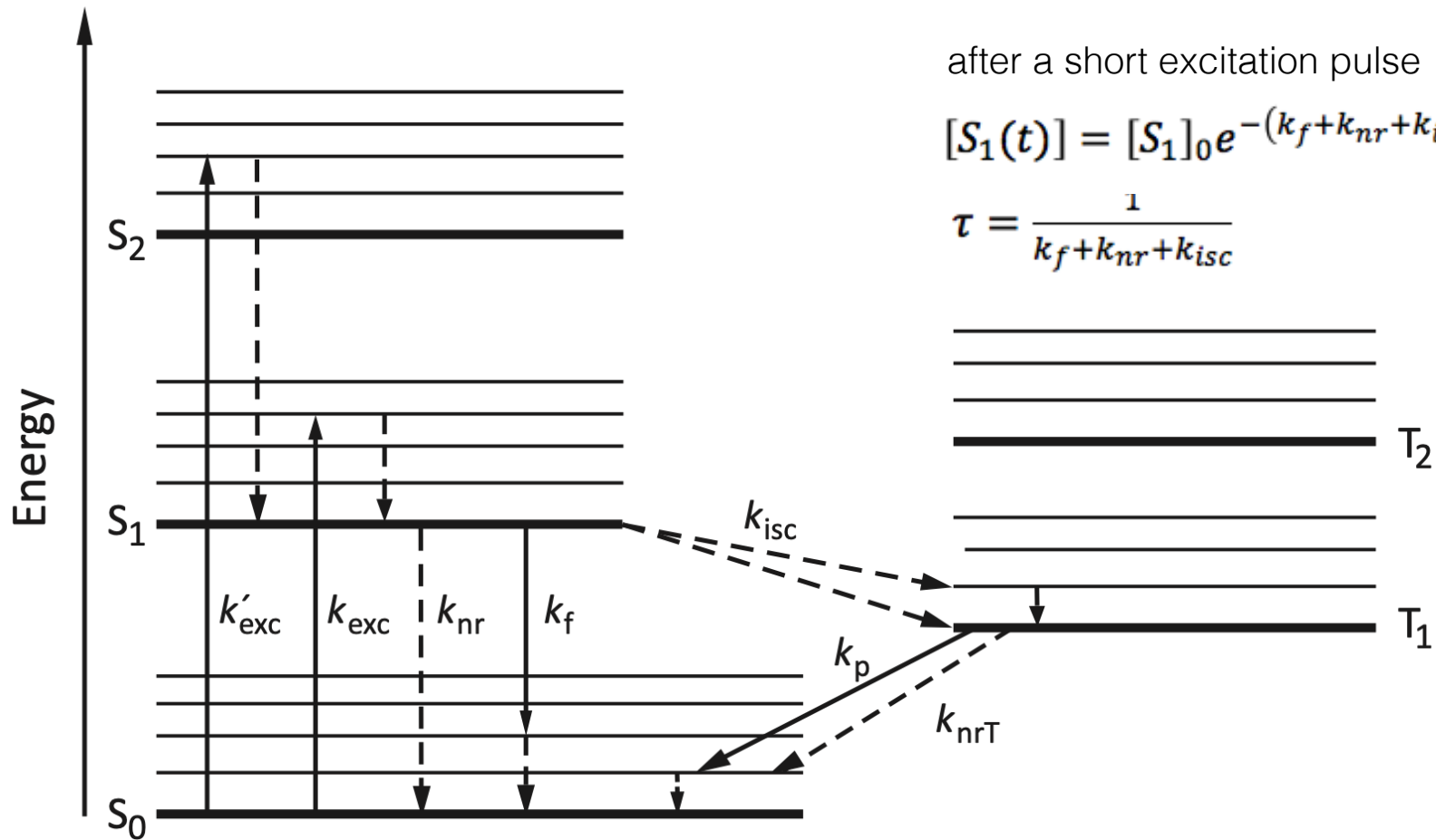
Electronic Absorption and Emission Bands



# Jablonski diagram



# Jablonski diagram



after a short excitation pulse

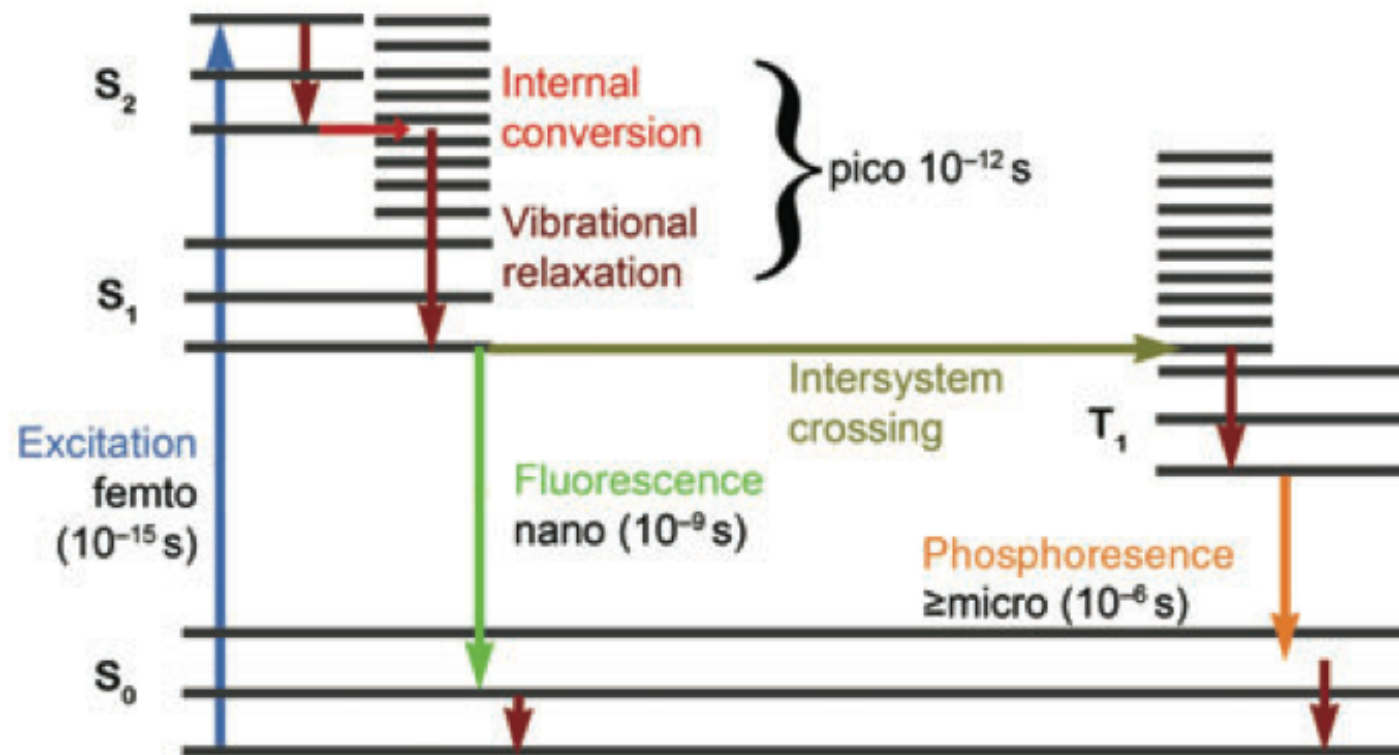
$$[S_1(t)] = [S_1]_0 e^{-(k_f+k_{nr}+k_{isc})t}$$

$$\tau = \frac{1}{k_f+k_{nr}+k_{isc}}$$

„quantum efficiency“

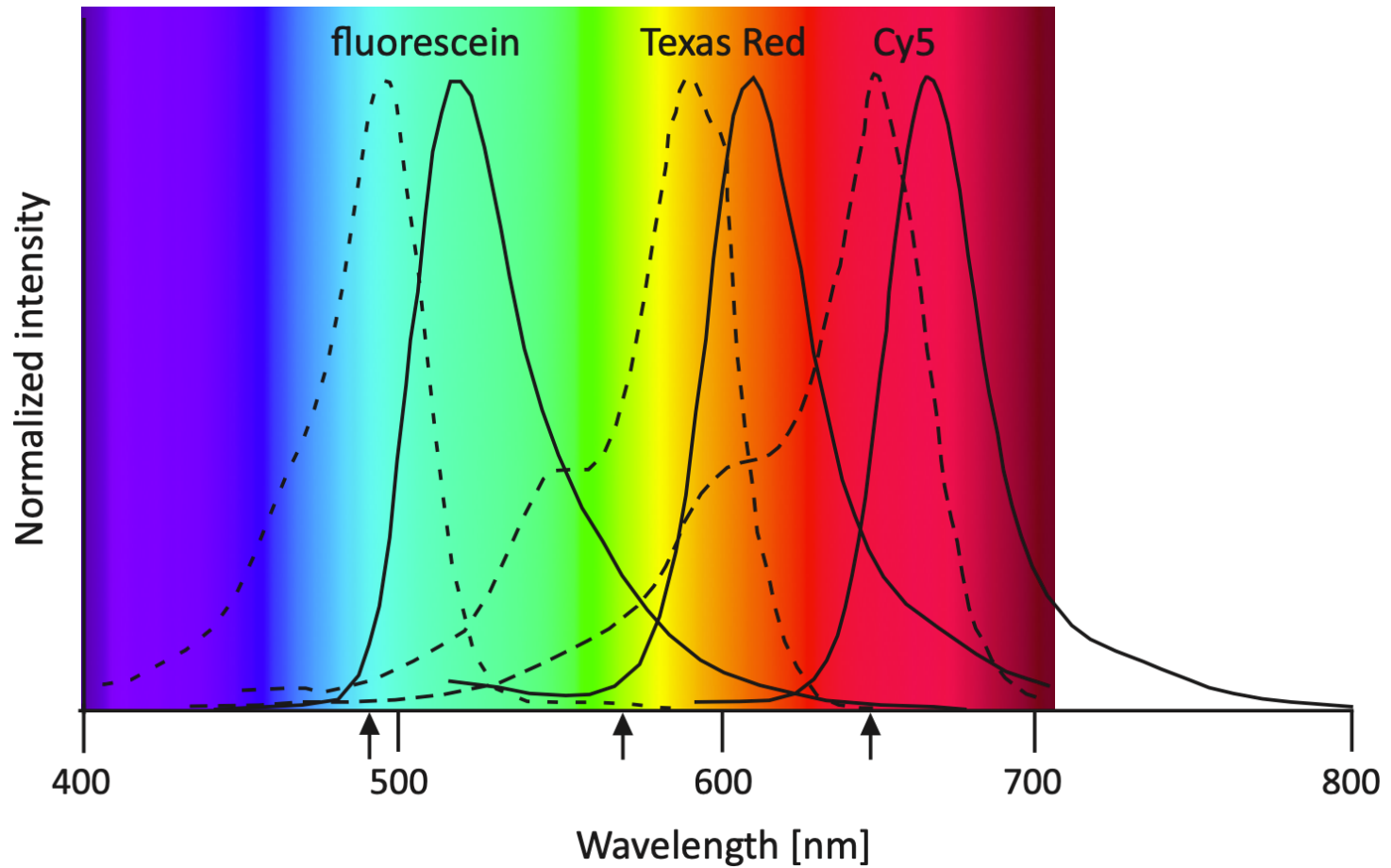
$$\Phi = \frac{k_f}{k_f+k_{nr}+k_{isc}}$$

# Time scales of relaxation processes



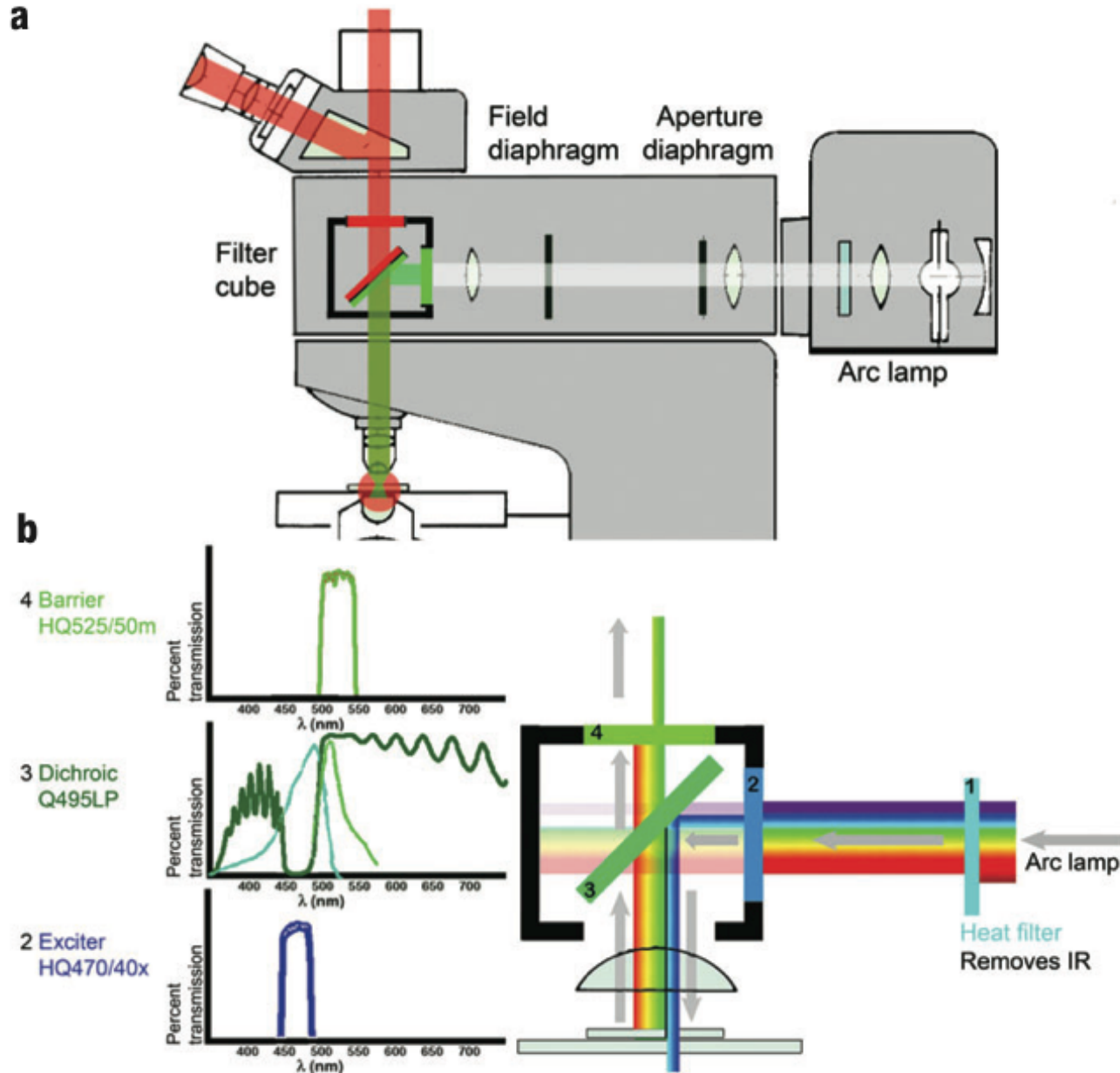
# Fluorescence spectra

---

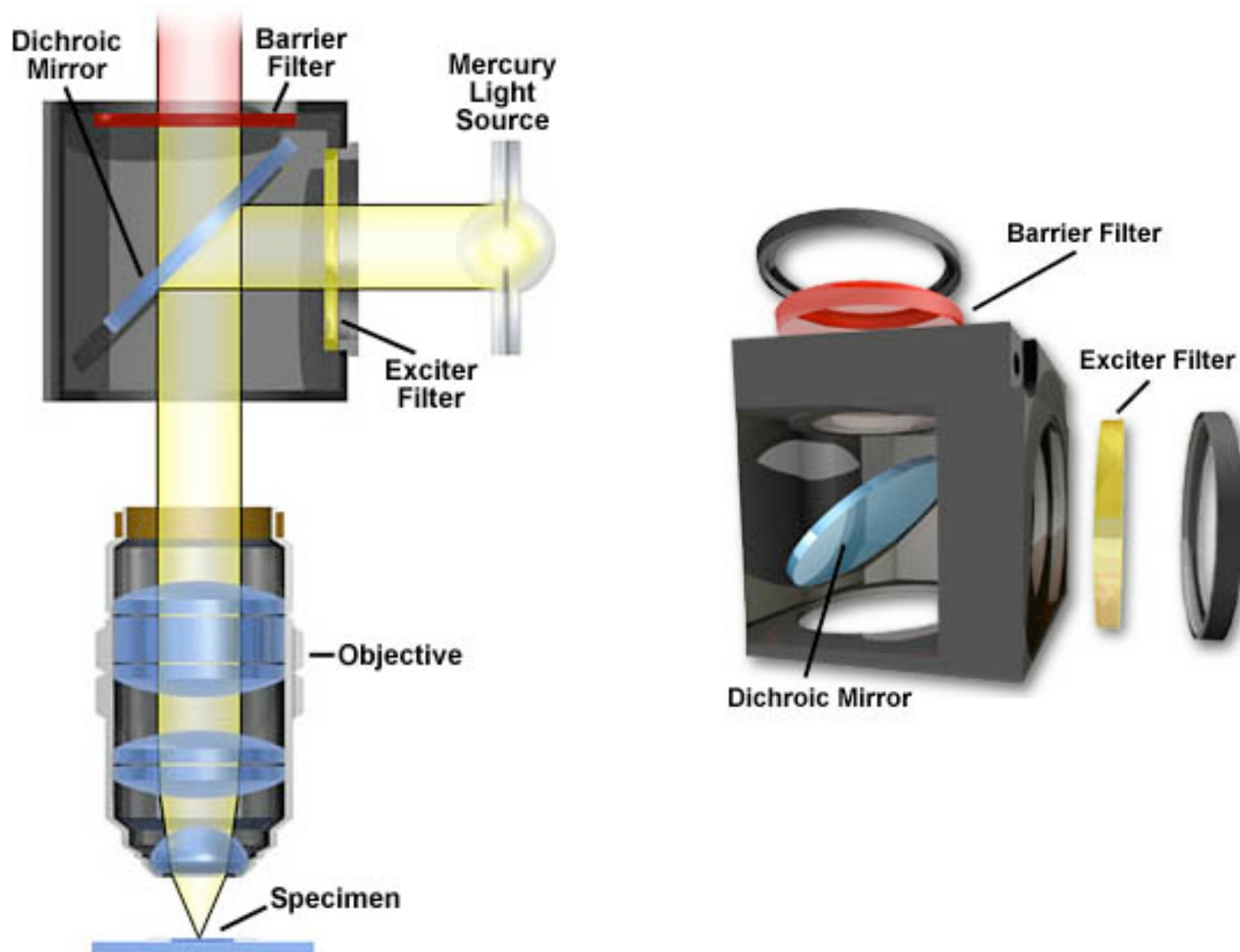


## 10. Fluorescence microscopy

# Upright fluorescence microscope



# Beam splitting cube

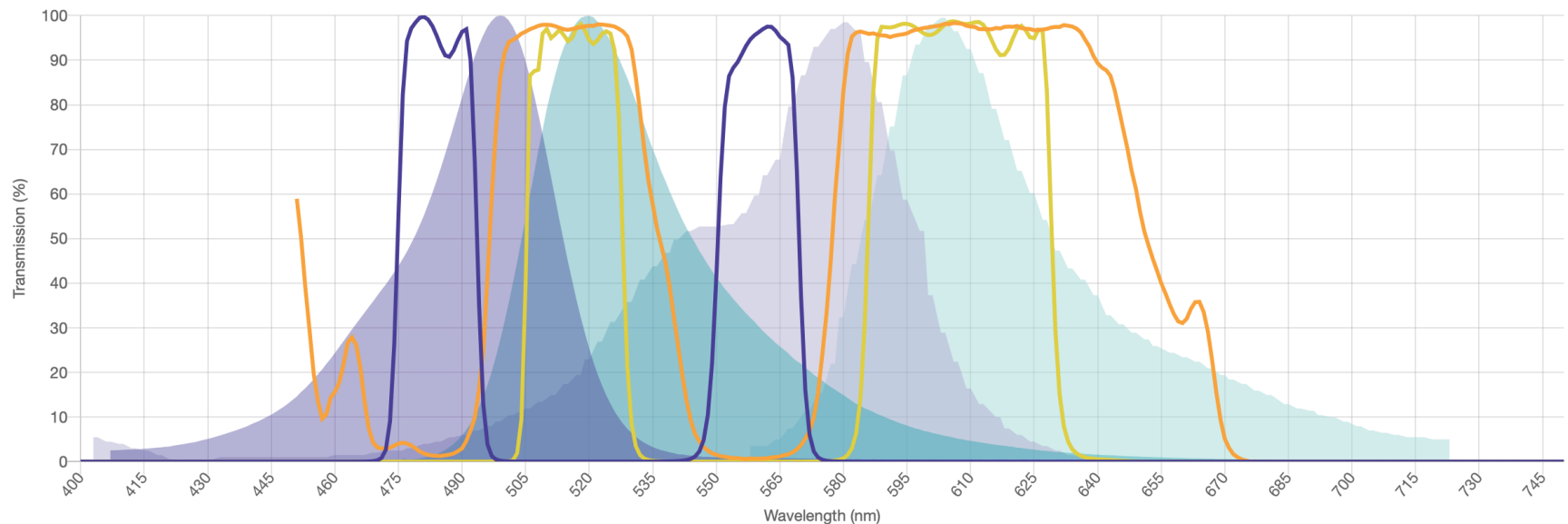




# How to find the correct filters for your fluorophore

<https://www.omegafilters.com/curvomatic/>

## Curvomatic Fluorescence Spectral Viewer



### Filters and Curves

Wavelength  to  nm

(Click and drag for horizontal scroll)

#### Fluorescence Sets

**XF452 FITC/ALEXA FLUOR 568 DUAL BAND PREMIUM FLUORESCENCE FILTER SET**

485-560DBEX:  --- %T at --- nm  
485-560DBDR:  --- %T at --- nm  
520-610DBEM:  --- %T at --- nm

#### Fluorophores

**ALEXA FLUOR® 488**

Excitation:  --- % at --- nm  
Emission:  --- % at --- nm

**ALEXA FLUOR® 568**

Excitation:  --- % at --- nm  
Emission:  --- % at --- nm

Alternative:

[Spectra Viewer](#) by the MPI for Brain Research, Frankfurt, Germany

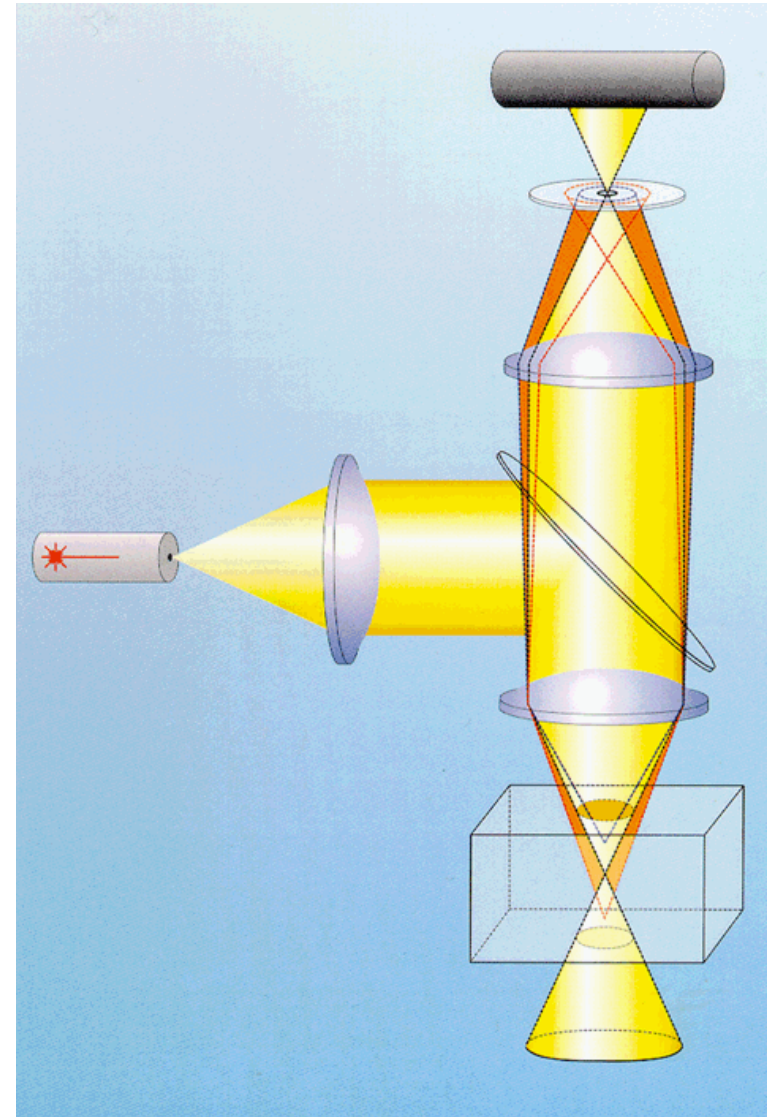
## II. Confocal microscopy

# The confocal principle

---

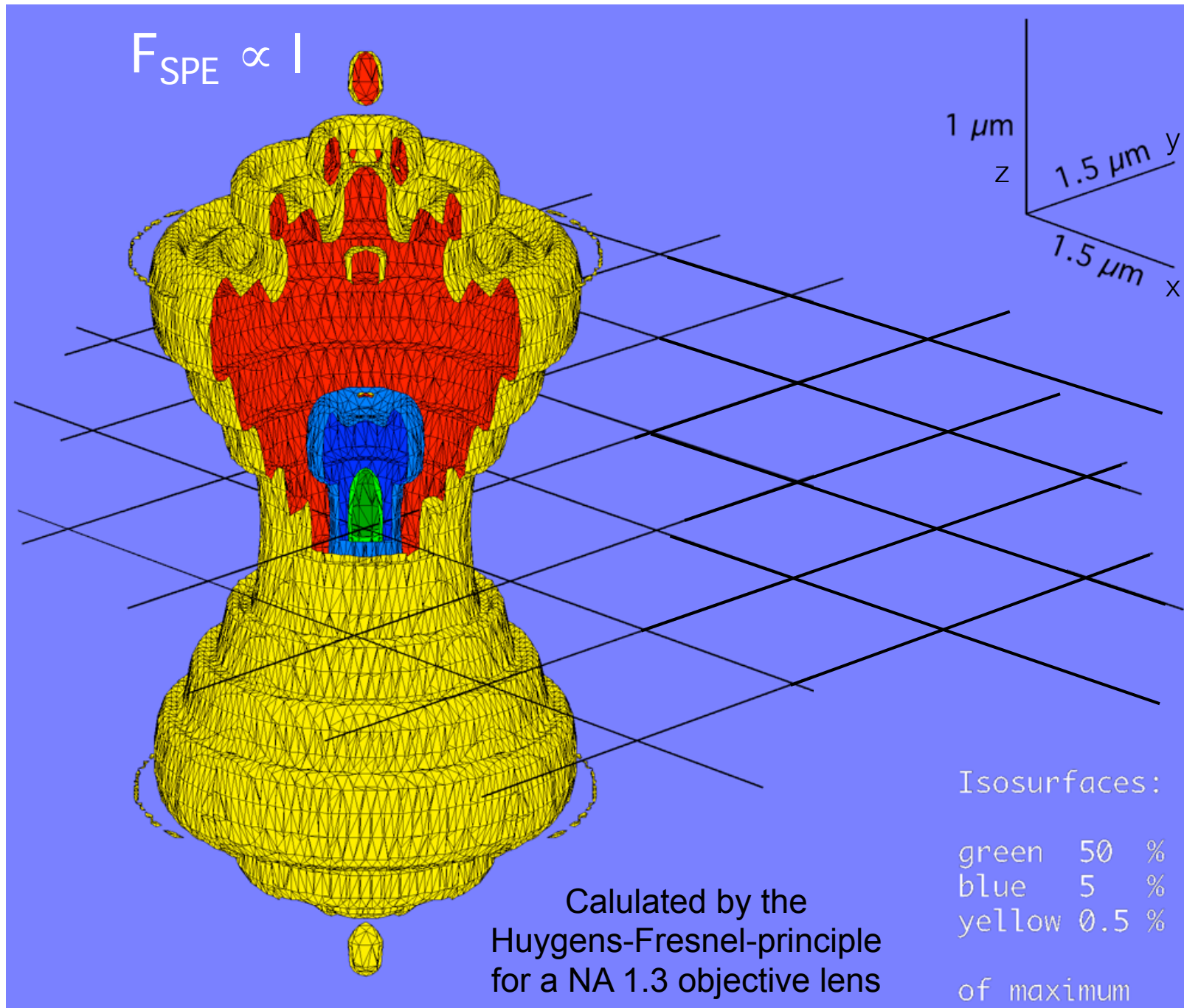
Combination of focussed laser illumination  
and  
detection through in pinhole placed in a  
conjugated optical plane

yields efficient background subtraction  
and axial resolution:  
„Optical Sectioning“



# 1-Photon Excitation Profile

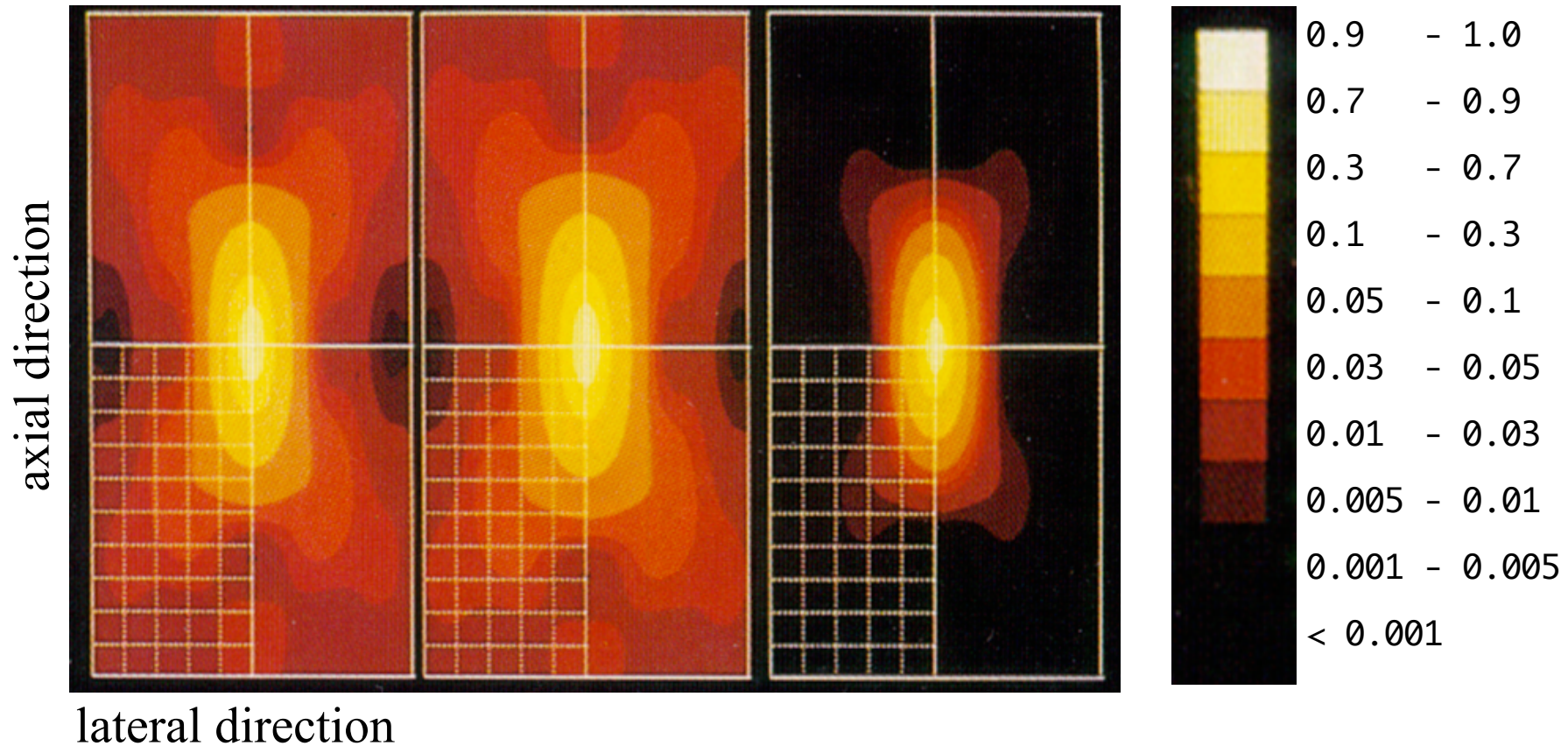
SPE,  $\lambda=488$  nm





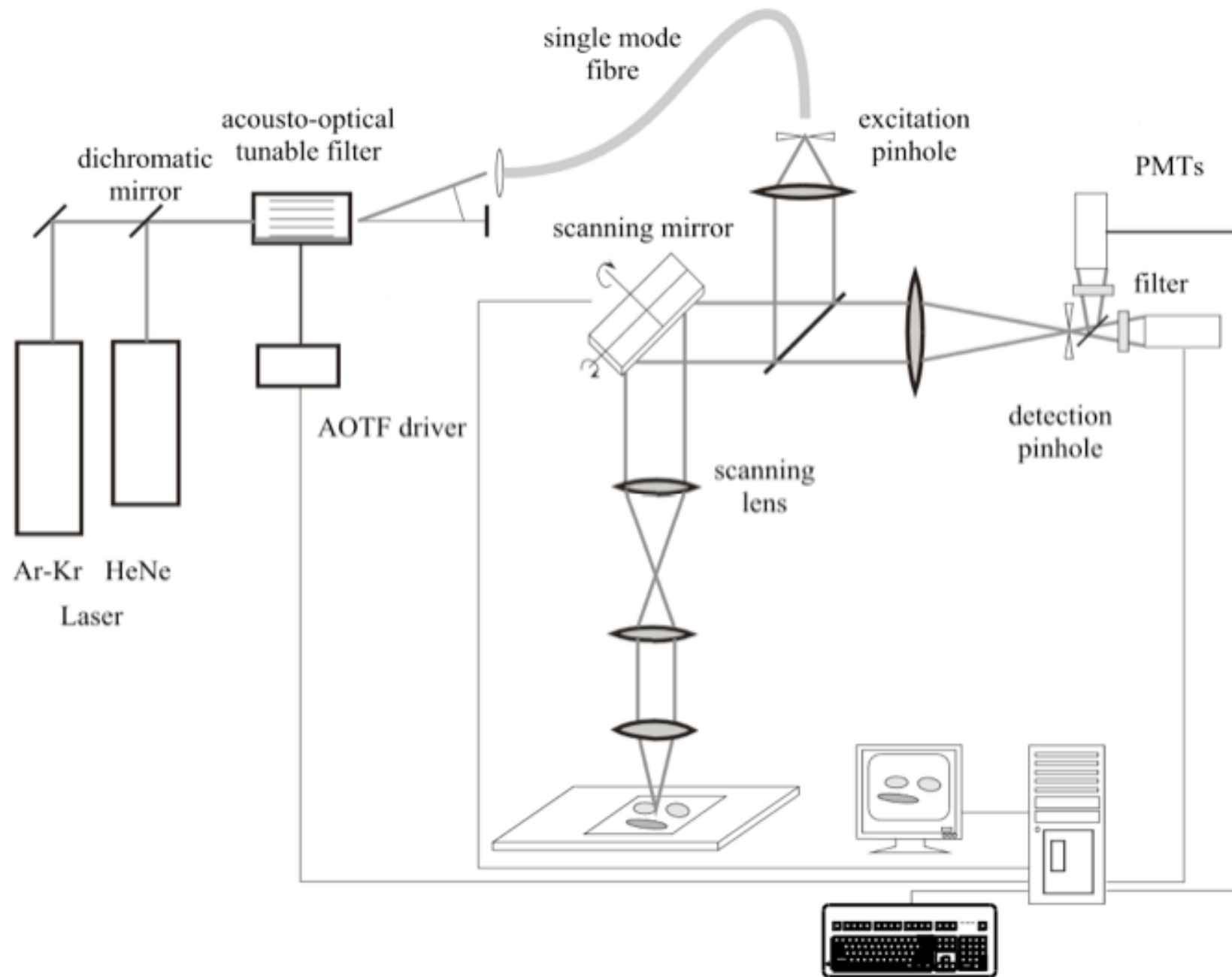
# Confocal point spread function

Excitation 488 nm Fluorescence 525 nm

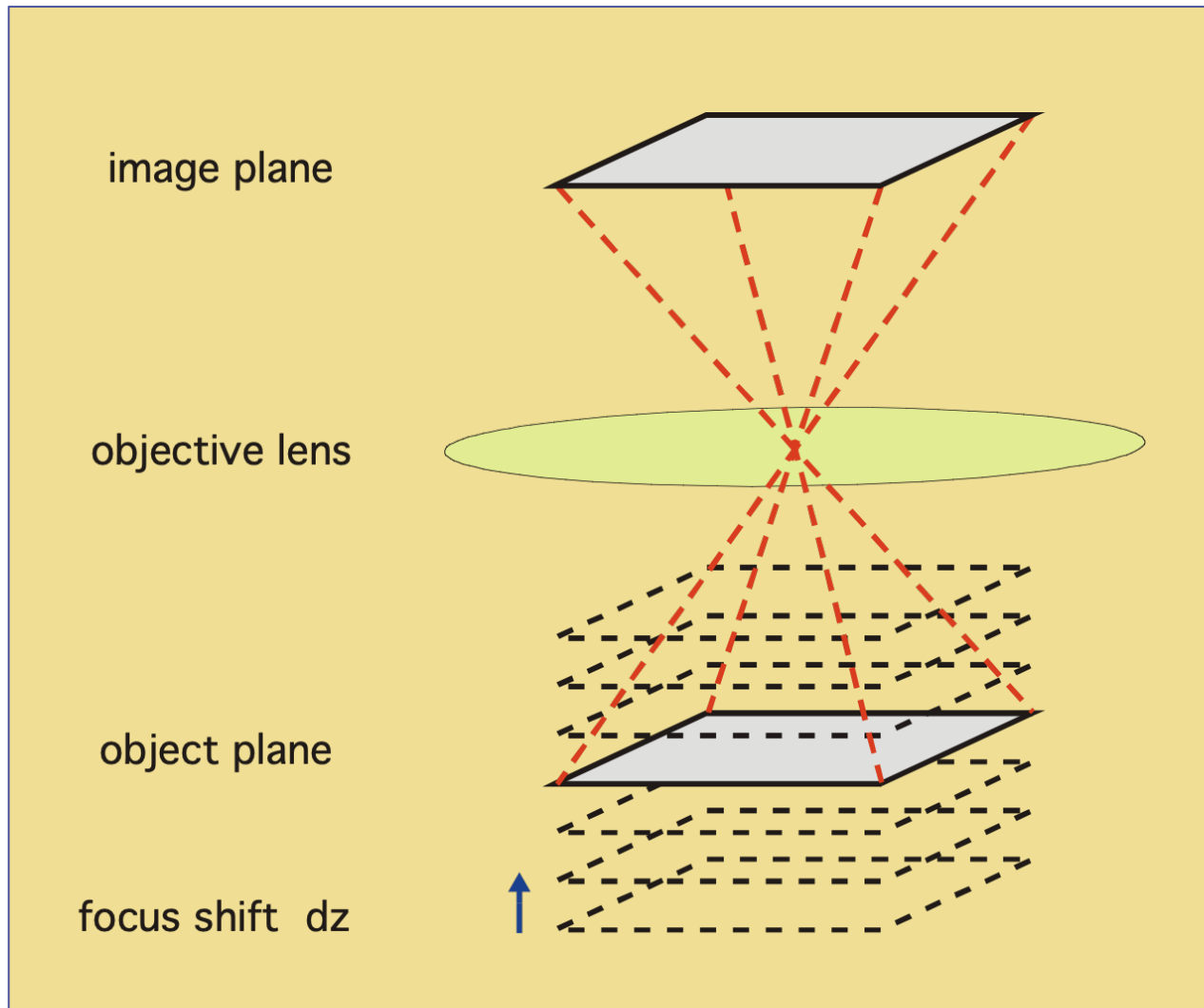


Objective 100X NA 1.32  
100 nm/division

# Scheme of a point scanning confocal microscope

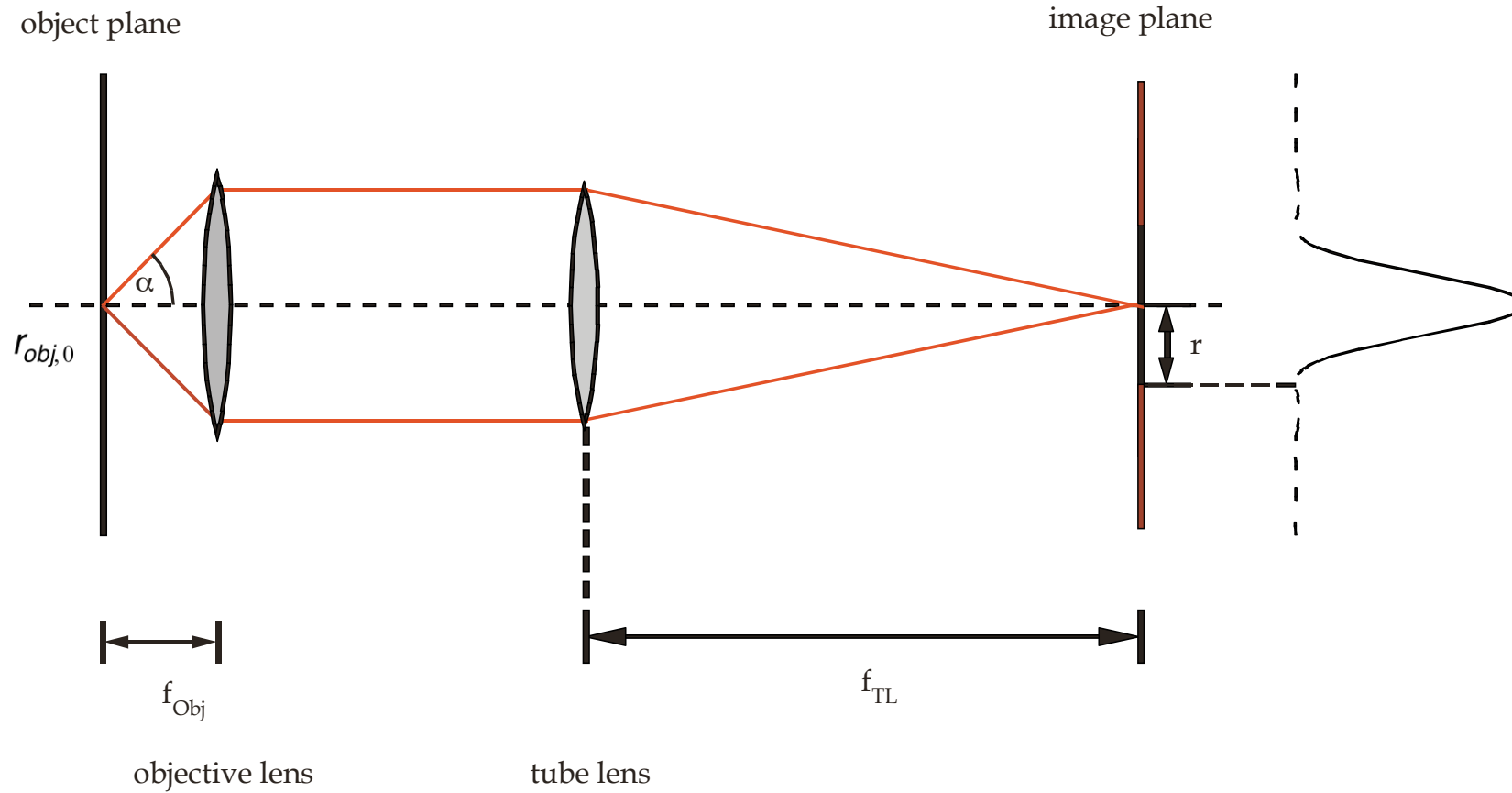


# Acquisition of optical slices



Alternatives: shift of object or shift of objective

# Role of the detection pinhole



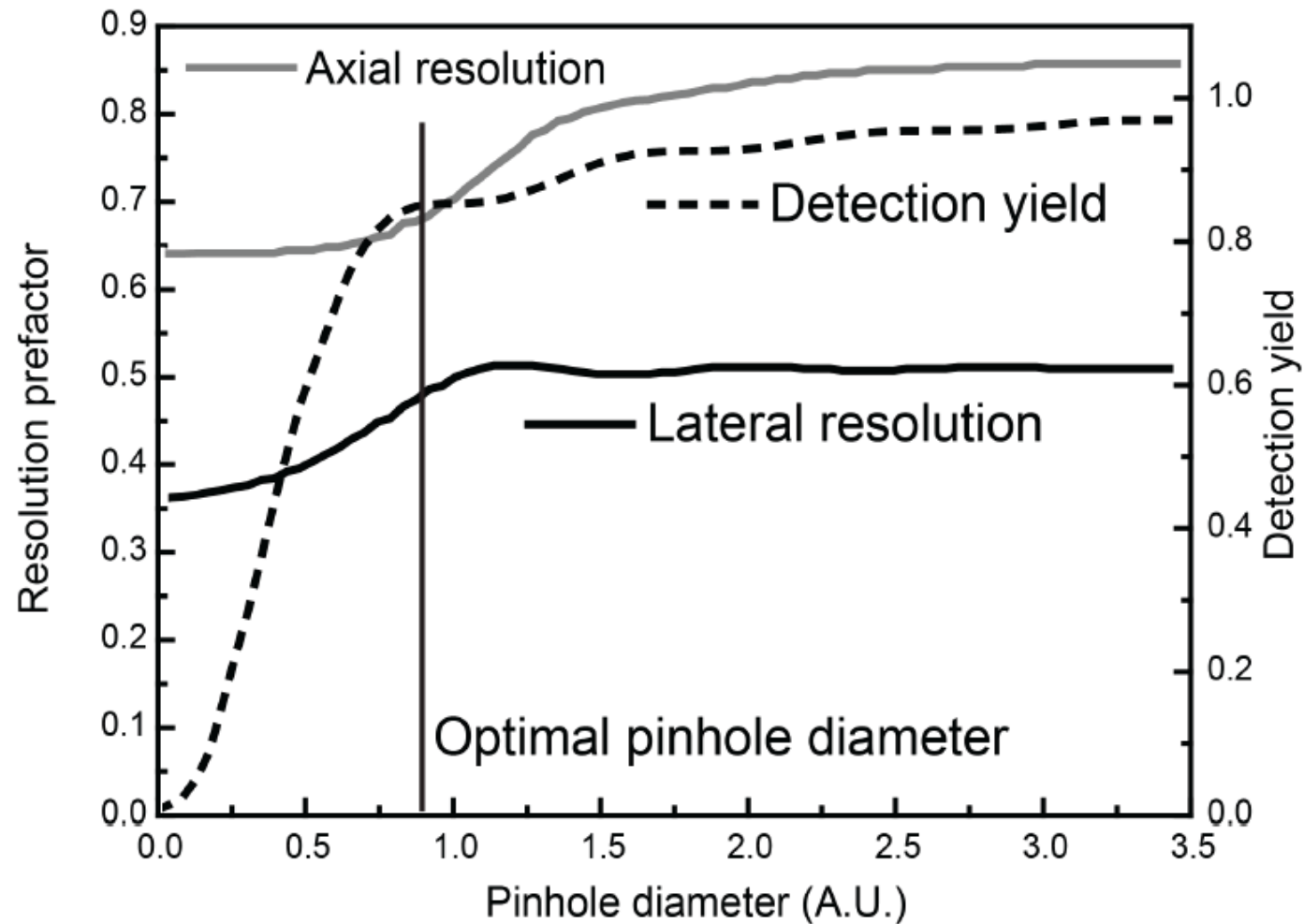
$\alpha$ : opening angle of the objective lens divided by 2  
 $n$  the refractive index of the medium in front of the objective lens.

$$r_{obj,0} = \frac{0.61 \lambda}{n \sin \alpha}$$

$$NA_{Obj} = n \sin \alpha$$

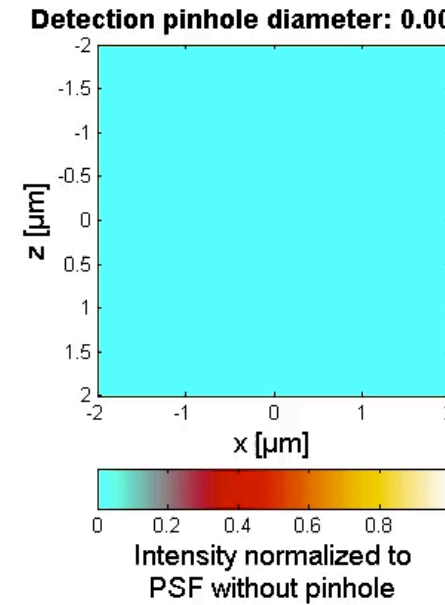
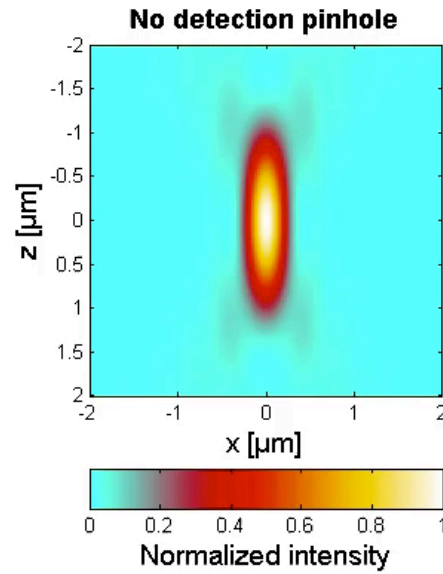


# Detection yield, axial and lateral resolution as function of detection pinhole diameter

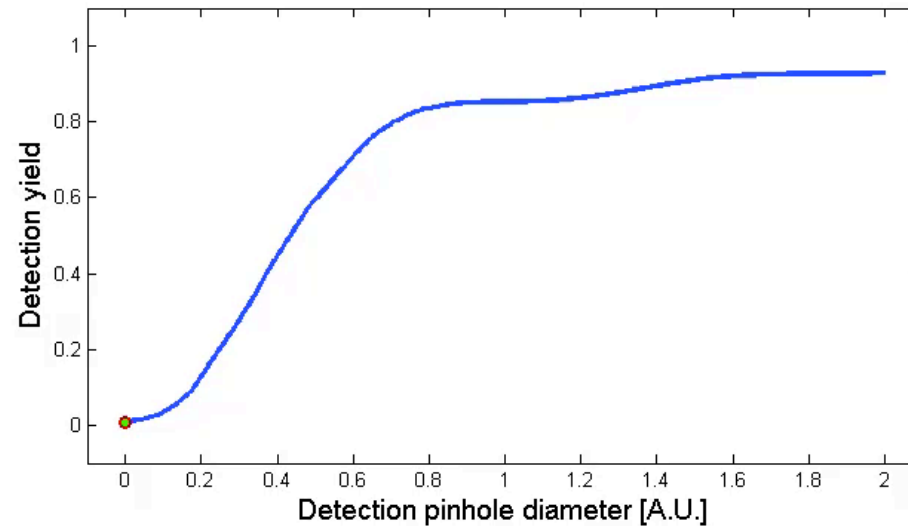


# Confocal Point Spread Function (PSF) as Function of Pinhole size

Excitation PSF without pinhole



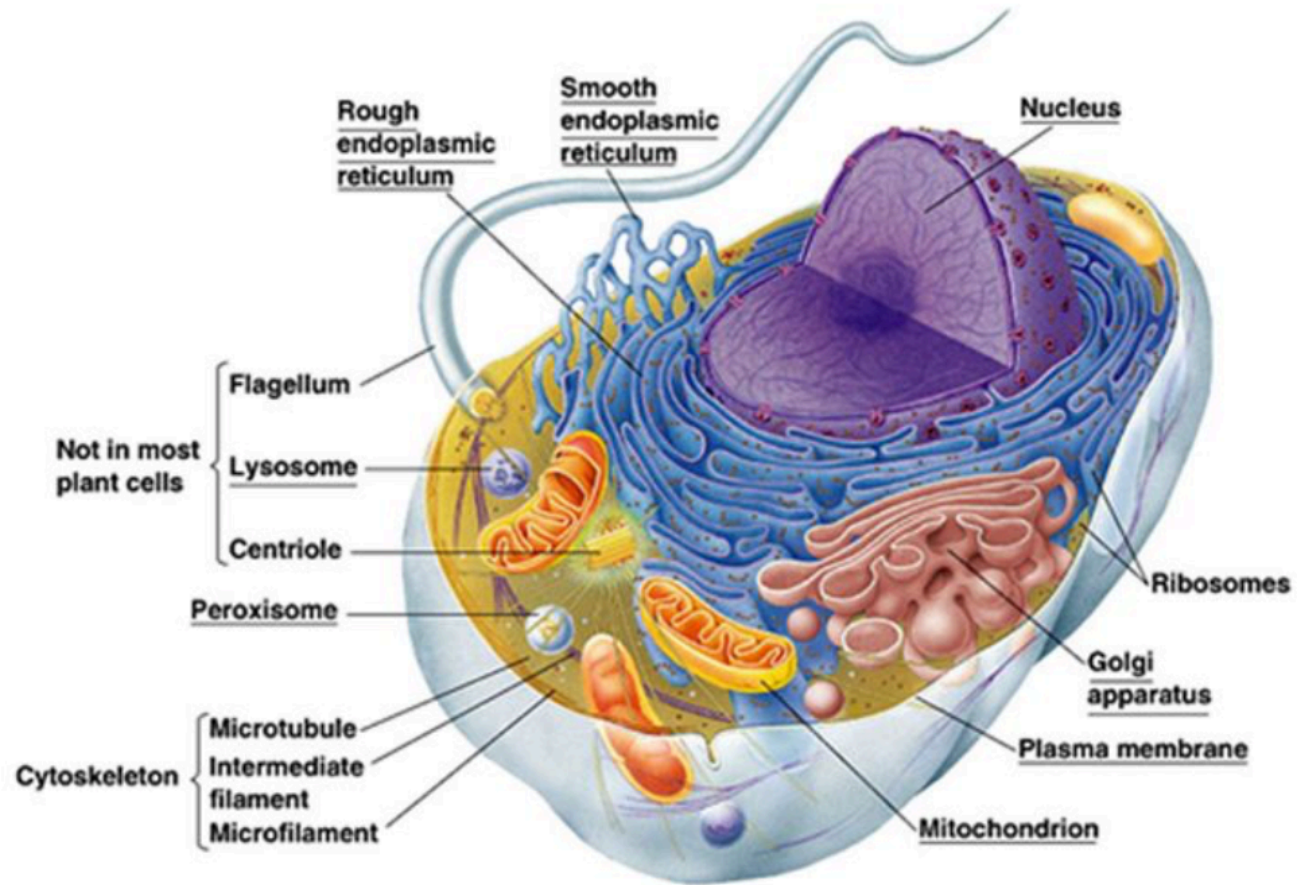
total PSF



Fraction of light that is transmitted through the pinhole is shown with the green cursor marking the current pinhole size for the calculated PSF. A smaller pinhole size yields a higher overall resolution, but at a significant loss in detection yield.

# Example: nuclear pore complexes in the nuclear envelope

---



# Example: nuclear pore complexes in the nuclear envelope

---

